SOLDER JOINT RELIABILITY & PROGNOSTICATION OF LEAD FREE ELECTRONICS IN HARSH THERMO-MECHANICAL

ENVIRONMENTS

Except where reference is made to the work of others, the work described in this thesis is my own or was done in collaboration with my advisory committee. This thesis does not include proprietary or classified information.

Chandan G Bhat

Certificate of Approval:

Jeffrey C. Suhling Quina Distinguished Professor Mechanical Engineering Pradeep Lall, Chair Thomas Walter Professor Mechanical Engineering

Roy W. Knight Assistant Professor Mechanical Engineering Joe F. Pittman Interim Dean Graduate School

SOLDER JOINT RELIABILITY & PROGNOSTICATION OF LEAD FREE ELECTRONICS IN HARSH THERMO-MECHANICAL

ENVIRONMENTS

Chandan G Bhat

A Thesis

Submitted to

the Graduate Faculty of

Auburn University

in Partial Fulfillment of the

Requirement for the

Degree of

Master of Science

Auburn, Alabama August 9, 2008

SOLDER JOINT RELIABILITY & PROGNOSTICATION OF LEAD FREE ELECTRONICS IN HARSH THERMO-MECHANICAL

ENVIRONMENTS

Chandan Bhat

Permission is granted to Auburn University to make copies of this thesis at its discretion, upon the request of individuals or institutions at their expense. The author reserves all publication rights.

Signature of Author

Date of Graduation

THESIS ABSTRACT

SOLDER JOINT RELIABILITY & PROGNOSTICATION OF LEAD FREE ELECTRONICS IN HARSH THERMO-MECHANICAL

ENVIRONMENTS

Chandan Bhat

Master of Science, August 9, 2008 (B.E., Mumbai University, 2003)

189 Typed Pages

Directed by Dr. Pradeep Lall

The trends in the electronic packaging industry are to design smaller packages that have higher complexity, and to improve package reliability while reducing costs. These needs in the packaging industry have lead to a newer generation of chip architectures, such as: Chip Scale Packages, Plastic Ball Grid Arrays, and Flip Chips. However, despite the increased performance capabilities of these leading-edge package types, their thermo-mechanical reliability is a concern for harsh environment applications. In this study, the thermo-mechanical reliability of a new architecture (D-PackTM) has been studied using finite element methods. Life prediction relationships based on damage accumulation principles have been used to calculate the characteristic life, and has been compared with thermal shock data. Failure analysis of the tested assemblies has been conducted to correlate failure locations with predictions from FEM.

While reliability analysis of any component is critical, it is also important to monitor the condition / state of the system from time to time in order to improve the system availability and upkeep. So far, traditional health monitoring methodologies have relied on reactive methods of failure detection often providing little on no insight into the remaining useful life of the system. Detection of system-state significantly prior to catastrophic failure can significantly impact the reliability and availability of electronic systems. Previously, Lall [2004, 2005] have developed methodologies for health management and interrogation of system state of electronic systems based on leading indicators for eutectic Sn-Pb & 95.5Sn4.0Ag0.5Cu solders. Examples of damage precursors include micro-structural evolution, intermetallics. In this study, a mathematical approach for interrogation of system state under cyclic thermo-mechanical and isothermal stresses has been developed for 4-different lead-free solder alloy systems. Data has been collected for leading indicators of failure for alloy systems including, SnAgCu, SnAgCuBi, SnAgCuBiNi, SnAg second-level interconnects under the application of thermo-mechanical loads. Methodology presented resides in the pre-failure space of the system in which no macro-indicators such as cracks or delamination exist. Systems subjected to thermo-mechanical damage have been interrogated for system state and the computed damage state correlated with known imposed damage. The approach involves the use of condition monitoring devices which can be interrogated for damage proxies at finite time-intervals. Interrogation techniques are based on non-linear least-squares methods. Various techniques including the Levenberg-Marquardt Algorithm have been investigated. The system's residual life is computed based on residual-life computation algorithms.

ACKNOWLEDGEMENTS

I would like express my sincere thanks to my advisor, Dr. Pradeep Lall, for letting me work on this challenging project. Without his guidance, patience and constant encouragement, completion of the thesis would not have been possible. I would also like to acknowledge and thank the Center for advanced Vehicle Electronics (CAVE) and National Science Foundation for their financial support towards this project. I also wish to extend my gratitude to Dr. Jeff Suhling and Dr. Roy Knight for serving on my thesis committee and examining my thesis. I also wish to thank Mr. John Marcell and Mr. Roy Howard for giving technical assistance with the thermal chambers and Scanning Electron Microscope.

I would also like to thank all my friends, especially Madhura, Sameep, Bhushan, Shirish, Darshan, Amit, Ganesh, Robert, Jordan, Kaysar and all other colleagues and friends whose names are not mentioned, for their support. Finally, many thanks go to my brothers Ram and Dhananjay for motivating me to pursue graduate studies, and my parents for their unwavering encouragement and love. Style manual or journal used <u>Graduate School: Guide to Preparation and Submission of Theses and Dissertations</u> Computer software used <u>Microsoft Office 2003, ANSYSTM 9.0 / 10.0, Sigma Plot 8.0,</u> <u>National Instruments - IMAQ Vision Builder 5.0, Microsoft Visual Studio 2005,</u> <u>MATLABv2006a.</u>

TABLE OF CONTENTS

LIST OF	FIGURES	xi
LIST OF	TABLES	.xxii
CHAPT	ER 1: INTRODUCTION	1
1.1	Reliability of Novel 3-D Architectures (D-PACK TM)	5
1.2	Prognostics of Lead Free electronics in Harsh Environments	6
CHAPT	ER 2: LITERATURE REVIEW	8
CHAPT	ER 3: THERMO-MECHANICAL RELIABILITY OF 3-D PACKAGES	20
3.1	D-Pack TM : Capacitor Construction	21
3.2	Material Models : Constitutive Relationships	29
3.3	Finite Element Models: Boundary Conditions	33
3.4	Finite Element Models: Modeling Assumptions	34
3.5	Post-Processing Results: Partial Interposer (Eutectic Sn-Pb Solder Joints)	36
3.6	Post-Processing Results: Partial Interposer (SAC 305 Solder Joints)	40
3.7	Post-Processing Results: Full Interposer (SAC 305 Solder Joints)	43
3.8	Post-Processing Results: Regular BGA (SAC 305 Solder Joints)	49
3.9	Results Summary:	52
3.10	Life Prediction vs. Experimental data:	53
3.11	Failure Analysis:	57
3.12	Summary & Conclusion:	62

CHAPT	ER 4: PROGNOSTICS HEALTH MANAGEMENT OF SnAgCu SOLDER	
ELECTI	RONICS IN HARSH AGING ENVIRONMENTS	63
4.1	Test Vehicle	70
4.2	Damage Proxies: Lead-Free Solder Grain Coarsening	72
4.3	Damage Proxies: Intermetallic Coarsening	84
4.4	Interrogation of System State	90
4.5	Levenberg – Marquardt Algorithm	91
4.6	Phase Growth Prediction	94
4.7	IMC Growth Prediction	. 100
4.8	Implementation of Damage Pre-Cursors Approach	. 106
4.9	Summary and Conclusions	. 107
CHAPT	ER 5: PROGNOSTICS HEALTH MANAGEMENT OF LEAD-FREE Ag	
BASED	SOLDER ELECTRONICS IN HARSH CYCLING ENVIRONMENTS	. 109
5.1	Introduction	. 109
5.2	Test Vehicle	. 110
5.3	Leading Indicators of Failure:	. 112
5.4	Interrogation of System State:	. 114
5.5	Levenberg – Marquardt Algorithm	. 115
5.6	Prognostication of Leading-Indicators	. 115
5.7	Micro-structural Evolution	. 115
5.8	Intermetallic Compound Growth	. 118
5.9	Characterization of Damage Progression	. 120
5.10	Model Validation: Thermal Cycling	. 131

5.11	Model Validation: Isothermal Aging	. 137
5.12	Implementation Of PHM Technique	. 143
5.13	Summary and Conclusions	. 144
СНАРТ	ER 6: SUMMARY AND FUTURE WORK	. 145
6.1	D-PACK: Thermo-Mechanical Reliability	. 145
6.2	Prognostics and Health Management Implementation	. 146
6.3	Future Work	. 148
BIBLIO	GRAPHY	. 150

LIST OF FIGURES

Figure 1: Various components of a BGA package with the corresponding approximate
coefficients of thermal expansion (CTE) values
Figure 2: Decoupling capacitors placed on PCB and Package level (Conventional
Configuration)
Figure 3: Matrix of decoupling capacitors embedded as a part of second level
interconnects structure [Prymak 2005]
Figure 4: Partial Interposer Configuration D-Pack TM
Figure 5: Full Interposer Configuration: <i>D-Pack</i> TM (Solder Joints at the periphery) 24
Figure 6: <i>D-Pack</i> TM assembled onto test PCB (without LTCC package on top). <i>D-Pack</i> TM
is a matrix of individual <i>D-sticks</i> assembled together. Figure also shows the
geometry / dimensions of <i>D-stick</i>
Figure 7: LTCC Package (Top and Bottom View) with D-Pack Assembled onto the
Package Land
Figure 8: Quarter Symmetry Finite Element Model for <i>D-Pack</i> TM Partial Interposer
Configuration
Figure 9: Quarter Symmetry Finite Element Model for <i>D-Pack</i> TM Full Interposer
Configuration
Figure 10: Finite Element Slice Model for <i>D-PackTM</i> Partial Interposer Configuration 28
Figure 11: Finite Element Slice Model for <i>D-PackTM</i> Full Interposer Configuration 28

Figure 12: Close up view of D -Stick TM (Finite Element mesh) and comparison with actual
SEM picture for a pristine assembly
Figure 13: Boundary Conditions applied on the Straight Slice FE model
Figure 14: Finite Element Slice Model for Partial Interposer Configuration: Front View
(2 Solders Tested: Eutectic Sn-Pb and SAC 305)
Figure 15: Contour plot of accumulated plastic work on the D-Pack TM solder joints
(Partial Interposer with eutectic Sn-Pb solder) at the end of two thermal cycles 38
Figure 16: Plastic Work / Volume plot for critical of solder element layer (Partial
Interposer with eutectic Sn-Pb solder) that was subjected to maximum plastic
damage at the end of two thermal cycles
Figure 17: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical solder joint
element (eutectic Sn-Pb) that was subjected to maximum plastic damage at the end
of two thermal cycles
Figure 18: Variation of maximum principal stress in dielectric versus time, temperature.
Figure 19: Contour plot of accumulated plastic work on the D-Pack TM solder joints
(Partial Interposer with SAC 305) at the end of two thermal cycles
Figure 20: Plastic Work / Volume plot for critical of solder element layer (Partial
Interposer with SAC 305 solder joints) that was subjected to maximum plastic
damage at the end of two thermal cycles
Figure 21: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical solder joint
element (Partial Interposer with SAC 305 solder) that was subjected to maximum
plastic damage at the end of two thermal cycles

Figure 23: Finite Element Slice Model for Full Interposer Configuration: Front View Figure 24: Contour plot of accumulated plastic work on the D-PackTM solder joints (Full Figure 25: Contour plot of accumulated plastic work on the periphery solder joints (SAC Figure 26: Plastic Work / Volume plot for critical of solder element layer in the D-PackTM joint (Full Interposer with SAC 305 solder) at the end of two thermal cycles. Figure 27: Plastic Work / Volume plot for critical solder ball in the periphery joints (Full Figure 28: Plastic Work / Volume plot for critical element layer in the periphery solder joints (Full Interposer with SAC 305 solder) at the end of two thermal cycles...... 47 Figure 29: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical D-PackTM solder Figure 30: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical periphery solder Figure 31: Variation of maximum principal stress in dielectric versus time, temperature. Figure 32: Finite Element Slice Model for BGA Configuration: Front View (SAC 305

Figure 22: Variation of maximum principal stress in dielectric versus time, temperature.

Figure 33: Contour plot of accumulated plastic work on the tall solder joints (Regular
BGA with SAC 305 solder) at the end of two thermal cycles
Figure 34: Plastic Work / Volume plot for critical of solder ball (Regular BGA with SAC
305 solder) subjected to maximum plastic damage at the end of two thermal cycles.
Figure 35: Plastic Work / Volume plot for critical element layer in the tall joint (Regular
BGA with SAC 305 solder) at the end of two thermal cycles
Figure 36: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical solder joint
element subjected to maximum plastic damage at the end of two thermal cycles 51
Figure 37: Hysteresis loops (for critical element in solder joints) for various
configurations analyzed
Figure 38: Two parameter Weibull plot for Thermal Shock Experiments (0°C to 100°C,
15 min ramp / dwell) on D-Pack Partial Interposer test assemblies (with both Sn-Pb
and SAC solder)
Figure 39: Two parameter Weibull plot for Thermal Shock Experiments (0°C to 100°C,
15 min ramp / dwell) on D-Pack Full Interposer test assemblies (with SAC solder)56
Figure 40: Comparison between life prediction data (based on simulations) with
experimental data
Figure 41: SEM image of failed D-Pack assembly (Partial Interposer with eutectic Sn-Pb
solder joints). Dielectric cracking at the package side
Figure 42: SEM image of failed D-Pack assembly (Partial Interposer with eutectic Sn-Pb
solder joints). Solder Joint cracks on package side and board side

Figure 43: SEM image of failed D-Pack assembly (Partial Interposer with eutectic SAC
solder joints). Solder Joint cracks on package side and board side
Figure 44: Damage Pre-Cursors Based Methodology for Prognostication of Electronic
Systems
Figure 45: Test Vehicle
Figure 46: Ag3Sn Grains in 95.5Sn4.0Ag0.5Cu solder microstructure
Figure 47: Micrograph from 7 mm BGA showing Tin and Ag ₃ Sn Phases
Figure 48: Microstructure mapping using Image Analysis
Figure 49: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,
95.5Sn4Ag0.5Cu solder, 16 mm BGA, Magnification: 750x)
Figure 50: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,
95.5Sn4Ag0.5Cu solder, 27 mm BGA, Magnification: 750x)
Figure 51: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,
95.5Sn4Ag0.5Cu solder, 15 mm BGA, Magnification: 750x)
Figure 52: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,
95.5Sn4Ag0.5Cu solder, 15 mm BGA, Magnification: 750x)
Figure 53: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,
95.5Sn4Ag0.5Cu solder, 10 mm BGA, Magnification: 750x) 80
Figure 54: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,
95.5Sn4Ag0.5Cu solder, 7 mm BGA, Magnification: 750x) 80
Figure 55: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,
95.5Sn4Ag0.5Cu solder, 6 mm BGA, Magnification: 750x)

Figure 56: Phase Growth Parameter versus Aging Time at 125°C for PBGA 676 SnAgCu
Alloy Solder Interconnects
Figure 57: Phase Growth Parameter versus Aging Time at 125°C for PBGA 196 SnAgCu
Alloy Solder Interconnects
Figure 58: Phase Growth Parameter versus Aging Time at 125°C for TAPE ARRAY 144
SnAgCu Alloy Solder Interconnects
Figure 59: Phase Growth Parameter versus Aging Time at 125°C for FLEX 280 SnAgCu
Alloy Solder Interconnects
Figure 60: Phase Growth Parameter versus Aging Time at 125°C for CABGA 84
SnAgCu Alloy Solder Interconnects
Figure 61: Phase Growth Parameter versus Aging Time at 125°C for TAPE ARRAY 64
SnAgCu Alloy Solder Interconnects
Figure 62: SEM Back-scattered images of IMC Growth versus Thermal Aging for
Sn4Ag0.5Cu (Magnification 1000x)
Figure 63: IMC Growth, at Various Levels of time for PBGA 676 with 95.5Sn4Ag0.5Cu
Alloy
Figure 64: IMC Growth, at Various Levels of time for PBGA 196 with 95.5Sn4Ag0.5Cu
Alloy
Figure 65: IMC Growth, at Various Levels of time for FLEX 280 with 95.5Sn4Ag0.5Cu
Alloy
Figure 66: IMC Growth, at Various Levels of time for TAPE ARRAY 144 with
95.5Sn4Ag0.5Cu Alloy

Figure 67: IMC Growth, at Various Levels of time for CABGA 84 with 95.5Sn4Ag0.5Cu
Alloy
Figure 68: IMC Growth, at Various Levels of time for TAPE ARRAY 64 with
95.5Sn4Ag0.5Cu Alloy
Figure 69: Schematic illustration of input to the LM minimization code
Figure 70: LM algorithm convergence plot for phase growth under aging load for 196 I/O
BGA
Figure 71: LM algorithm convergence plot for phase growth under aging load for 144 I/O
BGA
Figure 72: Graphical comparison of final results (PBGA 196)
Figure 73: Graphical comparison of final results (T144)
Figure 74: LM algorithm convergence plot for IMC growth under aging load for C84 I/O
BGA102
Figure 75: LM algorithm convergence plot for IMC growth under aging load for 676 I/O
Plastic BGA
Figure 76: Graphical comparison of final results (P676)
Figure 77: Graphical comparison of final results (P196)104
Figure 78: Graphical comparison of final results (F280)
Figure 79: Graphical comparison of final results (C84)
Figure 80: Graphical comparison of final results (T64)
Figure 81: Ag ₃ Sn Grains in 96.5Sn3.0Ag0.5Cu solder microstructure
Figure 82: Schematic illustration of input to the LM minimization code

Figure 83: SEM Back-scattered Images of Phase Growth versus Thermal cycling (-55°C
to 125°C, Sn0.3Ag0.7Cu0.1Bi solder, 100 I/O Chip Array BGA, Magnification
750x)
Figure 84: SEM Back-scattered Images of Phase Growth versus Thermal cycling (-55°C
to 125°C), Sn0.2Ag0.7Cu- 0.1Bi0.1Ni solder, 100 I/O Chip Array BGA,
Magnification 750x)
Figure 85: SEM Back-scattered Images of Phase Growth versus Thermal cycling (-55°C
to 125°C, 96.5Sn3.5Ag plus solder, 100 I/O Chip Array BGA, Magnification 750x)
Figure 86: Phase Growth parameter, at various levels of cycles for 100 I/O Chip Array
BGA, SAC-X solder interconnects
Figure 87: Phase Growth parameter, at various levels of cycles for 100 I/O Chip Array
BGA, Sn0.3Ag0.7Cu0.1Bi0.1Ni solder interconnects
Figure 88: Phase Growth parameter, at various levels of cycles for 100 I/O Chip Array
BGA, 96.5Sn3.5Ag solder interconnects
Figure 89: SEM Back-scattered images of IMC Growth versus Thermal Aging for
Sn0.3Ag0.7Cu0.1Bi (Magnification 1000x)126
Figure 90: SEM Back-scattered images of IMC Growth versus Thermal Aging
Sn0.3Ag0.7Cu0.1Bi0.1Ni (Magnification 1000x)
Figure 91: SEM Back-scattered images of IMC Growth versus Thermal Aging for
Sn3.5Ag (Magnification 1000x)
Figure 92: IMC Growth, at various levels of time for CABGA 100 with
Sn0.3Ag0.7Cu0.1Bi alloy 129

Figure 93: IMC Growth, at various levels of time for CABGA 100
Sn0.3Ag0.7Cu0.1Bi0.1Ni alloy
Figure 94: IMC Growth, at various levels of time for CABGA 100 with Sn3.5Ag alloy
Figure 95: Plot of Error vs. No. of Thermal cycles (N) for 100 I/O CABGA
Sn0.3Ag0.7Cu0.1Bi solder interconnects (Error minimum in the vicinity of 177
cycles)
Figure 96: Plot of Error vs. No. of Thermal cycles (N) for 100 I/O CABGA
Sn0.2Ag0.7Cu0.1Bi0.1Ni solder interconnects (Error minimum in the vicinity of
175 cycles)
Figure 97: Plot of Error vs. No. of Thermal cycles (N) for 100 I/O CABGA 96.5Sn3.5Ag
solder interconnects (Error minimum in the vicinity of 175 cycles)
Figure 98: Plot of Minimization Error vs. No. of Thermal cycles (N) for 100 I/O CABGA
Sn0.3Ag0.7Cu0.1Bi solder interconnects (Error minimum in the vicinity of 559
cycles)
Figure 99: Plot of Minimization Error vs. No. of Thermal cycles (N) for 100 I/O CABGA
Sn0.2Ag0.7Cu0.1Bi0.1Ni solder interconnects (Error minimum in the vicinity of
460 cycles)
Figure 100: Plot of Minimization Error vs. No. of Thermal cycles (N) for 100 I/O
CABGA 96.5Sn3.5Ag solder interconnects (Error minimum in the vicinity of 391
cycles)
Figure 102: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. grain
size from experimental values Sn0.3Ag0.7Cu0.1Bi alloy136

Figure 103: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. grain
size from experimental values Sn0.2Ag0.7Cu0.1Bi0.1Ni alloy 137
Figure 103: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. grain
size from experimental values 96.5Sn3.5Ag alloy
Figure 104: Global Minima for IMC based History Calculation for 100 I/O CABGA,
Sn0.3Ag0.7Cu0.1Bi Solder Alloy Interconnects (Error minimum in the vicinity of
830 hrs)
Figure 105: Global Minima for IMC based History Calculation for 100 I/O CABGA,
Sn0.2Ag0.7Cu0.1Bi0.1Ni Solder Alloy Interconnects (Error minimum in the
vicinity of 830 hrs)
Figure 106: Global Minima for IMC based History Calculation for 100 I/O CABGA,
Sn3.5Ag Solder Alloy Interconnects. (Error minimum in the vicinity of 914 hrs) 139
Figure 107: Global Minima for IMC based History Calculation for 100 I/O CABGA,
Sn0.3Ag0.7Cu0.1Bi Solder Alloy Interconnects (Error minimum in the vicinity of
1160 hrs)
Figure 108: Global Minima for IMC based History Calculation for 100 I/O CABGA,
Sn0.2Ag0.7Cu0.1Bi0.1Ni solder Alloy Interconnects. (Error minimum in the
vicinity of 1355 hrs)
Figure 109: Global Minima for IMC based History Calculation for 100 I/O CABGA,
Sn3.5Ag Solder Alloy Interconnects (Error minimum in the vicinity of 1150 hrs).
Figure 110: Prognostication of grain size from algorithm (based on g ₀ , a and b) vs. grain

Figure 111: Prognostication of grain size from algorithm (based on g₀, a and b) vs. grain

Figure 112: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. gra	ain
size from experimental values 96.5Sn3.5Ag alloy	143

LIST OF TABLES

Table 1 : Common Failure Modes in Electronic Packages	4
Table 2 : Configurations Tested for Thermal Shock Experiments	24
Table 3: Anand's Constant for SAC105, SAC305 and SAC405	
Table 4: Material Properties used for finite element modeling [Zahn 2003]	
Table 5 : Results Summary	52
Table 6: Life Prediction Calculations (Summary)	54
Table 7: Experimental Design	
Table 8: Variable Range for Phase-Growth in Thermal Aging (based on Experim	iental
data)	
Table 9: Results comparison with experiments	
Table 10: Variable Range for IMC growth for various alloys	101
Table 11: Algorithm Results comparison with experiments	103
Table 12 : Package Details	111
Table 13: Variable Range for phase growth in thermal cycling for various alloys	(based
on experimental data)	116
Table 14: Variable Range for IMC growth for various alloys	119
Table 15: Comparison of computed values of N, g ₀ , from prognostication model	versus
experimental result	133

Table 16: Comparison of computed values of a and b from Prognostication model versus
experimental result
Table 17: Comparison of computed values of N, g ₀ , from prognostication model versus
experimental result
Table 18: Comparison of computed values of a and b from Prognostication model versus
experimental result
Table 19: Comparison of computed values of t, y ₀ from prognostication model and
experimental result
Table 20: Comparison of computed values of t, y_0 from prognostication model and
experimental result
Table 21 : Proposed Test Matrix to quantify the effect of Sequential Stresses

CHAPTER 1

INTRODUCTION

The rapid evolution in microelectronic technology is a well known phenomenon. The decreasing feature sizes on IC's enable the integration of a huge number of transistors on a given area of silicon. In addition to the increase in complexity and size, the pin count of the die is increasing with time. The fast evolution in microelectronic technology has also enabled the circuits to run at higher speeds. Such high frequencies require special design of the IC's and packaging interconnections.

Electronic packaging is the process of interconnecting electronic and electromechanical components, devices, and modules between the various layers of the electronic system [Suhling, et.al. 2004]. Single-Chip packaging has evolved during the last 3 decades, starting with Dual-Inline Packages (DIPs) and wire bond in the 1970s, Quad Flat Packs (QFPs) and Surface-Mount Technologies (SMT) in the 1980s, and Ball-Grid Arrays (BGAs) in the 1990s. In the last two decades area-array packages, e.g., BGA, Chip Scale Package (CSP) have become more popular packaging alternatives as compared to their earlier counterparts.

BGA packages offer a lot of benefits over their leaded counterparts (QFPs / PQFPs) by providing increased functionality for the same package size while being compatible with existing surface mount technology infrastructure. BGAs fit ICs into a smaller footprint, decreasing pitch spacing, by utilizing an array of solder ball

connections. This allows for a higher density of I/O connections than QFPs, along with a high yield. The result is a considerably smaller finished package size. BGAs also offer better electrical performance due to reduced lead inductance. They also have an improved design-to-production cycle time and can be used in flip-chip-package (FCPs) and multi-chip modules (MCMs) configurations.

We know that electronics forms an integral part of most systems that we use, in the form of a simple alarm clock or the circuitry that controls the fuel injection under the hood of a vehicle. Failure of an electronic sub-system to perform reliably can sometimes, depending on the application, lead to catastrophic consequences. Reliability testing is therefore a very important criterion for any electronic system before it is being deployed in the field.

The work presented in this study mainly deals with the reliability of electronics subjected to harsh thermo-mechanical environments. The operation of any electronic device generates heat and with the increasing device density of the IC chips the amount of heat flux generated by the IC chips has gone to a level of 100-200 W/cm² [Nimkar, et al. 2005]. An electronic package like BGA (shown in Figure 1) is essentially an assembly of different materials sets (die, BT substrate, molding compound, etc) attached together using various processes. Each material set has unique properties like Coefficient of Thermal Expansion (CTE), Young's Modulus (E), poisons ratio (v), etc. When this assembly is subjected to a change in temperature, either on account of Joule heating or change in ambient temperatures, these unique materials tend to expand / contract at different rates resulting in cyclic shear strains and shear stresses, which over a period of time lead to fatigue.

The fatigue failure of the device can occur in various different modes [Viswanadham and Singh, 1998]. A summary of common failure modes is shown in Table 1 below



Figure 1: Various components of a BGA package with the corresponding approximate coefficients of thermal expansion (CTE) values.

Failure Mode	Reason
Pop-Corn	Occurs during the re-flow of the component due to moisture
Failure	absorbed by the molding compound.
Chip / Die	Occurs due to thermal stresses developed in the chip during
Cracking	package assembly or during the thermal cycling of the
	component due to the CTE mismatch within the package.
Delamination	Occurs due to thermal stresses developed in the chip during the
between	thermal cycling of the component due to the CTE mismatch
Interfaces	within the package.
Solder Joint	The expansion and contraction of material sets due to Joule
Failure	heating / change in ambient temperature introduces shear strains
	and shear stresses in the solder joint. The repeated heating and
	cooling can eventually cause fatigue of the solder joints.

Table 1 : Common Failure Modes in Electronic Packages

It has been established from various studies and failure analyses [Harmon 1974, Engelmaier 1984, Katlowitz 1986, Hwang 1988, Solomon 1989, Tien, et al. 1989, Lau 1991, Lall, et al. 1997, 2003, 2005, Suhling, et al. 2004] that the interconnect failure due to the thermal cycling is the most critical mode of failure in various leaded and SMT packages such as BGAs and flip-chips. Solder joint fatigue failure being a dominant failure mode contributing to 90% of all structural and electrical failures [Tummala 1997] demands greater focus for improving the mechanical reliability of the package.

1.1 Reliability of Novel 3-D Architectures (D-PACKTM)

Moving forward, miniaturization with increased functionality continues to be an important trend in all electronics products [Mallik, et al. 2005]. An example of miniaturization trend is also seen in the ever improving functionality of mobile handsets. Over the last five years or so, 2D games, and even more demanding 3D games, have become available in these devices. The increased functionality (music, video, gaming, etc) integration with each handheld product generation adds to the complexity of the baseband and power management units, which in turn requires more passive components (especially resistors and capacitors) for baseband power supply and management. The number of passive components in a typical cell phone has more than tripled in the last few years. This increase in passive counts leads to increase in assembly costs and reliability issues.

Capacitors are used to decouple the system-level power supply from individual electrical devices of an electronic package. Decoupling of an electronic device from the power supply reduces the overall noise in the power distribution network of the electronic package [Geissenger, et al. 2006]. However, due to increase in the speed and electrical current associated with high-speed electronic devices, traditional capacitor structures do not provide adequate performance because the inductance associated with these types of capacitors inhibits their operation at high speeds. Interconnect inductance in an electronic package chokes the capacitor, preventing the high-speed transfer of electrical current to and from the capacitor. Embedding capacitors directly into the electronic packages provides significant decoupling capacitance with very low interconnect inductance. This

approach facilitates very high-speed operation of electronic devices within an electronic package.

Kemet Corporation has patented a technology to embed capacitor in a Ceramic Ball Grid Array Package, called a D-PACKTM. The capacitors are embedded in the second-level interconnects of the package. In the present work, the thermo-mechanical reliability of two configurations of D-PACKTM (full interposer & partial interposer) in harsh environments has been studied using finite element simulations. Failure analyses of failed packages were carried out to investigate the failure modes and mechanisms.

1.2 Prognostics of Lead Free electronics in Harsh Environments

There is a growing need to develop and demonstrate technologies that can monitor and predict the remaining service life of key elements in our national civil infrastructure [Bond 1999]. Maintenance has evolved over the years from simply reacting to machinery breakdowns (corrective maintenance), to performing time-based preventive maintenance, to today's emphasis on the ability to detect early forms of degradation in predictive maintenance practices. The incentive for each incremental step has been a clear reduction in the cost of operating and maintaining (O&M) almost any process facility [Jarell, et al. 2002].

Health Monitoring (HM) refers to the broad concept of assessing the ongoing, inservice performance of a system using a variety of measurement techniques. Prognostics refer to interrogation of material state of a system based on computation of certain proxies, stressors, and to predict the Residual Life (RL) of the system for the intended environment. PHM application areas include fatigue crack damage in mechanical structures such as those in aircraft [Munns 2000], surface ships [Baldwin 2002], civil infrastructure [Chang 2003], railway structures [Barke 2005] and power plants [Jarrell 2002].

Wear and degradation in electronics is very difficult to detect and inspect compared to most other mechanical systems and structures due to complex and tiny structure. Methods like Built-In-Self-Test (BIST), embedding fuses and pre-calibrated canaries within circuits have been used to provide advance warning of failure in electronics due specific wear out failure mechanism.

A Prognostics & Health Management (PHM) approach has been presented in this study. The approach is different from the current state-of-art diagnostics and resides in the pre-failure space of the electronic-system, in which no macro-indicators such as cracks or delamination exist. The presented PHM methodologies enable the estimation of prior damage in deployed electronics by interrogation of the system state.

Data has been collected for leading indicators of failure for two separate test vehicles, with different area array packages soldered with various lead free alloys (SAC 405, SnAgCuBi, SnAgCuBiNi, 96.5Sn3.5Ag) under both single and sequential application of cyclic and isothermal thermo-mechanical loads.

CHAPTER 2

LITERATURE REVIEW

It is only natural that any major system used these days comprises several subsystems, each containing myriad components and elements. Since system-level reliability depends on the reliability of these individual components, it becomes critical to analyze the reliability of any component during design phase or before deployment in the field. Concurrent with the rapid progress in IC technology, packaging of an electronic system with high reliability is posing an ever increasing challenge. Whether the result of power transients or changes in ambient temperature, a solder joint must withstand repeated strain reversals caused by non-uniform thermal expansion of the carrier, the solder, and the board [Wong et. al. 1988]. Because of the cyclic nature of this loading, this type of failure has been called fatigue.

Although historically fatigue studies have been concerned with conditions of service in which failure occurred at more than 10^4 cycles of stress, there is growing recognition of engineering failures which occur at relatively high stress and low numbers of cycles to failure [Coffin 1979]. Low cycle fatigue conditions frequently are created where the repeated stresses are of thermal origin [Manson 1960]. Since thermal stresses arise from the thermal expansion of the material, it is easy to see that in this case fatigue results from cyclic strain rather than from cyclic stress [ASTM Standard 1969].

Solder joint fatigue failure being a dominant failure mode, contributing to 90% of all structural and electrical failures [Tummala 1997] demands greater focus for improving the mechanical reliability of the package. As newer packages and architectures continue to evolve with improvements in IC technology, there is a need to develop efficient predictive methodologies for maintaining high levels of package reliability. Over the years, this reliability problem has been approached using combination of experimental measurements and numerical simulations. There exist numerous life-prediction methods for solder fatigue. This section briefly discusses the evolution of various approaches used for solder joint reliability prediction, including inelastic strain or total strain based models, energy based models, physics of failure based models, statistical models and finite element models.

Coffin [1954] & Manson [1964] developed relationship between low-cycle fatigue life (cycles to failure) and plastic strain range ($\Delta \varepsilon_p$). Norris and Landzberg [1969] studied the effect of cycling frequency and maximum temperature of cycling on fatigue failure of solder joints and added an empirical correction factor for time dependent and temperature dependent effects for the thermal fatigue model.

Engelmaier [1982] developed a methodology to determine shear strains from inplane expansion mismatches. Further Engelmaier [1984] proposed that cyclic fatigue damage is directly proportional to the area circumscribed by the cyclic hysteresis loop in a stress-strain diagram. Engelmaier [1990] developed a surface mount solder joint reliability prediction model containing all the parameters influencing the shear fatigue life of a solder joint due to shear displacement caused by thermal expansion mismatch between component and substrate. The parameters of the model include effective solder joint area, solder joint height, diagonal flexural stiffness, distance from neutral point and thermal coefficient mismatch, thermal cycling conditions, degree of completeness of stress relaxation and slope of weibull distribution.

Solomon [1989] analyzed the fatigue failure of 60Sn/40Pb solder for various temperatures and developed an isothermal low cycle fatigue equation that correlated number of cycles to failure with applied plastic shear strain range. Solomon also studied the influence of factors like frequency of loading, temperature changes on the fatigue life, and added exponents to the fatigue equation to account for them.

Shine and Fox [1987] proposed a model correlating the number of cycles to failure with matrix creep shear strain γ_{mc} . This correlation was achieved using a steady-state creep law with different, experimentally determined coefficients for each sample considered; the matrix creep was then integrated over the actual measured stress history. Subsequently, Knecht and Fox [1990] proposed a constitutive equation for a typical Sn-Pb eutectic solder joint based on empirical data in shear strain. It was shown that the constitutive equation together with the matrix creep failure indicator gave an estimate of fatigue life which matched reasonably well with independent failure datasets.

Wong et al. [1988] developed an analytical framework to predict the failure of solders under creep conditions, based on micromechanics and fracture mechanics approach. This method assumed the presence of a pre-existing crack within the solder, and proposed a theory about nucleation of cavities, their subsequent interlinking around the local second phase particles in the vicinity of crack tip stress field. Based on cavity-crack inter-linkage, equation for crack growth was developed. The time to failure was calculated by assuming that a pre-existing crack grows by creep cavitation until it reaches

a critical length when instantaneous fracture occurs. Yamada [1989] showed that the concept of fracture mechanics could be suitably applied to solder joint cracking and that the fracture toughness of the solder is an important parameter to compare the influence of many variables on the strength relevant to soldering of electronic packages. The theory of strain energy release, and fracture toughness was applied to a 60Sn-40Pb soldered joint of beryllium copper to beryllium copper.

Subrahmanyan et al. [1989] proposed a damage integral calculation providing a numerical accounting of fatigue damage in solder joints. Using a simplistic crack propagation law, crack growth parameters were derived from isothermal fatigues tests and successfully applied to thermo-mechanical fatigue tests through the damage integral approach.

Dasgupta et al. [1992] proposed an energy partitioning approach that considered the complete stress-strain hysteresis response of the solder. The energy stored and dissipated during each cycle (determined by the hysteresis curve) was partitioned into elastic (recoverable) energy, plastic (instantaneous, irrecoverable) work and creep (timedependent, irrecoverable) work. This energy partitioning information was obtained from visco-plastic analysis such as finite element methods. Three independent power-law expressions relating the partitioned energy to the damage (or cycles to failure) were obtained from experimental data in the literature for eutectic Pb-Sn solder. The total damage incurred in each thermal cycle was calculated using a simple linear superposition of damage due to each of the three partitioned energy terms.

Syed [1995] presented an engineering approach to the life prediction of solder joints in thermal cycle environment. A damage mechanism based on creep crack growth model incorporating multiaxiality and time, temperature dependence of the solder joint in thermal cycling environments was proposed. The creep deformation mechanisms viz. grain boundary sliding and matrix creep phenomenon were treated separately in this approach. A three-dimensional finite element approach was used to accurately separate the contribution of each mechanism to the total damage. It was shown that creep crack growth rate was a function of temperature, dissipation rate of creep strain energy density and some material and crack growth parameters. For the same damage mechanisms, this model was capable of predicting the fatigue life for any loading profile, frequency and temperature range.

Pao [1992] proposed a crack growth model in terms of both C* integral based creep mechanisms (nucleation, growth and coalescence of cavities along grain boundaries) and J integral based fatigue mechanisms (applied stress in the solder joint acting as the driving force in the propagation of initial crack leading to fracture). In addition to the capability of predicting thermal fatigue life of solder joints, this method could also be used to design accelerated thermal tests.

Clech [1996] developed a solder reliability solutions model for leadless and leaded eutectic solder assemblies and extended it to area array and CSP packages. Clech obtained the inelastic strain energy density from area of solder joint hysteresis loop and developed a prediction equation correlating inelastic strain energy density with number of cycles to failure.

Darveaux et al. [1992] conducted shear and tensile loading experiments on various solders (60Sn40Pb, 96.5Sn3.5Ag, 97.5PbSn2.5, 95Pb5Sn) and presented the deformation behavior of these alloys by the same set of constitutive relations. Also,

numerical simulations were conducted to predict the solder joint response for these alloys under thermal cycling conditions, based on hysteresis loop calculations.

Darveaux [1996] developed a strain energy based methodology to predict the solder joint reliability. A three-dimensional finite element model of the package was created where the solder joints were modeled as visco-plastic material, printed circuit board as orthotropic linear elastic and rest of the material as linear elastic. Symmetric boundary conditions were imposed on the model to coincide with true symmetry plane. The energy-based method linked the fatigue life to the inelastic strain energy dissipation of solder joints. Based on extensive test of BGA solder joints and FE modeling, Darveaux proposed empirical equations to calculate the solder fatigue life [1996, 1997, and 2000].

In Darveaux's model, the total fatigue life consists of the life before crack initiation and the life after it. The constant terms are derived by curve fitting the FEA prediction with the test data. Because the inelastic strain energy depends strongly on the finite element mesh of the solder joints, different constants values were given according to the element size. The extracted plastic work accumulated per unit volume per thermal cycle was used for crack growth correlations. Volume averaging was applied to reduce the sensitivity of strain energy to meshing.

Hariharan [2006] presented models based on multiple linear regression, principal components regression and power law based methodologies for developing prediction models to enable higher-accuracy prediction of characteristic life by perturbing known accelerated-test data-sets using models, using factors which quantify the sensitivity of reliability to various design material, architecture and environmental parameters.
Of all these methodologies, Darveaux's seems to be the most popular due to the ease in its implementation. Also, methodology has been previously presented in the successful analyses of various electronic assemblies from multiple industry sources. Darveaux's energy based model has been used in this thesis to evaluate the thermomechanical reliability of 2nd level interconnects for capacitor embedded in a Ceramic Ball Grid Array Package.

While reliability analysis of any component is critical, it is also important to monitor the condition / state of the system from time to time in order to improve the system availability and upkeep. Majority of systems being used these days, e.g., nuclear power plant machinery, aircrafts engines / avionics, gas turbine systems, are expected to remain operational for lengthy periods of time and usually have an elaborately drawn maintenance / overhaul schedule. Also, maintenance techniques have evolved over the years from simply reacting to machinery breakdowns (corrective maintenance), to performing time-based preventive maintenance, to today's emphasis on the ability to detect early forms of degradation in predictive maintenance practices. The incentive for each incremental step has been a clear reduction in the cost of operating and maintaining (O&M) almost any process facility [Jarell, et al. 2002].

New advances in sensor technology and failure analysis are instigating a revolution in the way large electromechanical systems such as aircraft, helicopters, ships, power plants, and many industrial operations will be maintained in the future. For industry and the armed services, the 21st century will bring the age of PHM — Prognostics and Health-Management [Becker et al. 1998]

Health Monitoring refers to the broad concept of assessing the on-going, inservice performance of a system using a variety of measurement techniques. Prognostics means predictive diagnostics, which includes determining the remaining life or time span of the operational life of a component. Prognostics & Health Management (PHM) refers to the methodology of interrogation of material state of a system based on computation of certain proxies and to predict the Remaining Useful Life (RUL) of the system for the intended environment.

PHM methodology application areas include aircraft structures [Munns 2000], surface ships [Baldwin 2002], civil infrastructure [Chang 2003], gas turbines. This section briefly discusses the various applications where PHM methodology has been applied.

In case of mechanical systems like propulsion systems, compressors, gears, etc damage progresses mainly due to wear (prolonged usage), or imbalance condition in one of the rotating elements, or from misalignment of the shafts of the rotating components which leads to changes in the vibration signature of the equipment. By comparing the vibration signals from the defective equipment with those from sound equipment, the performance degradation can be characterized [Dyne 1992].

PHM of mechanical structures has been done by dynamic analysis based on natural frequencies, mode shapes, damping factors, and static analysis based on deformation or changes in structure orientation due to load or unexpected damage, using innovative signal processing, new sensors, and control theory. Transducers along with a wireless data acquisition system can enable the possibility of achieving long distance monitoring [Kok 2005]. Greitzer et al. [1999] has developed prototype diagnostic / prognostic system for main Battle Tank's (MBTs) engine health based on Antificial Neural Networks (ANNs) to diagnose and predict faults. This approach uses approximately thirty onboard sensors to measure temperature, pressure, RPM, vibration to construct a detailed thermodynamic picture of the engine's state. This data is then conveyed via telemetry to the command / control and maintenance support so that battle readiness and maintenance needs can be assessed immediately.

Smeulers et al. [2002] applied a model based PHM methodology to an aircraft hydraulic system using measurable condition parameters like valve port timing, internal leakage using two pressure transducers. The health of the system was monitored by means of signature analysis of pulses produced by pump at sensors. Similar concepts can be applied for health monitoring of other aircraft sub-systems like fuel system, lubrication system of main engine.

The technique of detecting specific faults by interrogating sensors placed along the sides of railway tracks is referred to as wayside detection. Barke [2005] has reviewed various types of wayside detection techniques used in the railway industry to provide extensive information about vehicle performance. The information generated is often recorded in an extensive database, providing information on the vehicle condition and performance over an extended period of time. This database can be interrogated with respect to certain critical performance parameters over time to provide information on condition of in-service railway vehicles.

Most of the PHM methodologies listed above operate by collecting precursor data from sensors, mounted on or near the components, which collect for data in the form of signals, pulse, etc. Signal feature analysis is performed to detect abnormalities that are related to an impending failure indication by an inference engine / system using an historical database [Hess 2001, 2002]. This approach can provide warning of failure but is inherently incapable of attaching a confidence interval to the remaining life prediction [Wilkinson et al. 2004]. In contrast, electronic systems cannot generally provide such kinds of precursor data.

Wear and degradation in electronics is very difficult to detect and inspect compared to most other mechanical systems and structures due to complex and tiny structure. Some examples of health monitoring in electronic circuits are discussed below.

It has been common practice to implement error detection and sometimes error correction, in dynamic RAM arrays. DRAMS are subject more than any other type of component to single event upsets arising from cosmic rays and alpha particles. Error may be detectable, or with increased hardware overhead, correctable for single bit errors. Similarly, due to their regular structure, the operating system can to keep track of 'bad sectors', analogous to the bad sector mapping applied to disk drives and map out the failed locations. Electronic part manufacturers apply a similar technique to DRAMS. They selectively laser-cut redundant cells into the array to replace those found to be defective on final test. These techniques rely upon precursors to indicate declining health and are very limited in the types of failure that can be predicted and in the warning period provided [Wilkinson et al. 2004].

Built- In-Self Test (BIST) circuit, which includes onboard hardware and software diagnostic, has been used for error detection and fault location [Drees 2004]. BIST is a methodology that embeds additional functionality in the product to give it the ability to

test and diagnose itself with minimal interaction from external test equipment [Williams 1983, Hassan 1992, Zorian 1994, Chandramouli 1996].

BIST controllers are typically used for reactive failure detection, to output failure data that can be correlated to show exactly when the failure occurred. This data can then be interpreted by diagnostic software to analyze the cause of failure. For example, Pseudo-Random Binary-Sequence (PRBS) test pattern generators, apply input vectors to digital or analog [Al-Qutayri 1992] modules. Self-Checking circuit designs provide on-line test for digital [Lala 1985] as well as for analog circuits [Kolarik 1993]. The obtained output is then compared with a "golden response". The results obtained from BIST functions can generate diagnostic information which in turn provides additional confidence in the measurement result and confirm the device availability.

BIST helps in minimizing the interaction with external automated test equipment (ATE) as well as provides the advantage of a more robust "at-speed" test of the circuitry. However, the current form gives little insight about the system level reliability or the remaining useful life of the system. Several studies conducted [Allen 2003, Drees 2004, Gao 2002, Rosenthal 1990] have shown that BIST can be prone to false alarms and can result in unnecessary costly replacement, re-qualification, delayed shipping, and loss of system availability.

Fuses and Canaries have been used to provide advance warning of failure in electronics due to specific wear out failure mechanism [Vichare 2006]. Fuses within circuits and thermostats, can be used to sense the abnormal conditions like voltage transients, critical temperature limit and to make adjustment to restore normal condition [Ramakrishnan 2000].

Canary devices like pre-calibrated cells which are located with the actual circuitry on the same chip experience similar stresses as the actual component, this leads to same damage mechanism. The cells are designed to fail faster by scaling the stress which is been experienced to avoid the catastrophic failure of actual component. The failure of the canary devices can be used to estimate the time to failure of actual product [Mishra 2002]. Similarly canary components created on printed circuit board is been used for prognostication by failing before the actual component [Anderson 2004].

However, replacement of fuses and canaries impacts the maintenance, repair and part replacement making it difficult to integrate these systems with the host system. In addition, fuses provide limited insight into the remaining use life prior to fuse-failure.

These approaches may be best described as health monitoring approaches. They do not (and cannot) address the prognostic side of the problem. PHM approach presented in this paper is different from state-of-art diagnostics and resides in the pre-failure space of the electronic-system, in which no macro-indicators such as cracks or delamination exist. The presented PHM methodologies enable the estimation of prior damage in deployed electronics by interrogation of the system state.

CHAPTER 3

THERMO-MECHANICAL RELIABILITY OF 3-D PACKAGES

Microelectronic packages continue to undergo significant changes to keep pace with the demands of the high performance silicon. From the traditional role of space transformation and mechanical protection, packages have evolved to be a means to costeffectively manage the increasing demands of power delivery, signal distribution, and heat removal. In the last decade or so, increasing frequency and power levels coupled with lower product costs have been driving new package technologies [Mallik, et al. 2005].

Because of current flow during the simultaneous switching of the circuits of digital systems, voltage fluctuations are generated across power supply buses. The magnitude of these fluctuations depends on the amount of current, its rise time, and the effective chip and package inductances [Humenik et al.1992]. This noise can couple through a quiet logic circuit driver and appear as a spurious voltage signal on the input terminals of a logic receiver circuit, sometimes causing switching [Davidson 1982, Ho 1982]. On-chip decoupling capacitors (decaps) are widely used to mitigate the power-supply-noise problem. By charging up during the steady state, decaps can assume the role of the power supply and provide the current needed during the simultaneous switching of multiple functional blocks [Wong 2007]. Alternatively, decoupling capacitors can be used to reduce the impedance of power delivery systems operating at high frequencies.

However, due to increase in the speed and electrical current associated with highspeed electronic devices, traditional capacitor structures do not provide adequate performance because the inductance associated with these types of capacitors inhibits their operation at high speeds [Geissinger 2006]. Interconnect inductance in an electronic package chokes the capacitor, preventing the high-speed transfer of electrical current to and from the capacitor. Since the inductance scales poorly [Mezhiba 2004], the location of the decoupling capacitors significantly affects the design of the power / ground (P/G) networks in high performance ICs such as microprocessors. With increasing frequencies, a distributed system of on-chip decoupling capacitors is needed.

3.1 **D-Pack**TM: Capacitor Construction

Embedding capacitors directly into the electronic packages provides significant decoupling capacitance with very low interconnect inductance. This approach facilitates very high-speed operation of electronic devices within an electronic package [Geissinger 2006]. The decoupling capacitors are placed on the PCB, package, and chip levels, respectively [Kim 2001] as shown in Figure 2:. In case of on-chip decaps, the costs associated with layer count in substrates, and other additional processes to facilitate the connection (traces) between decaps and operating device, drive the overall package costs upwards, making them uneconomical.

Kemet Corporation has patented a technology to make monolithic multi-layer capacitors with improved lead-out structure [Prymak 2005]. The individual monolithic multi-layer capacitors D-SticksTM are assembled into a matrix structure called as D-PackTM as shown in Figure 3. The top and bottom sides of D-Pack have metal layers

(including a thin layer of solder) deposited so that it can be attached to both the package as well as the Printed circuit Board (PCB).

The *D-Pack* serves as a physical interconnection between the substrate and the PCB, and also serves a decoupling capacitor performing the functions of reducing signal noise and inductance. Figure 2 and Figure 3 show the conventional configuration of decoupling capacitors vis-à-vis the configuration proposed by Kemet.



Figure 2: Decoupling capacitors placed on PCB and Package level (Conventional Configuration)



Figure 3: Matrix of decoupling capacitors embedded as a part of second level interconnects structure [Prymak 2005].

Two configurations of *D-Pack*TM have been assembled and subjected to thermal shock experiments at the Center of Advance Vehicle Electronics (CAVE) at Auburn University. The first configuration was called as Partial Interposer, where the *D-Pack*TM is sandwiched between the LTCC Ceramic package and the FR-4 PCB such that solder terminations on the top and bottom surface of the *D-Pack*TM (at package center) form the electrical and mechanical interconnections. This configuration did not have the solder balls on the outer periphery of the package. Figure 4 shows the partial interposer configuration.

The second configuration was called as Full Interposer, where in addition to the D- $Pack^{TM}$ capacitor matrix at the central core, the package was assembled with the PCB using an intermediate layer of FR-04 PCB with two rows of spherical solder ball forming the electrical and mechanical connections between package and the PCB.



Figure 4: Partial Interposer Configuration D-PackTM.



Figure 5: Full Interposer Configuration: *D-Pack*TM (Solder Joints at the periphery).

The objective of this chapter is to evaluate the thermo-mechanical reliability of these interconnect configurations using finite element simulations in ANSYS® and present the failure analysis report of the failed specimens. Life prediction calculations based on Inelastic Strain Energy Density (ΔW) have also been included in the report in order to compare results predicted from finite element models with experimental results. Table 2 shows the *D-Pack*TM configurations that were tested at the Center of Advance Vehicle Electronics (CAVE), Auburn University. The table also includes the details of the solder used in each configuration, the duration of the test as well as the hot / cold dwell times.

Configuration	Solder Type	Temperature	Dwell Times
		Range	(Hot / Cold)
Partial Interposer	Sn63-Pb37	0°C to 100°C	20 mins. / 20 mins.
Partial Interposer	Sn3.0Ag0.5Cu	0°C to 100°C	20 mins. / 20 mins.
Full Interposer	Sn3.0Ag0.5Cu	0°C to 100°C	20 mins. / 20 mins.

Table 2 : Configurations Tested for Thermal Shock Experiments

Figure 6 and Figure 7 figure show actual photographs of the D-Pack assemblies tested.



Figure 6: D- $Pack^{TM}$ assembled onto test PCB (without LTCC package on top). D- $Pack^{TM}$ is a matrix of individual D-sticks assembled together. Figure also shows the geometry / dimensions of D-stick.



Figure 7: LTCC Package (Top and Bottom View) with D-Pack Assembled onto the Package Land.

In order to capture the true symmetry of the package, quarter symmetry finite element models for both configurations were constructed. Figure 8 and Figure 9 show the quarter symmetry finite element model for partial interposer and full interposer configuration respectively. However, it was observed that the number of nodes in both models exceeded 1 million. Therefore, in view of the file size and the associated computational time for non-linear simulation, it was decided to study the thermomechanical reliability using slice models. Figure 10 and Figure 11 show the quarter symmetry finite element model for partial interposer and full interposer configuration respectively.



Figure 8: Quarter Symmetry Finite Element Model for D-PackTM Partial Interposer Configuration.



Figure 9: Quarter Symmetry Finite Element Model for D-PackTM Full Interposer Configuration.



Figure 10: Finite Element Slice Model for *D-Pack*TM Partial Interposer Configuration.



Figure 11: Finite Element Slice Model for *D-Pack*TM Full Interposer Configuration.



Figure 12: Close up view of D-StickTM (Finite Element mesh) and comparison with actual SEM picture for a pristine assembly.

3.2 Material Models : Constitutive Relationships

In general, a change in temperature causes the mechanical properties and performance of materials to change. Some properties and performance, such as elastic modulus and strength decrease with increasing temperature. Others, such as ductility, increase with increasing temperature. Therefore, in the material modeling of the various materials in the package, constitutive relations that predict strain as a function of stress, temperature, and time should be taken into consideration.

Linear and non-linear, elastic, plastic, creep, temperature, time dependent and time independent material properties have been incorporated in the finite element model. Most of the package materials are considered as linear elastic with no temperature dependency except solder. It is known that solder is above half its melting point at room temperature and therefore time-dependent creep phenomena dominates the solder joint fatigue life.

The thermal fatigue of electronic packages is associated with combined plasticdeformation and creep of solder joints. The Anand Viscoplasticity model (a standard material in ANSYS library) has been used by several researchers to model the constitutive behavior of the solder. The modeling methodology utilizes finite element analysis to calculate the viscoplastic strain energy density that is accumulated per cycle during thermal cycling. The Anand Viscoplasticity constitutive law has been used by Darveaux [1996, 2000], Zahn [2003] and several other researchers, toward the development of damage relationships. These relationships can be used for the life prediction of the electronic packages with solder joint cracking as the failure mode.

Anand's model [1985] is split into a flow equation and three evolution equations that describe the strain hardening or softening of materials.

Flow Equation:

$$\frac{d\varepsilon_p}{dt} = A(\sinh(\xi\sigma/s_0)^{1/m}\exp\left(\frac{-Q}{kT}\right)$$

Evolution Equations:

$$\frac{ds_0}{dt} = \left\{ h_0(|B|)^a \frac{B}{|B|} \right\} \left(\frac{d\varepsilon_p}{dt} \right)$$
$$B = 1 - \frac{s_0}{s^*} \qquad s^* = s^{-1} \left[\frac{d\varepsilon_p}{dt} \exp\left(\frac{Q}{kT}\right) \right]^n$$

The nomenclature and the material constants used for simulation are listed in Table 3. Also thermo-mechanical properties used for other material sets are listed in Table 3 below. The solder joints were meshed using element VISCO107, where as the other materials were meshed using SOLID45 in the ANSYS element library.

Definition	Sn63-Pb37	SAC 305
	[Darveaux 2000]	[Chang 2006]
Initial Value of Deformation Resistance s_0 (MPa)	12.41	45.9
Activation Energy <i>Q/R</i> (°K)	9400	7460
Pre-Exponential Factor A (sec-1)	$4.00 \ge 10^6$	5.87 x 10 ⁶
Multiplier of Stress ξ	1.5	2
Strain Rate Sensitivity of Stress m	0.303	0.0942
Hardening Constant h_0 (MPa)	1378.95	9350
Coefficient of Deformation	13.79	58.3
Resistance Saturation Value S [^] (MPa)		
Strain Rate Sensitivity of Saturation Value <i>n</i>	0.07	0.015
Strain Rate Sensitivity of Hardening <i>a</i>	1.3	1.5

Table 3: Anand's Constant for SAC105, SAC305 and SAC405

Material	Modulus	CTE	Poisson's
	of Elasticity (E)	(ppm/°C)	ratio
	MPa		
Copper Pad	128,932	16.30	0.34
Solder Mask	3,100	16.3	0.30
Solder (SAC 305)	47,572	25	0.35
Solder (Sn63-Pb37)	30,550	24	0.35
Silicon	162,716	25.4	0.28
Die Adhesive	6,769	52.5	0.25
Substrate	17,890 (X & Z)	12.4 (X & Z)	0.39 (XY & YZ)
	7846 (Y)	57 (Y)	0.11 (XZ)
РСВ	16,898 (X & Z)	14.50 (X & Z)	0.39 (XY & YZ)
	7,436 (Y)	67.20 (Y)	0.11 (XZ)
Mold	23,520	15	0.3

Table 4: Material Properties used for finite element modeling [Zahn 2003]

In ANSYSTM, VISCO107 element has plastic work (PLWK) as a standard output. Temperature cycling was simulated until total plastic strain energy density accumulated per cycle for the critical solder joint stabilizes. Inelastic work per volume per cycle was calculated for the elements at the interface of the solder interconnect with package pad and board pad. In order to overcome the stress singularity effects, volumetric averaging of inelastic strain-energy density (accumulated per cycle) across a layer of critical elements was done using the following formula:

$$\Delta W_{avg} = \frac{\sum_{k=1}^{N} \Delta W_{k} V_{k}}{\sum_{k=1}^{N} V_{k}}$$

Where ΔW_k is the plastic work for each element, V_k is the volume of each element.

3.3 Finite Element Models: Boundary Conditions

In order to save the computational time and effort, it is more practical to exploit the symmetry of the package. Some of the modeling options used includes quarter symmetry model, 1/8th model, diagonal slice, straight slice, etc. In order to compromise on the computational time, it was decided to explore the diagonal slice symmetry. However, on account of D-PackTM geometry being unsymmetrical along the diagonal, it was decided to create a straight slice model. The straight slice model extends from the center of a package out to the outermost solder joint (as shown in Figure 13). In this modeling approach, all materials are included through the thickness of the package, and the model captures a full row of solder joints from the center joints to the outermost joints. When the model itself is simplified, the boundary condition choices become more important on the effect of analysis. This slice plane is neither a true symmetry plane nor a free

surface [Zahn 2003]. A compromise between the two options is to couple the surface. For the slice plane surface, a coupling boundary condition of UZ on all nodes on the surface was chosen, and allows the plane to move freely in the Z direction, but is restricted in that plane. All boundary conditions applied for slice models in this research are displayed in Figure 13.



Figure 13: Boundary Conditions applied on the Straight Slice FE model.

3.4 Finite Element Models: Modeling Assumptions

Several assumptions were made in modeling electronic packages. Due to memory limits and computational time, and very complex geometries, intelligent simplifications had to be made to advance the modeling process. The LTCC package used in this study was a Flip Chip BGA (Ceramic Package). It would have been very tedious to incorporate the geometry effects of layers like underfill, solder bumps, thermal insulation material, adhesive between copper lid and substrate, etc. Moreover, in view of the objective to study the thermo-mechanical reliability of the 2nd level interconnects, these layers were not modeled explicitly. However, the physical effects of these layers have been included in the analysis using a smeared property [Clech 1996, 1998] / effective material approach

[Li 2003]. All layers above ceramic substrate were replaced by a single layer of material termed as 'smeared package'. The following equations were used to calculate the effective material properties:

$$\begin{aligned} h_{eff} &= \sum_{k=1}^{n} h_i \\ E_{eff} &= \frac{\sum_{k=1}^{n} E_i V_i}{\sum_{k=1}^{n} V_i} \\ \upsilon_{eff} &= \frac{\sum_{k=1}^{n} h_i \upsilon_i}{\sum_{k=1}^{n} h_i} \\ (CTE)_{eff} &= \frac{\sum_{k=1}^{n} (CTE)_i E_i V_i}{\sum_{k=1}^{n} E_i V_i} \end{aligned}$$

where

E = Modulus of Elasticity

v = Poisson's ratio

h = Layer Thickness

V = Volume

Subscript 'eff' indicates effective material property

Subscript '*i*' indicates individual layer

Another simplification used in the finite element model was the geometry of solder joints formed at the package / PCB interface with the D-PackTM. From Figure 12 (SEM image of pristine D-StickTM), we can see that the geometry of the joints at the

package side and the board side are different from one another. The joint is similar to Non-Solder mask Defined (NSMD) at the package side, and similar to Solder Mask Defined (SMD) at the board side. However, in view of the computational time, mesh continuity due to complex NSMD mesh geometry, joints at both interface were modeled as SMD.

Other simplifications include modeling the Ceramic Substrate and PCB board as homogeneous materials. In reality, these two components have several layers, adhesive, and traces. These features require extensive time to model, and due to their extremely small size relative to the package structure, their effect on the simulation results has been safely assumed to be minimal. Therefore these minute details have not been included in the model.

Also, it is known that strains near the solder joint interface (due to thermal cycling) can alter the chemical composition and grain structure of the alloy. However, finite element methodology currently does not offer the convenience of incorporating the changes in microstructure on account of thermal strains. Therefore, the intermetallics and the changes occurring in the solder joint microstructure have not been included in the analysis.

3.5 Post-Processing Results: Partial Interposer (Eutectic Sn-Pb Solder Joints)

The Partial Interposer package was modeled in ANSYS 10.0 with two solders (eutectic Sn-Pb and SAC 305) and subjected to thermal cycling in order to estimate plastic work accumulation to determine the reliability in a finite element simulation framework. In case of Partial Interposer configuration, mechanical and electrical

interconnections between the package and PCB were formed by the solder joints on the top and bottom terminations of the D-PackTM. Figure 14 shows the finite element slice model used. Two cycles were simulated in order to stabilize the stress – strain hysteresis loop. The area under the hysteresis loop was used to make life prediction calculations.



Figure 14: Finite Element Slice Model for Partial Interposer Configuration: Front View (2 Solders Tested: Eutectic Sn-Pb and SAC 305).

Figure 15 and

Figure 16 show the plots for accumulation of plastic work after simulation of two thermal cycles (0°C to 100°C, 20 min dwell /ramps) for eutectic Sn-Pb solder. It was seen that the D-PackTM solder joints farthest from package center were subjected to maximum amount of plastic work. Figure 17 shows the hysteresis loop for the solder element that underwent maximum amount of plastic work accumulation.



Figure 15: Contour plot of accumulated plastic work on the D-Pack[™] solder joints (Partial Interposer with eutectic Sn-Pb solder) at the end of two thermal cycles.



Figure 16: Plastic Work / Volume plot for critical of solder element layer (Partial Interposer with eutectic Sn-Pb solder) that was subjected to maximum plastic damage at the end of two thermal cycles.

Hysteresis Plot for D-PackTM Joint Element



Figure 17: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical solder joint element (eutectic Sn-Pb) that was subjected to maximum plastic damage at the end of two thermal cycles.

In order to overcome the stress singularity effects, volumetric averaging of inelastic strain-energy density (accumulated per cycle) across a layer of critical solder joint elements was done. The value was found out to be 0.5912 MPa.

Since the D-Pack is a multi-layer capacitor, and dielectric cracking is a very common mode of failure found in multilayer capacitors subjected to high temperatures, the variation of maximum principal stress generated in the dielectric during thermal cycling was also plotted versus time. Figure 18 shows the variation of maximum principal stress in the dielectric vs. time for two thermal cycles. It can be seen that that stress is maximum (~315 MPa) at the lowest temperature.



Figure 18: Variation of maximum principal stress in dielectric versus time, temperature.

3.6 Post-Processing Results: Partial Interposer (SAC 305 Solder Joints)

Figure 19 and Figure 20 show the plots for accumulation of plastic work after simulation of two thermal cycles (0°C to 100°C, 20 min dwell /ramps) for partial interposer configuration with eutectic SAC solder. Similar to partial interposer with eutectic Sn-Pb joints, it was seen that the D-PackTM solder joints farthest from package center were subjected to maximum amount of plastic work. Figure 17 shows the hysteresis loop for the solder element that underwent maximum amount of plastic work accumulation.



Figure 19: Contour plot of accumulated plastic work on the D-PackTM solder joints (Partial Interposer with SAC 305) at the end of two thermal cycles.



Figure 20: Plastic Work / Volume plot for critical of solder element layer (Partial Interposer with SAC 305 solder joints) that was subjected to maximum plastic damage at the end of two thermal cycles.

Hysteresis Plot for D-PackTM Joint Element



Figure 21: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical solder joint element (Partial Interposer with SAC 305 solder) that was subjected to maximum plastic damage at the end of two thermal cycles.

In this case, the volumetrically averaged value of inelastic strain-energy density (accumulated per cycle) across a layer of critical solder joint elements was found out to be 0.643 MPa. Figure 22 shows the variation of maximum principal stress in the dielectric vs. time for two thermal cycles. The nature of variation of principal stress was very similar to partial interposer with eutectic Sn-Pb joints, though the magnitude was found to be lower (~291 MPa).



Figure 22: Variation of maximum principal stress in dielectric versus time, temperature.

3.7 Post-Processing Results: Full Interposer (SAC 305 Solder Joints)

For Full Interposer, in addition to the D-PackTM capacitor matrix at the central core, the package was assembled using an intermediate layer of FR-04 PCB with two rows of spherical solder balls forming the electrical and mechanical connections between package and the PCB. Figure 23 shows the slice model used in the analysis.



Figure 23: Finite Element Slice Model for Full Interposer Configuration: Front View (SAC 305 solder).

Figure 24 to Figure 27 show the plots for accumulation of plastic work after simulation of two thermal cycles (0°C to 100°C, 20 min dwell /ramps) for SAC 305 solder. There were two solder joint geometries that were to be analyzed from the point of view of thermo-mechanical reliability, D-PackTM joints and the periphery joints (spherical). In both cases it was seen that the solder joints farthest from package center were subjected to maximum amount of plastic work, though the damage accumulation for D-PackTM was considerably more. Figure 29 and Figure 30 shows the hysteresis loop for the solder element (D-Pack joint and periphery joint respectively) that underwent maximum amount of plastic work accumulation.

In this case, the volumetrically averaged value of inelastic strain-energy density (accumulated per cycle) across a layer of critical solder joint elements was found out to be 0.62 MPa (D-Pack joint) and 0.2233 MPa (spherical periphery joint). Figure 31 shows the variation of maximum principal stress in the dielectric vs. time for two thermal cycles (Max value was ~ 291 MPa).



Figure 24: Contour plot of accumulated plastic work on the D-PackTM solder joints (Full





Figure 25: Contour plot of accumulated plastic work on the periphery solder joints (SAC 305 solder) at the end of two thermal cycles.



Figure 26: Plastic Work / Volume plot for critical of solder element layer in the D-PackTM joint (Full Interposer with SAC 305 solder) at the end of two thermal cycles.



Figure 27: Plastic Work / Volume plot for critical solder ball in the periphery joints (Full Interposer with SAC 305 solder) at the end of two thermal cycles.



Figure 28: Plastic Work / Volume plot for critical element layer in the periphery solder joints (Full Interposer with SAC 305 solder) at the end of two thermal cycles.



Hysteresis Plot for D-PackTM Joint Element

Figure 29: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical D-PackTM solder joint element (eutectic Sn-Pb) at the end of two thermal cycles.





Figure 30: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical periphery solder joint element (SAC 305) at the end of two thermal cycles.



Figure 31: Variation of maximum principal stress in dielectric versus time, temperature.

3.8 Post-Processing Results: Regular BGA (SAC 305 Solder Joints)

In order to compare the reliability of D-Pack configurations with contemporary packages being used, a BGA slice model was created with same material sets, same boundary conditions and subjected to same temperatures and ramp rates. Figure 32 shows the slice model used for analysis.



Figure 32: Finite Element Slice Model for BGA Configuration: Front View (SAC 305 solder).

Figure 33 and Figure 35 show the plots for accumulation of plastic work after simulation of two thermal cycles (0°C to 100°C, 20 min dwell /ramps) for SAC 305 solder. It was seen that the solder joints farthest from package center were subjected to maximum amount of plastic work. Figure 36 shows the hysteresis loop for the solder element that underwent maximum amount of plastic work accumulation.


Figure 33: Contour plot of accumulated plastic work on the tall solder joints (Regular

BGA with SAC 305 solder) at the end of two thermal cycles.



Figure 34: Plastic Work / Volume plot for critical of solder ball (Regular BGA with SAC 305 solder) subjected to maximum plastic damage at the end of two thermal cycles.



Figure 35: Plastic Work / Volume plot for critical element layer in the tall joint (Regular BGA with SAC 305 solder) at the end of two thermal cycles.



Hysteresis Plot for Regular BGA Solder Joint Element

Figure 36: Hysteresis plot (Shear Stress vs. Plastic Strain) for the critical solder joint element subjected to maximum plastic damage at the end of two thermal cycles.

In this case, the volumetrically averaged value of inelastic strain-energy density (accumulated per cycle) across a layer of critical solder joint elements was found out to be 0.1276 MPa.

3.9 **Results Summary:**

The results obtained for simulation for various configurations are summarized in Table 5 below. Using visco-plastic strain energy density as a metric for life prediction calculations, it can be seen that regular BGA (with tall solder joints) performs considerably better than all the other configurations analyzed. Also, based on the fatigue testing data on BaTiO₃ and S-N curves generated [Tanimoto et al. 1992] it can be safely assumed that for a cyclic stress of magnitude 315 MPa, D-PackTM dielectric would likely crack at approximately 10^6 cycles (well beyond the desired life cycle duration).

Configuration	Solder	Joint Type	Plastic Work	Max Principal Stress	
			(ΔW)	(in Dielectric)	
			MPa	MPa	
Partial Interposer	Sn – Pb	D-Pack	0.591	315	
(No Outer Joints)	SAC 305	D-Pack	0.643	292	
		D-Pack	0.620		
Full Interposer	SAC 305	Periphery	0.223	292	
		Solder Ball			
BGA (Tall Joints)	SAC 305	Tall Solder	0.127	NA	
		Ball			

Table 5 : Results Summary

3.10 Life Prediction vs. Experimental data:

Based on simulation and experimental data for several test configurations, different temperatures ranges, different ramp / dwell rates, Darveaux [1996, 2000], Zahn [2003] and several other researchers have developed empirical life prediction relationships. In these studies, Inelastic Strain Energy Density obtained from finite element simulation framework was correlated with the test failure data and empirical relationships were developed to predict the number of cycles to failure. The mode of failure considered for this study was solder joint cracking on account of fatigue.

In this study, empirical relationships presented by Zahn [2003] have been used to calculate the cycles to failure for both eutectic Sn-Pb as well as lead free solder joints. The form of the equation used in this study is as follows:

$$N_{63,2} = C_1 (\Delta W)^{C_2}$$

Where

 ΔW – Averaged inelastic strain energy density at the solder / pad interface.

 C_1, C_2 – Constants obtained by correlating the test data with simulation.

Table 6 below summarizes the life prediction calculations based on ΔW calculated for the various D-Pack constructions analyzed above. Figure 39 shows the hysteresis loops (for critical element in solder joint) for various configurations analyzed.

Configuration	Solder	Joint	Plastic Work	Characteristic Life
		Туре	(ΔW) MPa	N _{63.2%} (Cycles to
				failure)
Partial	Sn – Pb	D-Pack	0.591	2143
Interposer	SAC 305	D-Pack	0.643	2814
Full	SAC 305	D-Pack	0.620	2833
		Periphery	0.223	3322
interposer		Solder Ball		
BGA	SAC 305	Tall Solder	0.127	3627
(Tall Joints)		Ball		

Table 6: Life Prediction Calculations (Summary)



Plastic Shear Strain

Figure 37: Hysteresis loops (for critical element in solder joints) for various configurations analyzed.

Since the stabilization of hysteresis loop implies a constant rate of damage accumulation with each cycle, it can be reasonably concluded that BGA configuration undergoes least amount of damage/cycle, and therefore would have the largest characteristic life. Figure 38 and Figure 39 show the two-parameter Weibull plots for thermal shock experiments conducted for partial and full interposer configurations.



Figure 38: Two parameter Weibull plot for Thermal Shock Experiments (0°C to 100°C, 20 min ramp / dwell) on D-Pack Partial Interposer test assemblies (with both Sn-Pb and SAC solder)



Figure 39: Two parameter Weibull plot for Thermal Shock Experiments (0°C to 100°C, 20 min ramp / dwell) on D-Pack Full Interposer test assemblies (with SAC solder)

Figure 40 shows the comparison of life data based on thermal shock experiments with life prediction based on simulations. We see that life predicted from simulations is within $\pm 20\%$ of the experimental data, which is within the acceptable limits.



Comparison of Experimental vs Predicted Values

Figure 40: Comparison between life prediction data (based on simulations) with experimental data.

3.11 Failure Analysis:

In order to identify the failure mode, the tested assemblies were cross-sectioned and studied by a Field Emission Scanning Electron Microscope instrument (SEM), JEOL JSM-7000F operated at an accelerating voltage of 20 kV. Most solder joint failures were found on the farthest D-Stick, inline with the finite element model predictions. More solder joint failures were found on the package side than on the board side. The joints on the package side are more like Solder Mask Defined (SMD) while those at the board side are Non-Solder Mask Defined (NSMD). It may be possible to attribute this skewed failure distribution (on the package side) to the fact that NSMD morphology performs better than SMD pads. In one of the samples, dielectric cracking was also observed. The location of dielectric cracking was also inline with the results predicted from finite element simulations. Representative figures for solder joint failure (package / board side), dielectric cracking, etc for different configurations are shown below.



Figure 41: SEM image of failed D-Pack assembly (Partial Interposer with eutectic Sn-Pb solder joints). Dielectric cracking at the package side.



Figure 42: SEM image of failed D-Pack assembly (Partial Interposer with eutectic Sn-Pb solder joints). Solder Joint cracks on package side and board side.



Figure 43: SEM image of failed D-Pack assembly (Partial Interposer with eutectic SAC solder joints). Solder Joint cracks on package side and board side.



Figure 44: SEM image of failed D-Pack assembly (Full Interposer with SAC solder joints). Outer periphery Solder Joint cracks on top row and bottom row.



Figure 45: SEM image of failed D-Pack assembly (Full Interposer with SAC solder joints). Outer periphery Solder Joint cracks on top row and bottom row.

3.12 Summary & Conclusion:

The thermo-mechanical reliability of D-Pack has been evaluated using finite element models. Slice models were created for different configurations (Partial Interposer, Full Interposer), solders (eutectic Sn-Pb, SAC) in ANSYS and subjected to two thermal cycles from 0°C to 100°C (20 min dwell / ramps). The reliability was assessed from the point of view of fatigue in solder joints as well as capacitor dielectric cracking.

Volumetrically averaged visco-plastic strain energy density (across a layer of critical elements) was used as a metric to calculate the damage in solder joints due to cyclic temperature loading. Based on empirical relations for life prediction available in literature, cycles to failure was calculated using the energy approach and the predictions were compared with experimental data. The predictions based on finite element methodology were in close agreement with the experimental data.

The maximum principal stress generated in the dielectric was also observed during the simulation. Based on the S-N curves available from fatigue testing for BaTiO₃ (dielectric in D-Pack), it was concluded that the stresses generated in D-Pack were well within the maximum stress limits.

Also, in order to correlate the failure locations predicted by finite element simulations, the tested (failed) assemblies were cross sectioned and observed under Scanning Electron Microscope (SEM). The solder joint failures and dielectric cracking observed in failed samples were inline with the results shown during the finite element post processing.

CHAPTER 4

PROGNOSTICS HEALTH MANAGEMENT OF SnAgCu SOLDER ELECTRONICS IN HARSH AGING ENVIRONMENTS

There is a growing need to develop and demonstrate technologies that can monitor and predict the remaining service life of key elements including electronics in implantable biological applications [Stanton 2002], automotive applications [Bodensohn 2005], defense [Grietzer 1999], and civil infrastructure applications [Bond 1997]. Health Monitoring (HM) refers to the broad concept of assessing the ongoing, in-service performance of a system using a variety of measurement techniques.

Health Monitoring is aimed at the immediate detection and diagnosis of offnormal system operation, and to take real-time corrective actions to avert the possibility of a system failure. The technical approach here relies on fusion of heterogeneous information derived from physics-based models of fatigue damage and real-time sensor data [Keller 2003]. HM can also provide the Operation and Maintenance (O&M) team with the information necessary to select and follow the optimum asset management path leading to substantial reduction in life cycle cost of the system [Jarrell 2002]. Prognostics refer to interrogation of material state of a system based on computation of certain proxies, stressors, and to predict the Residual Life (RL) of the system for the intended environment. Pacemakers and implantable cardioverter-defibrillators (ICDs) are among the most critical life-support and complex medical devices in use today. However, several recent high-profile device malfunctions have called into question their safety and reliability. Several database registries including the United Kingdom, Danish and Bilitch Registries have monitored pacemaker and ICD safety performance. In total, hundreds of device malfunctions affecting dozens of pacemaker and ICD models have been reported. A study of pacemaker and ICD advisories, a surrogate marker of device reliability, demonstrated that the number and the rate of pacemakers and ICDs affected by advisory has increased since 1995 [Hauser 2001, Maisel 2001, 2002, Song 1994, Stanton 2002].

Previously, the PHM of mechanical structures has been done by dynamic analysis based on natural frequencies, mode shapes, damping factors, and static analysis based on deformation or changes in structure orientation due to load or unexpected damage, using innovative signal processing, new sensors, and control theory [Kok 2005]. New advances in sensor technology and failure analysis have catalyzed a broadening of application scope for prognostication systems to include large electromechanical systems such as aircraft, helicopters, ships, power plants and many industrial applications. HM application areas include fatigue crack damage in mechanical structures such as those in aircraft [Munns 2000], surface ships [Baldwin 2002], civil infrastructure [Chang 2003], railway structures [Barke 2005] and power plants [Jarrell 2002].

In case of mechanical systems like propulsion systems, compressors, gears, etc damage progresses mainly due to wear (prolonged usage), or imbalance condition in one of the rotating elements, or from misalignment of the shafts of the rotating components which leads to changes in the vibration signature of the equipment. By comparing the vibration signals from the defective equipment with those from sound equipment, the performance degradation can be characterized [Dyne 1992].

Other examples include, aircraft engines, which start and stop quite frequently and run at high speeds, a model-based method has been used for the on-line identification of cracks in a rotor while it is passing through its flexural critical speed [Sekhar 2003]. Detection of surface corrosion has been used to reduce the maintenance required, and trigger preventive repair for increased aircraft availability and significantly reduced cost of ownership. Fluorescent fiber optic sensors that detect aluminum coating from the early stages of the corrosion process have been used for providing early warning of corrosion in susceptible areas of an aging aircraft [Maalej 2004].

Optical fiber based sensor system has been used on concrete structure to evaluate its performance for health monitoring [Fernando 2003]. Monitoring bridge performance has been done to answer questions on the performance of existing bridges, refine techniques needed to evaluate different bridge components, and develop approaches that can be used to provide a continuous picture of a bridge's structural integrity using structural health monitoring [DeWolf 2002]. Transducers along with a wireless data acquisition system can enable the possibility of achieving long distance monitoring [Kok 2005]. These techniques help in detection of damage of bridges or building to avoid the economic and social effect of aging and deterioration [Chang 2003].

Wayside detection involving fault identification using interrogating sensors placed along the sides of railway tracks has been used in the railway industry for gathering information about vehicle performance. Information on the vehicle condition and performance over an extended period of time is recorded in an online database, which is interrogated for critical performance parameters to provide information on condition of in-service railway vehicles [Barke 2005]. In other applications, signal feature analysis is used to detect abnormalities related to impending failure indication by an inference system using an historical database [Hess 2001, 2002].

Wear and degradation in electronics is very difficult to detect and inspect compared to most other mechanical systems and structures due to complex and tiny structure. Health management of electronic systems requires knowledge of impending failure. Presently, acquisition of mechanical system-diagnostics has been successfully achieved for automotive applications through an elaborate system of fault codes. The state-of-art health management systems focus on detection and isolation of faults and failures, and are largely reactive in nature, limiting the scope of maintenance decisions.

Built- In-Self Test (BIST) circuit, which includes onboard hardware and software diagnostic, has been used for error detection and fault location [Drees 2004]. BIST is a methodology that embeds additional functionality in the product to give it the ability to test and diagnose itself with minimal interaction from external test equipment [Chandramouli 1996, Hassan 1992, Williams 1983, Zorian 1994]. BIST controllers are typically used for reactive failure detection, to output failure data that can be correlated to show exactly when the failure occurred. This data can then be interpreted by diagnostic software to analyze the cause of failure. For example, Pseudo-Random Binary-Sequence (PRBS) test pattern generators, apply input vectors to digital or analog [Al-Qutayri 1992] modules. Self-Checking circuit designs provide on-line test for digital [Lala 1985] as well as for analog circuits [Kolarik 1993]. The obtained output is then compared with a "golden response".

The results obtained from BIST functions can generate diagnostic information which in turn provides additional confidence in the measurement result and confirm the device availability. BIST helps in minimizing the interaction with external automated test equipment (ATE) as well as provides the advantage of a more robust "at-speed" test of the circuitry; however, the current form gives little insight about the system level reliability or the remaining useful life of the system. Several studies conducted [Allen 2003, Drees 2004, Gao 2002, Rosenthal 1990] have shown that BIST can be prone to false alarms and can result in unnecessary costly replacement, re-qualification, delayed shipping, and loss of system availability.

Fuses and Canaries have been used to provide advance warning of failure in electronics due to specific wear out failure mechanism [Vichare 2006]. Fuses within circuits and thermostats, can be used to sense the abnormal conditions like voltage transients, critical temperature limit and to make adjustment to restore normal condition [Ramakrishnan 2000]. Canary devices like pre-calibrated cells which are located with the actual circuitry on the same chip experience similar stresses as the actual component, this leads to same damage mechanism. The cells are designed to fail faster by scaling the stress which is been experienced to avoid the catastrophic failure of actual component. The failure of the canary devices can be used to estimate the time to failure of actual product [Mishra 2002]. Similarly canary components created on printed circuit board is been used for prognostication by failing before the actual component [Anderson 2004]. However, replacement of fuses and canaries impacts the maintenance, repair and part replacement making it difficult to integrate these systems with host system. In addition, fuses provide limited insight into the remaining use life prior to fuse-failure.

The reliability of electronic control and safety systems in harsh environment applications, such as automotive safety systems, can be significantly impacted through development of methodologies for monitoring the degradation and understanding damage evolution to enable avoidance of system-level failures. Challenges in implementing prognostics can be attributed to the lack of understanding of the underlying component degradation mechanisms.

An electronic component operating in a harsh environment is subjected to both temperature variations as well aging for a finite duration during use-life. Therefore, a time-temperature history of the electronic system ambient would be extremely helpful in using life prediction models and computing life. Continuous capture of time-temperature history would put immense demands on existing system function. Reconstruction of operational profiles is often challenging and future operational profiles often unpredictable. In addition, it may not be always possible to characterize the operational loads under all possible scenarios (assuming they are known and can be simulated). Damage pre-cursors target fundamental understanding of underlying degradations in electronic systems, such a thermo-mechanical interconnect-fatigue, interfacial delamination of underfills, etc. Once identified for specific package elements and failure mechanisms, the pre-cursors are scalable for future package architectures and for application across a broad spectrum of designs.

In this study, a mathematical approach has been presented to calculate the prior damage in electronics subjected to isothermal thermo-mechanical loads. PHM approach presented in this paper is different from state-of-art diagnostics and resides in the prefailure-space of the electronic-system, in which no macro-indicators such as cracks or delamination exist. The presented PHM methodologies enable the estimation of prior damage in deployed electronics by interrogation of the system state.

In this study, investigation of the changes of the features as well as time-evolution of physical damage, and the relationship between physical damage and feature-set has been established for thermo-mechanical stresses. Comprehensive heath monitoring framework proposed here will facilitate quick assessment of system state and potential for failure of critical electronic systems. A methodology for pre-cursors based computation of residual life of electronic systems has been presented. A damage precursors based residual life computation approach for various package elements has been developed, to prognosticate electronic systems prior to appearance of any macroindicators of damage (Figure 46).



Figure 46: Damage Pre-Cursors Based Methodology for Prognostication of Electronic Systems.

In order to implement the system-health monitoring system, precursor variables or leading indicators-of-failure have been identified for various package elements and failure mechanisms. Model-algorithms have been developed to correlate precursors with impending failure for computation of residual life. The correlations serve a basis for interrogation of damage-state and extraction of features quantifying underlying degradation. Examples of damage pre-cursors include phase-growth, intermetallic thickness, and patterns in interfacial stress distributions. Change in damage pre-cursors are sensed through a network of system-state monitors. Mathematical relationships have been developed for computation of residual life based in terms of damage proxies.

The pre-cursor based damage computation approach eliminates the need for knowledge of prior operational stresses and enables health management of deployed nonpristine electronic systems under unknown prior-loading conditions. The approach is powerful, since it reduces the demands on electronic system field-usage and deployment logistics required for acquisition of prior stress histories. Use of pre-cursors for damage computation addresses the limitation of life-prediction model based prognostication techniques, which target damage estimation for known stress histories imposed on pristine materials. Examples of life prediction models include Paris's Power Law [Paris, et. al 1960 1961], Coffin-Manson Relationship [Coffin 1954; Tavernelli, et. al. 1959; Smith, et. al. 1963; Manson, et. al. 1964] and the S-N Diagram.

4.1 Test Vehicle

Area-array packages with 95.5Sn4.0Ag0.5Cu solder balls assembled on FR4-06 laminates and immersion Ag finish have been studied under isothermal aging at 125°C.

Phase growth data has been gathered and analyzed using image processing. Components analyzed include various packaging architectures including, plastic ball-grid arrays, chip-array ball-grid arrays, tape-array ball-grid arrays, flex-substrate ball-grid arrays, and discrete resistors. Ball counts are in the range of 64 to 676 I/O, pitch sizes are in the range of 0.5 mm to 1mm, and package sizes are in the range of 6mm to 27mm (Table 7). The boards contain six trace layers to simulate the thermal mass of a true production board, though all functional traces were run on the topmost layer.



TARRAY 144

Figure 47: Test Vehicle

Body Size	Package Type	Ball	Ball	Die	Die	BT	BT Pad	Ball
		Count	Pitch	Thickness	Size	Thickness	Туре	Diameter
			(mm)	(mm)	(mm)	(mm)		(mm)
6 mm	TABGA	64	0.5	0.36	4	0.36	NSMD	0.32
7 mm	CABGA	84	0.5	0.36	5.4	0.36	NSMD	0.48
10 mm	TABGA	144	0.8	0.36	7	0.36	NSMD	0.48
15 mm	PBGA	196	1	0.36	6.35	0.36	SMD	0.5
16 mm	FlexBGA	280	0.8	0.36	10	0.36	NSMD	0.48
27 mm	PBGA	676	1	0.36	6.35	0.36	SMD	0.63

Table 7: Experimental Design

Phase growth and intermetallic-growth under steady-state temperature have been identified as pre-cursors for understanding progression of damage in this study. Evolution of solder microstructure and the growth of intermetallic due to thermal fatigue have been reported previously by several researchers.

4.2 Damage Proxies: Lead-Free Solder Grain Coarsening

Electronics deployed in underhood automotive applications is subjected to temperature variations in the neighborhood of -40°C to 125°C. These temperature excursions during operation of a circuit are due to both power-cycling and variations in ambient conditions resulting in thermo-mechanical cyclic stresses and strains induced primarily by thermal expansion mismatch between the package and the board assembly. Micro-structural coarsening during thermo-mechanical deformation is attributed to the generation of excess vacancies caused by the combined effect of local hydrostatic state of stress, and the instantaneous inelastic strain rate [Dutta 2003^a, 2003^b, 2004; Jung 2001].

Previous researchers have examined changes in microstructure occurring in the Sn63/Pb37 and lead-free chip resistor solder joints during thermal cycling [Sayama, et al. 1999, 2003], investigated the grain-size evolution and derivatives of phase growth rate as prognostics parameters on a wide range of leaded devices in underhood applications [Lall, et. al. 2004^b], correlated thermal fatigue with occurrence of microstructural coarsening in the fatigue damaged region in of 63Sn37Pb solder interconnects [Frear, et. al. 1990, Morris, et al. 1991]. Correlation of grain coarsening with thermal fatigue has also been established for high-lead solders [Bangs, et. al. 1978, Wolverton 1987, Tribula, et. al. 1989]. In this study, prognostics health management methodology has been presented to assess the prior damage is based on solder grain coarsening model. Phase growth under thermal aging has been identified as the damage precursor to compute the residual life.

In this study, changes in solder microstructure and its derivatives have been investigated for use as the leading indicators of failure and interrogation of system state for assessment of damage from prior stress histories. Quantitative metrics of changes in microstructure have been identified and relationships developed to represent damage progression. Data presented covers a wide range of Sn4Ag0.5Cu lead-free packaging architectures and discrete devices in extreme steady-state temperature environments.

The phase growth parameter has been defined as the relative change from phasestate after reflow, instead of the absolute value of phase state. Figure 48 shows Ag₃Sn Grains in 95.5Sn4Ag0.5Cu microstructure. The fundamental reason for selection of phase growth and its derivatives is that, superplastic alloys are usually made of fine grain structure. Therefore a considerable growth of the matrix grains and the second phase particles frequently occurs during high temperature deformation. The grain growth rate (per unit time) is found to increase with increasing strain rate.



Figure 48: Ag₃Sn Grains in 95.5Sn4.0Ag0.5Cu solder microstructure

Callister [1985] states that for many polycrystalline materials phase size varies with time according to the following relations.

$$g^n - g_0^n = Kt \tag{1}$$

Where g is the phase size at time t, and g_0 is the initial phase size, and K and n are time independent constants. The value n is generally varies between 2 to 5. The process of the particle growth induced by volume diffusion was theoretically analyzed by Lifshitz, et al. [1961]. It was revealed that the variation of the average particle radius with time is

$$r^{3} - r_{0}^{3} = B_{1} \frac{\gamma \Omega C_{0} D_{b}}{RT} t$$
 (2)

where r is the average particle radius, r_0 is the initial radius of an average particle, B_1 is the parameter related to the volume fraction of the particles, γ is the free energy per unit area of the phase boundary, Ω is the molar volume of the particle phase, C_0 is equilibrium solute concentration near the phase boundary. D_b is the coefficient of solute diffusion in the phase boundary. R is the gas constant, T is the absolute temperature, and t is time.

Senkov and Myshlev [1986] applied the theory the phase growth process of a superplastic alloy and validated the theory in that of Zn/Al eutectic alloy. They expressed the evolution of the average phase size g with the time as shown below,

$$g^4 - g_0^4 = \frac{B\delta\Omega C_0 D_b}{RT}t$$
(3)

Where g_0 is the initial average phase size, B is the phase geometry parameter, δ is the phase boundary width. Dutta [2003^a, 2003^b, 2004] represented the total vacancy concentration at any location within the solder joint at any instant of 't' may be written as the sum of the equilibrium vacancy concentration, and vacancy concentration under applied instantaneous strain rate,

$$n_{total} = n_{eqlm} + n_{strn} \tag{4}$$

$$n_{eqlm} = \exp\left(\frac{-Q_{f,v}}{kT}\right) \exp\left(\frac{\sigma_h \Omega}{kT}\right)$$
(5)

$$n_{strn} = \exp\left(\frac{-Q_{f,v}}{kT}\right) \exp\left(\frac{\sigma_{h}\Omega}{kT}\right) N\dot{\varepsilon} \left[1 - \exp\left(\frac{-t}{\tau_{c}}\right)\right]$$
(6)

Here, $Q_{f,v}$ is the enthalpy of formation of a vacancy, Ω is the molar volume, τ_c is a time constant associated with the decay of a vacancy following formation, and N is a constant that scales the vacancy concentration to $\dot{\varepsilon}$.

Based on Lifshitz-Wagner theory, and assuming a linear time dependence of temperature $(T = T_{min} + \beta t)$ during thermal cycle, Dutta [2003^a, 2003^b, 2004] showed that the final particle size, at any time r(t) can be expressed as,

$$r(t) \approx \left\{ \left[\left(\frac{B_1 \gamma_s V_m C_0}{RT} \right) \overline{D}_{sol} \left(t + 2N \hat{\eta}_{hc} \nu_c \phi \right) + r_0^3 \right]^{1/3} \right\}$$
(7)

Where,

$$\overline{D}_{sol} = \frac{\int_{0}^{sol} D_{0}^{sol} \exp\left[\left(\frac{\sigma_{h}\Omega}{k} - \frac{Q_{sol}}{R}\right)\frac{1}{T}\right]dt}{\int_{0}^{t_{hc}} dt}$$
(8)

and, D_{sol} is the effective solute diffusivity in the matrix, D_{sol}^{0} and Q_{sol} are the associated frequency factor and activation energy, $\hat{\gamma}$ is the average shear-strain rate during a half cycle, and can be approximated as $\hat{\gamma} \approx \frac{\Delta \alpha (T_{max} - T_{min})}{ht_{hc}}$, where $(T_{max} - T_{min})$ is the temperature range of the cycle, v_c is the number of thermal cycles, each with a half period of t_{hc} .

In the Equation (7), when $\hat{\gamma} = 0$, value of phase-radius, r, represents the coarsened size caused by isothermal aging only. For $\hat{\gamma} \neq 0$, the value of phase-radius, r, includes contributions caused by both static aging and strain-enhanced (thermal cycling) coarsening.

Samples were subjected to single-stresses of steady-state temperature at 125°C. The stresses were increased gradually in magnitude. The samples were cross-sectioned at various level of stress and exposure length. The cross-sections were studied by a Field Emission Scanning Electron Microscope instrument (SEM), JEOL JSM-7000F operated at an accelerating voltage of 20 kV. The pictures were taken at magnification of 750x. All samples were imaged after polishing and etching to reveal grain structure. The quantitative measure of Ag₃Sn particle size was established from a 60µm x 45µm rectangular region selected from a backscattered SEM image of a highest strain corner

solder ball. The location of the examination region was identical for various samples. Grain size was averaged from various samples for each package architecture and stress exposure. The typical SEM pictures before and after the mapping of phase size using image analysis are shown in Figure 49 and Figure 50.



Figure 49: Micrograph from 7 mm BGA showing Tin and Ag₃Sn Phases



Figure 50: Microstructure mapping using Image Analysis

Error! Reference source not found. Figure 51 to Figure 57 shows SEM backscattered images exhibiting an example of Ag₃Sn phase growth process in different BGA packages during thermal aging test condition.



Figure 51: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,

95.5Sn4Ag0.5Cu solder, 16 mm BGA, Magnification: 750x)



Figure 52: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,

95.5Sn4Ag0.5Cu solder, 27 mm BGA, Magnification: 750x)



Figure 53: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,

95.5Sn4Ag0.5Cu solder, 15 mm BGA, Magnification: 750x)



Figure 54: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,

95.5Sn4Ag0.5Cu solder, 15 mm BGA, Magnification: 750x)



Figure 55: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,

95.5Sn4Ag0.5Cu solder, 10 mm BGA, Magnification: 750x)



Figure 56: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,

95.5Sn4Ag0.5Cu solder, 7 mm BGA, Magnification: 750x)



Figure 57: SEM Back-scattered Images of Phase Growth versus Thermal Aging (125°C,

95.5Sn4Ag0.5Cu solder, 6 mm BGA, Magnification: 750x)



Figure 58: Phase Growth Parameter versus Aging Time at 125°C for PBGA 676 SnAgCu

Alloy Solder Interconnects.



Figure 59: Phase Growth Parameter versus Aging Time at 125°C for PBGA 196 SnAgCu

Alloy Solder Interconnects.



Figure 60: Phase Growth Parameter versus Aging Time at 125°C for TAPE ARRAY 144

SnAgCu Alloy Solder Interconnects.



Figure 61: Phase Growth Parameter versus Aging Time at 125°C for FLEX 280 SnAgCu

Alloy Solder Interconnects.



Figure 62: Phase Growth Parameter versus Aging Time at 125°C for CABGA 84 SnAgCu Alloy Solder Interconnects.



Figure 63: Phase Growth Parameter versus Aging Time at 125°C for TAPE ARRAY 64 SnAgCu Alloy Solder Interconnects.

From this graphs we have found that phase growth rate varies for different components. Figure 58 to Figure 63 shows a comparative study of phase growth rate between various packaging architectures with 95.5Sn4Ag0.5Cu alloys. A correlation between phase growth rate and time can be used as a proxy parameter and evaluation of time at temperature for a deployed part.

4.3 Damage Proxies: Intermetallic Coarsening

Solder joint formation involves wetting and bonding interactions between the solder alloy and the substrate metal. In most cases this interaction manifests itself as reaction between the tin phase and the substrate metal to produce inter-metallic compound (IMC) layers. These are hard, brittle, stoichiometric, metal-metal compounds with high melting points. [Mackay & Levine 1986]. For copper and tin-lead eutectic solder alloy, two such compounds are formed, resulting in a duplex layer consisting of

Cu₃Sn at the copper interface and Cu₆Sn₅ at the tin interface [Unsworth 1976, Kay 1973, --- 1979].

Solid-state IMC layer growth has been investigated for several Sn-containing solders on Cu including the following couples: 63Sn-37Pb/Cu (wt.%), 100Sn/Cu, 96.5Sn-3.5Ag/Cu, 95.5Sn-0.5Ag-4.0Cu/Cu, 95Sn-5Sb/Cu, 91.84Sn-3.33Ag-4.83Bi/Cu, and 58Bi-42Sn/Cu [Vianco 1994^a, 1994^b, 1995, 1999, 2001, 2004 Pang et. al 2001, Tu 1997, Harris 1998, Gupta 2004]. These cited studies and various other researchers have documented the composition and growth kinetics of the IMC layers that develop at the solder/Cu interface.

In this portion of the study, the growth of the intermetallic thickness during thermal aging as leading indicator of failure has been explored. In order to investigate the correlation of interfacial intermetallic thickness growth versus thermal aging, the component has been cross sectioned at various interval of thermal aging. The aged components are sliced periodically to measure the thickness in SEM using 1000x magnification. The mean thickness of IMC layers are measured using commercial image processing software on SEM images. An energy dispersive X-ray (EDX) has been used to examine the morphology and the composition of the intermetallic compound layer at the copper/solder interface. Colloidal silica solution has been applied for the detailed intermetallic compound composition observation and detection.

The interfacial intermetallic layers are formed between solder and copper, and some precipitates appeared near the interface of the IMCs/solder. The intermetallic layers were identified in SEM micrograph and the morphologies are identified by EDX as Cu₃Sn and Cu₆Sn₅ phases. The compositions of the IMC layer are identified as Cu₆Sn₅
for the layer near the Solder Interconnect, and Cu₃Sn, for the layer near the Copper Pad. With the increasing aging time, the IMC layers thicken, and the local irregularities appear to gradually smooth out. Figure 64 shows SEM backscattered images exhibiting an example of intermetallic growth process in the 17 mm BGA solder ball during the thermal aging test condition.



Figure 64: SEM Back-scattered images of IMC Growth versus Thermal Aging for Sn4Ag0.5Cu (Magnification 1000x)

Trend analysis of intermetallic thickness growth on SEM using image processing software, indicates a square root dependence of IMC thickness versus aging time,

$$y = y_0 + kt^n \tag{9}$$

where y(t) is IMC growth thickness during aging, y_0 is the initial thickness of intermetallic compounds, k is the coefficient standing for the square root of the diffusivity at aging temperature, and t is test time. The exponent value, $n = \frac{1}{2}$ has

been used in Equation (9) above, which reveals a diffusion-controlled mechanism during aging. The IMC growth data in this study indicates that growth rate stays fairly uniform during the thermal aging. It is observed that for both Sn-Ag solder systems, the intermetallic compound thickens roughly as $t^{1/2}$ in a linear manner, where t is the aging time as expected for diffusion-controlled growth.

The average IMC growth measured at each level of test time for each component set cross-sectioned has been shown in Figure 65 to Figure 70.



Figure 65: IMC Growth, at Various Levels of time for PBGA 676 with 95.5Sn4Ag0.5Cu Alloy.



Figure 66: IMC Growth, at Various Levels of time for PBGA 196 with 95.5Sn4Ag0.5Cu Alloy.



Time, hr^0.5 Figure 67: IMC Growth, at Various Levels of time for FLEX 280 with 95.5Sn4Ag0.5Cu

Alloy.



Figure 68: IMC Growth, at Various Levels of time for TAPE ARRAY 144 with

95.5Sn4Ag0.5Cu Alloy.



Figure 69: IMC Growth, at Various Levels of time for CABGA 84 with 95.5Sn4Ag0.5Cu

Alloy.



Figure 70: IMC Growth, at Various Levels of time for TAPE ARRAY 64 with 95.5Sn4Ag0.5Cu Alloy.

From this graphs we see that IMC growth rate varies for different components. Figure 65 to Figure 70 shows a comparative study of IMC growth rate between various packaging architectures with 95.5Sn4Ag0.5Cu alloys. A correlation between IMC growth rate and time can be used as a proxy parameter and evaluation of time at temperature for a deployed part.

4.4 Interrogation of System State

We have so far characterized the evolution of damage proxies (phase growth, IMC growth) by subjecting test packages to discrete time intervals of isothermal stress. In this section, a methodology for determining prior damage by interrogating the damage proxies of test structures has been presented. A set of electronic assembly has been subjected to thermal aging (125°C). The thermal environment is intended to simulate a field application environment. The parts are withdrawn form the application environment for redeployment in a new field environment. The damage proxies have been interrogated

to determine the extent of damage inflicted and also remaining useful life of that assembly if it is to be redeployed. Following sections will explain the prediction of stress history using phase growth and IMC growth in thermal aging environments.

4.5 Levenberg – Marquardt Algorithm

The relationship between the phase growth parameter and time is nonlinear because it contains terms with fourth power. Inverse solution for interrogation of systemstate is challenging for damage evolution in such systems. Levenberg-Marquardt (LM) algorithm is an iterative technique that computes the minimum of a non-linear function in multi-dimensional variable space [Madsen 2004, Lourakis 2005, Nielsen 1999]. It has been used successfully for computation of nonlinear least-square solutions. The Levenberg-Marquardt method with a combination of steepest descent using line-search and the Gauss-Newton method has been used for solution of the problem.

Let *f* be an assumed functional relation between a measurement vector referred to as prior-damage and the damage parameter vector, p, referred to as predictor variables. Mathematically, the function, f, which maps a parameter vector $p \in Rm$ to an estimated measurement vector is represented as, $x=f(p) \ x \in Rn$. The measurement vector is the current values of the leading-indicator of failure and the parameter vector includes the prior system state, and accumulated damage and the damage evolution parameters. An initial parameter estimate p_0 and a measured vector x are provided and it is desired to find the parameter vector p, that best satisfies the functional relation *f* i.e. minimizes the squared distance or squared-error, $\varepsilon^{T}\varepsilon$ with $\varepsilon = x - f(p)$. Assume that $g(p) = \varepsilon^{T}\varepsilon$ in the squared error. The basis of the LM algorithm is a linear approximation to g in the neighborhood of p. For a small δp , a Taylor series expansion leads to the approximation

$$g(p + \delta p) \approx g(p) + J(p)\delta p$$
 (10)

Where, $J = Jacobian matrix \partial f(p)/\partial p$. For each step, the value of δp that minimizes the quantity $\varepsilon = x - Jf(p)$, has been computed. Then the minimizer parameter vector, p, for the error function has been represented as,

$$F(p) = \frac{1}{2} \sum_{i=1}^{m} (g_i(p))^2 = \frac{1}{2} ||g(p)||^2 = \frac{1}{2} g(p)^T g(p)$$

$$F'(p) = J(p)^T g(p)$$
(11)

$$F''(p) = J(p)^T J(p) + \sum_{i=1}^{m} g_i(x) g_i''(x)$$

Where F(p) represents the objective function for the squared error term $\varepsilon^{T}\varepsilon$, J(p) is the Jacobian, and F'(p) is the gradient, and F''(p) is the Hessian. An initial parameter estimate p₀ and a response-vector "x" are provided and it is desired to find the vector p+, that best satisfies the functional relation x=f(p), while minimizing the squared distance $\varepsilon^{T}\varepsilon$. The steepest gradient descent method has been used to impose the descending condition, i.e., $F(p_{k+1}) < F(p_k)$. Depending on the starting guess p₀, a given function may have numerous minimizers, not necessarily the global minima. It therefore becomes necessary to explore the whole bounded space to converge to the global minima. The iteration involves finding a descent direction "h" and a step length giving a good decrease in the F-value.

The variation of an F-value starting at "p" and with direction "h" is expressed as a Taylor expansion, as follows:

$$F(p+\alpha h) = F(p) + \alpha h^{T} F'(p) + O(\alpha^{2})$$
(12)

where α is the step-length from point "p" in the descent direction, "h". For a sufficiently small α , $F(p + \alpha h) \cong F(p) + \alpha h^T F'(p)$. If $F(p + \alpha h)$ is a decreasing function of α at $\alpha = 0$, then 'h' is the descent direction. Mathematically, "h" is the descent direction of F(p) if $h^T F'(p) < 0$. If no such "h" exists, then F'(p)=0, showing that in this case the function is stationary. Since the condition for the stationary value of the objective function is that the gradient is zero, i.e. f'(p+h) = L'(h) = 0.

Therefore, the descent direction can be computed from the equation,

$$(J^T J)h_{gn} = -J^T g \tag{13}$$

In each step, Newton method uses $\alpha = 1$, and $p = p + \alpha h_{gn}$. The value of α is found by line search principle described above. Levenberg-Marquardt algorithm is a hybrid method which utilizes both steepest descent principle as well as the Gauss-Newton method. When the current solution is far from the correct one, the algorithm behaves like a steepest descent method: slow, but guaranteed to converge. When the current solution is close to the correct solution, it becomes a Gauss-Newton method. The LM method actually solves a slight variation of Equation (11), known as the augmented normal equations.

$$(J^T J + \mu I) h = -J^T g \tag{14}$$

The term μ is called as the damping parameter, $\mu > 0$ ensures that coefficient matrix is positive definite, and this ensures that h is a descent direction. When the value

of μ is large, we get $h \approx -\frac{1}{\mu}J^T g = -\frac{1}{\mu}F'(p)$ implying a short

step in the steepest descent direction, which is beneficial if the iterate is far from the solution. When the value of μ is very small, then the step size for LM and Gauss-Newton are identical. Algorithm has been modified to take the equations of phase growth and inter-metallic growth under both iso-thermal aging loads to calculate the unknowns.

4.6 Phase Growth Prediction

The following phase growth equation [Callister, 1985, Senkov 1986] has been used to for development of the prior stress history,

$$g^4 - g_0^4 = a(t)^b \tag{15}$$

where b is slope of the equation and a is a constant term. g_0 is the initial grain size, g is the grain size at time t. From the population devices subjected to thermal aging, four condition monitoring devices have been withdrawn and sectioned for four-different isothermal aging durations. The damage proxies have been measured for all the samples. Each following equation represents each interval

$$g_{1}^{4} = g_{0}^{4} + a(t + \Delta t_{1})^{b}$$
(16)

$$g_{2}^{4} = g_{0}^{4} + a(t + \Delta t_{2})^{b}$$
(17)

$$g_{3}^{4} = g_{0}^{4} + a(t + \Delta t_{3})^{b}$$
(18)

$$g_{4}^{4} = g_{0}^{4} + a(t + \Delta t_{4})^{b}$$
(19)

Since the equations being non-linear in nature, a solution using simultaneous equation approach is very difficult to achieve. Therefore, non-linear least square method has been used for obtaining solution. Variable Solutions differ widely in their magnitudes. In order to find the global minima of error, it is necessary to solve the equations for a bounded solution of the variables. Based on accelerated test experimental data, acceptable ranges of solutions for the variables a, b and g_0 was developed (See

Table 8).

 Table 8: Variable Range for Phase-Growth in Thermal Aging (based on Experimental data)

Variables	Trust Region
Constant 'a'	0.0002 - 0.005
Constant 'b'	0.60 - 1.50
Initial Grain size 'g ₀ ' (µm)	0.60- 1.00
Aging Time (hrs)	1 - 150

The equations used in LM algorithm for phase growth are of the form x = f(p)

$$g = \sqrt[4]{g_0 + a(t + \Delta t)^b}$$

Where g is the grain size at different time intervals (Δt), and g₀, a, t and b are the parameters to be found. Since the LM method does a linear approximation to the specified function in the neighborhood of parameter to be found, it does so by using a Taylor series expansion for next approximation. Therefore, it is necessary to give the Jacobian with respect to each unknown.

$$\frac{\partial g}{\partial g_0} = \frac{g_0^3}{\left(g_0^4 + a\left(t + \Delta t\right)^b\right)^{3/4}}$$
(20)

$$\frac{\partial g}{\partial a} = \frac{(t + \Delta t)^{b}}{4\left(g_{0}^{4} + a\left(t + \Delta t\right)^{b}\right)^{3/4}}$$
(21)

$$\frac{\partial g}{\partial t} = \frac{ab(N + \Delta N)^{b}}{4(t + \Delta t) \left(g_{0}^{4} + a(t + \Delta t)^{b}\right)^{3/4}}$$
(22)

$$\frac{\partial g}{\partial b} = \frac{\operatorname{alog}(t + \Delta t)(t + \Delta t)^{b}}{4\left(g_{0}^{4} + a\left(t + \Delta t\right)^{b}\right)^{3/4}}$$
(23)

Variables g_0 , a, t, b, were varied one at a time, while keeping the other three variables constant and were provided as input to the Levenberg-Marquardt algorithm. Schematic illustration of the operation is shown in Figure 71.



Figure 71: Schematic illustration of input to the LM minimization code

The output from the algorithm, g_0 , a, t, b and minimization error was computed for each iteration. Sample row-wise output provided below

0.880941 0.001154379 28.8075 1.13218 0.007383792

The row corresponding to the least minimization error was isolated, and the variables in that row were selected as the final values for g_0 , a, t, b. In order to calculate the damage and remaining useful life under isothermal load the phase-growth data were taken for different packages for four different cycle intervals in the time-neighborhood of prognostication of the electronic package, at various thermal aging times. The measured grain size values were given as input to the Levenberg-Marquardt Algorithm. The solution has been identified as the one with minimum error. Show the plots for minimization error versus aging time.



Figure 72: LM algorithm convergence plot for phase growth under aging load for 196 I/O BGA.



Figure 73: LM algorithm convergence plot for phase growth under aging load for 144 I/O BGA.

In the case of isothermal aging, the values of g_0 , a, b and t have been computed. The computed values of g_0 , a, b and t have been compared with the experimentally measured values for the same package. The error is minimum in the neighborhood of 19 hours, indicating that prior deployed-life, t = 19 hours is the solution for the 196 I/O BGA. The error is minimum in the neighborhood of 30 hours, indicating that prior deployed-life, t = 30 hours is the solution for the 144 I/O BGA. Both the values correlate well with the actual value of 24 hours from experimental data.

Table 9 shows the g₀, t values and their correlation of computed values with experimental values for the various packages including, 144 I/O Tape Array BGA, 196 I/O Plastic BGA. The packages have been prognosticated in the neighborhood of five experimental data-points including, 24, 48, 96, 124, and 240 hours. The computed phase-

sizes and aging-time have been plotted in Figure 25. The experimental data and the model predictions show good correlation.

	Results					
Package	T (hrs)		g ₀ (μm)			
	LM Algorithm	Experiment	LM Algorithm	Experiment		
T144	30.29	24	0.832	0.834		
P196	19.89	24	0.895	0.899		

Table 9: Results comparison with experiments



Figure 74: Graphical comparison of final results (PBGA 196).



Figure 75: Graphical comparison of final results (T144).

4.7 IMC Growth Prediction

In this portion of the study, a second damage proxy, the growth of the intermetallic thickness during thermal aging as leading indicator of failure, has been measured. The following IC growth equation has been used for the development of the prior stress history is as follows:

$$y(t) = y_0 + k(t)^{0.5}$$
 (24)

In order to interrogate the system state using IMC as a damage proxy, three condition monitoring devices have been withdrawn at discrete time intervals, leading to the following equations for the evolution of IMC thickness.

$$y_1(t) = y_0 + k(t + \Delta t_1)^{0.5}$$
 (25)

$$y_{2}(t) = y_{0} + k(t + \Delta t_{2})^{0.5}$$
(26)

$$y_3(t) = y_0 + k(t + \Delta t_3)^{0.5}$$
 (27)

The unknowns in this case are y_0 , k and t. Similar to the methodology used for phase growth (explained above), Levenberg – Marquardt Algorithm was used to get the solution. In order to explore the whole design space, acceptable range for each variable, for each alloy was developed. Table 10 shows the range for each variable for each alloy system.

Table 10: Variable Range for IMC growth for various alloys

Variable	Trust Region
Initial IMC 'y ₀ ' (µm)	3.0 - 5.5
Constant 'k'	0.05 - 0.27
Time 't' (hrs)	1 – 100

Similar to the methodology adopted for phase growth, Jacobian(s) with respect to each unknown were also provided as follows:

$\frac{\partial \mathbf{y}}{\partial \mathbf{y}_0} = 1$	(28)
$\frac{\partial \mathbf{y}}{\partial \mathbf{k}} = \left(\mathbf{t} + \Delta \mathbf{t}\right)^{1/2}$	(29)
$\frac{\partial y}{\partial t} = \frac{1}{2} \frac{k}{\left(t + \Delta t\right)^{1/2}}$	(30)

Initial guess values for variables y_0 , k, t were varied one at a time, while keeping the other three variables constant and were provided as input to the Levenberg-Marquardt algorithm. The output from the algorithm, y_0 , k, t and minimization error was computed for each iteration. The row corresponding to the least minimization error was isolated,

and the variables in that row were selected as the final values for y_0 , k, t. The computed values of y_0 , k and t have been compared with the experimentally measured values for the same package. The error is minimum in the neighborhood of 19 hours, indicating that prior deployed-life, t = 18 hours is the solution for the 196 I/O BGA. The error is minimum in the neighborhood of 22 hours, indicating that prior deployed life, t = 22 hours is the solution for the 84 I/O BGA. Both the values correlate well with the actual value of 24 hours from experimental data.

Table 11 shows the y₀, t values and their comparison with experimental values for the various packages including, 64 I/O Tape Array BGA, 84 I/O Chip Array BGA, 196 I/O Plastic BGA, 280 I/O Flex BGA, and 676 I/O Plastic BGA. The packages have been prognosticated in the neighborhood of five-experimental data points including, 24, 48, 96, 124, and 240 hours. The computed IMC thickness and aging-time have been plotted in Figure 78 to Figure 82. The experimental data and the model predictions show good correlation.



Figure 76: LM algorithm convergence plot - IMC growth under aging for C84 I/O BGA.



Figure 77: LM algorithm convergence plot for IMC growth under aging load for 676 I/O Plastic BGA.

	Results				
	Т ((hrs)	y ₀ ((µm)	
	LM		LM		
Package	Algorithm	Experiment	Algorithm	Experiment	
P676	30.13	24.00	5.499	5.285	
P196	17.97	24.00	3.715	4.141	
C84	22.00	24.00	5.499	4.311	
F280	29.04	24.00	3.388	4.116	
T64	23.87	24.00	3.301	3.231	

Table 11: Algorithm Results comparison with experiments



Figure 78: Graphical comparison of final results (P676).



Figure 79: Graphical comparison of final results (P196).



Figure 80: Graphical comparison of final results (F280).



Figure 81: Graphical comparison of final results (C84).



Figure 82: Graphical comparison of final results (T64).

4.8 Implementation of Damage Pre-Cursors Approach

The prognostics approach presented in here may be implemented using sacrificial devices, which can be cross-sectioned to determine the failure progression of the assembly. It is envisioned that the sacrificial devices will be small, low cost devices, such that several of these can be conveniently located along edge of card assemblies to enable cross-sectioning or on a separate card within an electronic module or card cage.

For example, in the case of solder interconnects, chip resistors may be included on the board assembly and serve as sacrificial devices, which can be periodically crosssectioned. It is not required to assume that all the components mounted on the same board have the same exposure to environmental or operational stresses. However, it is required that the stress variation for the different devices be known and characterized. The sacrificial components are cross-sectioned when the card assemblies, e.g. avionic card assemblies aboard aircraft, need to be redeployed. The baseline phase-size is then measured. The part assemblies to be deployed in the intended use environment will then be subjected to finite-cycles of controlled environmental temperature exposure characteristic of the intended use environment. Another sample of the sacrificial device is then cross-sectioned to enable calculation of the phase growth rate. The residual life can then be calculated based on knowledge of the accumulated initial damage and the phase growth rate in intended use environment. The sacrificial components include the same mechanisms that lead to failure in standard components. Further, given the damage state of a deployed component, the prior-elapsed time in any thermal environment can be computed based on known phase growth rate, given the initial phase size after reflow. The residual life can then be computed based on the computed phase growth rate for the desired use environment.

4.9 Summary and Conclusions

A damage pre cursors based methodology for prognostication-of-electronics including assessment of residual-life, has been developed and demonstrated under single stresses of thermal cycling and steady-state temperature. The damage pre-cursors enable assessment of system damage-state significantly prior to appearance of any macroindicators of damage. Phase growth rate and interfacial intermetallic layers growth rate have been identified as valid proxies for determination of residual life in electronic structures. The theoretical basis for the selection of prognostic parameters has been justified based on particle growth induced by volume diffusion. Mathematical relationships have been developed between phase growth, derivatives of phase growth, intermetallic growth for interrogation of residual life and damage state. A framework for implementation of the prognostication approach has been discussed including, sacrificial devices, which can be examined to determine the damage state of the assembly.

CHAPTER 5

PROGNOSTICS HEALTH MANAGEMENT OF LEAD-FREE Ag BASED SOLDER ELECTRONICS IN HARSH CYCLING ENVIRONMENTS

Requirements for system availability for ultra-high reliability electronic systems such as implantable biological systems are driving the need for advanced heath monitoring techniques for early detection of onset of damage. Traditional health monitoring methodologies have relied on reactive methods of failure detection often providing little on no insight into the remaining useful life of the system. Detection of system-state significantly prior to catastrophic failure can significantly impact the reliability and availability of electronic systems.

Applications for the presented PHM framework include, implantable biological applications such as pacemakers, and implantable cardioverter-defibrillators, consumer applications such as automotive safety systems including front and rear impact protection system, chassis-control systems, x-by-wire systems; and defense applications such as avionics systems, naval electronic warfare systems.

5.1 Introduction

Previously, Lall, et. al. [2004, 2005, 2006, 2007] have developed methodologies for health management and interrogation of system state of electronic systems based on leading indicators. Examples damage pre- cursors include micro-structural evolution, intermetallics, stressgradients. Pre-cursors have been developed for both eutectic 63Sn37Pb and Sn4Ag0.5Cu alloy systems on a variety of area-array architectures.

In this study, a mathematical approach for interrogation of system state under cyclic thermo-mechanical stresses has been developed for 3-different leadfree solder alloy systems. Thermal cycles may be experienced by electronics due to power cycling or environmental cycling. Data has been collected for leading indicators of failure for alloy systems including, Sn3Ag0.5Cu-Bi, Sn3Ag0.5Cu-Bi-Ni, 96.5Sn3.5Ag second-level interconnects under the application of cyclic thermo-mechanical loads. Methodology presented resides in the pre-failure space of the system in which no macro-indicators such as cracks or delamination exist. Systems subjected to thermo-mechanical damage have been interrogated for system state and the computed damage state correlated with known imposed damage. The approach involves the use of condition monitoring devices which can be interrogated for damage proxies at finite time-intervals. Interrogation techniques are based on non-linear least-squares methods. Various techniques including the Levenberg-Marquardt Algorithm have been investigated. The system's residual life is computed based on residual-life computation algorithms.

5.2 Test Vehicle

In the present study, three lead free solder compositions including, Sn0.3Ag0.7Cu-0.1Bi, Sn0.2Ag0.7Cu-0.1Bi0.1Ni, 96.5Sn3.5Ag on identical ball-grid arrays with FR4-06 laminates have been studied under thermo-mechanical loads. Table 12 shows package parameters for the test vehicles used in this study.



Figure 82: Test Vehicle (15 CABGA 100 I/O Packages)

Table	12	:	Pack	age	Details
-------	----	---	------	-----	---------

Body	Solder	Ball	Ball	Die	Die	BT	Ball
Size		Count	Pitch	Thick	Size	Thickness	Diameter
			(mm)	(mm)	(mm)	(mm)	(mm)
10 mm	Sn0.3Ag0.7Cu0.1Bi	100	0.8	0.26	6.4	0.26	0.50
10 mm	Sn0.2Ag0.7Cu0.1Bi0.1Ni	100	0.8	0.26	6.4	0.26	0.50
10 mm	96.5Sn3.5Ag	100	0.8	0.26	6.4	0.26	0.50

Phase growth and IMC data has been gathered and analyzed using image processing. Components analyzed include chip-array ball grid arrays with I/O counts in of 100, and body size of 10 mm. The boards contain six trace layers to simulate the thermal mass of a true production board, though all functional traces were run on the topmost layer. All pads on the board were non-solder mask defined (NSMD) and had an immersion silver finish. All components were assembled to the electroless nickel gold (ENIG) finish printed circuit board and subjected to -55°C to 125°C Cycle, 2.5 hour per cycle. In addition, separate set of board assemblies have been subjected to isothermal

aging at 125°C. All the assemblies were daisy-chained and continuously monitored for failure detection during cycling.

Temperature excursions during operation of a circuit are due to both powercycling and variations in ambient conditions resulting in thermo-mechanical cyclic stresses and strains induced primarily by thermal expansion mismatch between the package and the board assembly. Previous researchers have studied the micro structural evolution of ternary SnAgCu alloys at elevated temperatures using bulk real solder joints with different designs, geometry and process conditions. The SnAgCu microstructure comprises Ag₃Sn and Cu₆Sn₅ dispersed within the tin matrix. The relatively low percentage of alloying elements, 1-4% for Ag and 0.5% for Cu results in phases which comprise a small percentage of the total volume within the solder joint. The microstructural evolution of SnAgCu alloys over time has been found to effect the thermo-mechanical properties and damage behavior [Ye 2000, Allen 2004a, b, Kang 2004, Xiao 2004, Henderson 2004, Kang 2005, Korhonen 2006, Jung 2001].

5.3 Leading Indicators of Failure:

Micro-structural coarsening during thermo-mechanical deformation is attributed to the generation of excess vacancies caused by the combined effect of local hydrostatic state of stress, and the instantaneous inelastic strain rate [Dutta 2003a, 2003b, 2004; Jung 2001]. Evolution of solder microstructure in 63Sn37Pb and lead-free chip resistor solder joints due to thermal fatigue have been studied previously by previous researchers [Sayama, et al. 1999, 2003] and thermal fatigue correlated with occurrence of microstructural coarsening in the fatigue damaged region in of 63Sn37Pb solder interconnects [Frear 1990, Morris 1991]. Correlation of grain coarsening with thermal fatigue has also been established for high-lead solders [Bangs 1978, Wolverton 1987, Tribula 1989]. Previously the authors have investigated the grain-size evolution and derivatives of phase growth rate as prognostics parameters on a wide range of leaded and Sn4Ag0.5Cu devices in underhood applications [Lall 2004^b, 2005, 2006^{a,b}, 2007^{a,b}].

In this paper, prognostics health management methodology has been presented to assess the prior damage is based on solder grain coarsening model. Phase growth under thermal cycling and thermal aging has been identified as the damage precursor to compute the residual life. The relation between phase growth parameter and time for polycrystalline material is given by [Callister 1985]

$$g^n - g_0^n = Kt \tag{31}$$

Where g is the average grain size at time t, g_0 is the average grain size of solder after reflow, K and n (varies from 2 to 5) are time independent constants.

Senkov and Myshlev [1986] applied the theory of phase growth process in a super plastic alloy and validated the theory for Zn/Al eutectic alloy. They expressed the phase growth parameter S as:

$$S = g^4 - g_0^4 = Kt$$
 (32)



Figure 83: Ag₃Sn Grains in 96.5Sn3.0Ag0.5Cu solder microstructure

In this study, changes in solder microstructure and its derivatives have been investigated for use as the leading indicators of failure and interrogation of system state for assessment of damage from prior stress histories. Quantitative metrics of changes in microstructure have been identified and relationships developed to represent damage progression. Data presented covers a wide range of solder alloys including Sn0.3Ag0.7Cu0.1Bi, Sn0.2Ag0.7Cu0.1Bi0.1Ni, 96.5Sn3.5Ag lead-free area-array packaging architectures in extreme temperature cycling and steady-state temperature environments. The phase growth parameter has been defined as the relative change from phase-state after reflow, instead of the absolute value of phase state. Figure 83 shows Ag₃Sn Grains in solder microstructure.

5.4 Interrogation of System State:

In this section, a methodology for determining prior damage by interrogating the damage proxies of test structures has been presented. Two sets of electronic assemblies has been subjected to thermal cycling (-55°C to 125°C). The thermal environments are

intended to simulate a field application environment. The parts are withdrawn from the application environment for redeployment in a new field environment. The damage proxies have been interrogated to determine the extent of damage inflicted and also remaining useful life of that assembly if it is to be re-deployed. Following sections will explain the prediction of stress history using phase growth and IMC growth in thermal cycling and thermal aging environments respectively.

5.5 Levenberg – Marquardt Algorithm

The methodology presented in Section 4.5 of Chapter 4 has been implemented to interrogate the system state. Mathematical basis of method is not repeated here for the sake of brevity.

5.6 Prognostication of Leading-Indicators

Since the equations governing the phase growth and IMC compound are nonlinear in nature, we have used Levenberg-Marquardt Algorithm to interrogate the system state in terms of damage proxies. The LM algorithm has been modified to take the equations for leading indicators of failure (e.g. phase growth and inter-metallic growth) under cycling loads and iso-thermal aging loads. The methodology is as follows:

5.7 Micro-structural Evolution

The following phase growth equation has been used for the development of the prior stress history is as follows:

$$g^4 - g_0^4 = a(N)^b$$
 (33)

From the population devices subjected to thermal cycling, four condition

monitoring devices have been withdrawn and sectioned for four different thermal cycle durations. The phase size has been measured for all samples. Each of the following equations represents an interval of withdrawal, leading to the following equations.

$$g_1^{4} = g_0^{4} + a(N + \Delta N_1)^{b}$$
(34)

$$g_2^{\ 4} = g_0^4 + a(N + \Delta N_2)^b \tag{35}$$

$$g_3^{\ 4} = g_0^4 + a(N + \Delta N_3)^b \tag{36}$$

$$g_4^{\ 4} = g_0^4 + a(N + \Delta N_4)^b \tag{37}$$

In equations (34) - (37), we can see that there are four unknowns g_0 , a, b and t. In order to compute the damage (no. of thermal cycles), it is necessary to solve this set of non-linear equations using a least squares methodology. In the present case, we have used the Levenberg Marquardt Algorithm (LMA) to obtain the solution. Variable solutions differ widely in their magnitudes. In order to find the global minima of the error, it is necessary to solve the equations for a bounded solution space. Based on the accelerated test experimental data, acceptable range for each variable, for each alloy system was developed. The variable range, for each variable was divided uniformly to form numerous initial guess values to be given as input guesses to the LM algorithm. Table 13 shows the range for each variable for each alloy system.

Table 13: Variable Range for phase growth in thermal cycling for various alloys (based on experimental data)

Alloy	Constant	Constant	Initial Grain
System	ʻa'	ʻb'	size 'g ₀ '
Sn0.3Ag0.7Cu0.1Bi	0.0001 - 0.002	1.15 - 1.40	1.40 - 1.60

Sn0.2Ag0.7Cu0.1Bi0.1Ni	0.0001 - 0.002	1.50 - 1.70	1.00 - 1.20
Sn3.5 Ag	0.002 - 0.02	1.00 - 1.20	1.35 – 1.55

The form of equation used in LMA for phase growth is

$$g = \sqrt[4]{g_0 + a(N + \Delta N)^b}$$
 (38)

Since the method does a linear approximation to the specified function in the neighborhood of the parameter to be found using Taylor series expansion for next approximation, it is necessary to give Jacobian with respect to each unknown.

$$\frac{\partial g}{\partial g_{0}} = \frac{g_{0}^{3}}{\left(g_{0}^{4} + a\left(N + \Delta N\right)^{b}\right)^{3/4}}$$
(39)

$$\frac{\partial g}{\partial a} = \frac{\left(N + \Delta N\right)^{b}}{4\left(g_{0}^{4} + a\left(N + \Delta N\right)^{b}\right)^{3/4}}$$
(40)

$$\frac{\partial g}{\partial N} = \frac{ab(N + \Delta N)^{b}}{4(N + \Delta N) \left(g_{0}^{4} + a(N + \Delta N)^{b}\right)^{3/4}}$$
(41)

$$\frac{\partial g}{\partial b} = \frac{a \log(N + \Delta N)(N + \Delta N)}{4 \left(g_0^4 + a \left(N + \Delta N\right)^b\right)^{3/4}}$$
(42)

Initial guess values for variables g_0 , a, N, b, were varied one at a time, while keeping the other three variables constant and were provided as input to the Levenberg-Marquardt algorithm. The output from the algorithm, g_0 , a, N, b and minimization error was computed for each iteration. Sample row-wise output provided below

$0.68026 \quad 0.001154379 \ 228.8075 \ 1.1418 \ 0.006663792$

The row corresponding to the least minimization error was isolated, and the variables in that row were selected as the final values for g_0 , a, N, b. Variables g_0 , a, N, b, were varied one at a time, while keeping the other three variables constant and were

provided as input to the Levenberg-Marquardt algorithm. Schematic illustration of the operation is shown in Figure 84,



Figure 84: Schematic illustration of input to the LM minimization code

5.8 Intermetallic Compound Growth

The following IC growth equation has been used for the development of the prior stress history is as follows:

$$y(t) = y_0 + k(t)^{0.5}$$
(43)

In order to interrogate the system state using IMC as a damage proxy, three condition monitoring devices have been withdrawn at discrete time intervals, leading to the following equations for the evolution of IMC thickness.

$$y_1(t) = y_0 + k(t + \Delta t_1)^{0.5}$$
(44)

$$y_2(t) = y_0 + k(t + \Delta t_2)^{0.5}$$
(45)

$$y_3(t) = y_0 + k(t + \Delta t_3)^{0.5}$$
(46)

The unknowns in this case being $y_{0,}$ k and t. Similar to the methodology used for microstructural coarsening (explained above), LMA was used to get the solution. In order to explore the whole design space, acceptable range for each variable, for each alloy was developed. Table 10 shows the range for each variable for each alloy system.

Table 14: Variable Range for IMC growth for various alloys

Alloy	Initial IMC	Constant	Time
System	'y ₀ ' (μm)	'k'	't' (hrs)
Sn0.3Ag0.7Cu0.1Bi			
Sn0.2Ag0.7Cu0.1Bi0.1Ni	3.66 - 5.41	0.012 - 0.074	200 - 1600
96.5Sn3.5Ag			

The form of equation used in LM for IMC growth is,

$$y(t) = y_0 + k(t + \Delta t)^{1/2}$$
 (47)

The Jacobian with respect to each unknown was also provided as follows:

$$\frac{\partial y}{\partial y_0} = 1 \tag{48}$$

$$\frac{\partial y}{\partial k} = \left(t + \Delta t\right)^{1/2} \tag{49}$$

$$\frac{\partial y}{\partial t} = \frac{1}{2} \frac{k}{\left(t + \Delta t\right)^{1/2}}$$
(50)

Initial guess values for variables y_0 , k, t were varied one at a time, while keeping the other three variables constant and were provided as input to the Levenberg-Marquardt algorithm. The output from the algorithm, y_0 , k, t and minimization error was computed for each iteration. The row corresponding to the least minimization error was isolated, and the variables in that row were selected as the final values for y_0 , k and t.

5.9 Characterization of Damage Progression

Two identical sets of test-samples have been subjected to thermal cycling. In this section, the first data-set has been discussed. The first data-set has been used to characterize the progression of leading indicators of failure with the initiation and progression of thermo-mechanical damage. The average phase growth parameter S, which changes with thermal cycling has been measured from SEM back-scattered images. Figure 85 to Figure 87 show the SEM back-scattered images exhibiting examples of Ag₃Sn phase growth process in the 100 I/O Chip Array BGA at different levels of thermal cycle.

Most of the SnAgCu solder is comprised of Sn-phases, so that the growth rate of tin and Ag₃Sn intermetallic crystals are significant. Since Ag atoms have a higher diffusion rate in the molten solder, they can diffuse out of the way and thus allow the Sn dendrites to grow. Particles of Ag₃Sn grow either to spheres or to needles shape



Figure 85: SEM Back-scattered Images of Phase Growth versus Thermal cycling (-55°C to 125°C, Sn0.3Ag0.7Cu0.1Bi solder, 100 I/O Chip Array BGA, Magnification 750x)


Figure 86: SEM Back-scattered Images of Phase Growth versus Thermal cycling (-55°C to 125°C), Sn0.2Ag0.7Cu 0.1Bi0.1Ni solder, 100 I/O Chip Array BGA, Magnification 750x)



Figure 87: SEM Back-scattered Images of Phase Growth versus Thermal cycling (-55°C to 125°C, 96.5Sn3.5Ag plus solder, 100 I/O Chip Array BGA, Magnification 750x)

The average phase growth parameter S measured under thermal cycling and thermal aging for each individual component has been plotted versus cycles in Figure 88 to Figure 90. The phase growth data in this study indicates that phase growth rate stays fairly uniform during the thermal cycle tests. The phase growth also follows a linear pattern under isothermal aging. Since, and electronic system may have variety of material sets and packaging architectures, the linearity of micro-structural evolution depicts the validity of phase growth as a proxy for damage progression. The damage progression can thus be tracked in various devices based on damage proxies.



Figure 88: Phase Growth parameter, at various levels of cycles for 100 I/O Chip Array BGA, Sn0.3Ag0.7Cu0.1Bi solder interconnects



Figure 89: Phase Growth parameter, at various levels of cycles for 100 I/O Chip Array BGA, Sn0.3Ag0.7Cu0.1Bi0.1Ni solder interconnects



Figure 90: Phase Growth parameter, at various levels of cycles for 100 I/O Chip Array BGA, 96.5Sn3.5Ag solder interconnects

In addition to the phase growth progression, the progression of IMC growth has also been studied. The cycled components have been cross sectioned at various interval of thermal aging. The IMC thickness has been measured in SEM using 1000x magnification using commercial image processing software. An energy dispersive X-ray (EDX) has been used to examine the morphology and the composition of the intermetallic compound layer at the copper/solder interface. Colloidal silica solution has been applied for the detailed intermetallic compound composition observation and detection. Figure 91 to Figure 93 show SEM backscattered images exhibiting examples of IMC growth with aging time for 100 I/O, BGA solder ball for the three-alloys.



Figure 91: SEM Back-scattered images of IMC Growth versus Thermal Aging for Sn0.3Ag0.7Cu0.1Bi (Magnification 1000x)



Figure 92: SEM Back-scattered images of IMC Growth versus Thermal Aging Sn0.3Ag0.7Cu0.1Bi0.1Ni (Magnification 1000x)



Figure 93: SEM Back-scattered images of IMC Growth versus Thermal Aging for Sn3.5Ag (Magnification 1000x)

Trend analysis of intermetallic thickness growth on SEM using image processing software, indicates a square root dependence of IMC thickness versus aging time,

$$y = y_0 + kt^n \tag{51}$$

where y(t) is IMC growth thickness during aging, y_0 is the initial thickness of intermetallic compounds, k is the coefficient standing for the square root of the diffusivity at aging temperature, and t is test time. The exponent value, $n = \frac{1}{2}$ has been used in the above equation, which reveals a diffusion-controlled mechanism during aging. The average IMC growth measured at each level of test time has been plotted versus time. (Figure 94 to Figure 96)



Figure 94: IMC Growth, at various levels of time for CABGA 100 with Sn0.3Ag0.7Cu0.1Bi alloy



Figure 95: IMC Growth, at various levels of time for CABGA 100 Sn0.3Ag0.7Cu0.1Bi0.1Ni alloy



Figure 96: IMC Growth, at various levels of time for CABGA 100 with Sn3.5Ag alloy

5.10 Model Validation: Thermal Cycling

In case of thermal cycling, values of g_0 , a, N, b were computed. For example from Figure 97, we can say that the error is minimum in the neighborhood of 177 cycles, indicating that prior deployed life, N = 177 cycles is the solution for CABGA 100 I/O Package with Sn0.3Ag0.7Cu0.1Bi solder interconnects. This correlates well with the actual value of 250 cycles from experimental data. This method was implemented to interrogate the system state for thermal cycling environments in the vicinity of 250 & 500 cycles respectively. Figure 97 to Figure 102 show the plots of error vs. no. of thermal cycles. Table 15 to



Table 18 show the comparison between values from experiment and algorithm

Figure 97: Plot of Error vs. No. of Thermal cycles (N) for 100 I/O CABGA Sn0.3Ag0.7Cu0.1Bi solder interconnects (Error minimum in the vicinity of 177 cycles)



Figure 98: Plot of Error vs. No. of Thermal cycles (N) for 100 I/O CABGA Sn0.2Ag0.7Cu0.1Bi0.1Ni solder interconnects (Error minimum in the vicinity of 175 cycles)



Figure 99: Plot of Error vs. No. of Thermal cycles (N) for 100 I/O CABGA 96.5Sn3.5Ag solder interconnects (Error minimum in the vicinity of 175 cycles)

Alloy System	Cycles 'N'		Grain Size 'g ₀ '	
			(µm)	
	Expt	LM	Expt	LM
	Data	Algo	Data	Algo
Sn0.3Ag0.7Cu0.1Bi	250	177	1.555	1.60
Sn0.2Ag0.7Cu0.1Bi0.1Ni	250	175	1.113	1.20
96.58n3.5Ag	250	175	1.429	1.50

Table 15: Comparison of computed values of N, g₀, from prognostication model versus experimental result.

Table 16: Comparison of computed values of a and b from Prognostication model versus experimental result.

Alloy System	Constant 'a'		Constant 'b'	
	Expt.	LM	Expt.	LM
	Data	Algo	Data	Algo
Sn0.3Ag0.7Cu0.1Bi	0.00154	0.0009	1.207	1.280
Sn0.2Ag0.7Cu0.1Bi0.1Ni	0.00131	0.0007	1.240	1.330
96.5Sn3.5Ag	0.00081	0.0006	1.328	1.369



Figure 100: Plot of Minimization Error vs. No. of Thermal cycles (N) for 100 I/O CABGA Sn0.3Ag0.7Cu0.1Bi solder interconnects (Error minimum ~ 559 cycles)



Figure 101: Plot of Minimization Error vs. No. of Thermal cycles (N) for 100 I/O CABGA Sn0.2Ag0.7Cu0.1Bi0.1Ni solder interconnects (Error minimum ~ 460 cycles)



Figure 102: Plot of Minimization Error vs. No. of Thermal cycles (N) for 100 I/O CABGA 96.5Sn3.5Ag solder interconnects (Error minimum in the vicinity of 391 cycles)

Table 17: Comparison of computed values of N, g_0 , from prognostication model versus experimental result.

Alloy System	Cycles 'N'		Grain Size 'g ₀ '	
			(µm)	
	Expt	LM	Expt	LM
	Data	Algo	Data	Algo
Sn0.3Ag0.7Cu0.1Bi	500	559	1.555	1.60
Sn0.2Ag0.7Cu0.1Bi0.1Ni	500	460	1.113	1.20
96.5Sn3.5Ag	500	391	1.429	1.50

Alloy System	Constant 'a'		Constant 'b'	
	Expt	LM	Expt	LM
	Data	Algo	Data	Algo
Sn0.3Ag0.7Cu0.1Bi	0.00154	0.0018	1.207	1.1909
Sn0.2Ag0.7Cu0.1Bi0.1Ni	0.00131	0.001	1.240	1.2980
96.5Sn3.5Ag	0.00081	0.00064	1.328	1.3700

Table 18: Comparison of computed values of a and b from Prognostication model versus experimental result.

Based on the values computed from algorithm, it is possible to predict the phase size at different intervals of time. Figure 103 to Figure 105 show the comparison between the predicted versus the experimental values of phase size. The experimental data and model show good correlation.



Figure 103: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. grain size from experimental values Sn0.3Ag0.7Cu0.1Bi alloy



Figure 104: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. grain size from experimental values Sn0.2Ag0.7Cu0.1Bi0.1Ni alloy



Figure 105: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. grain size from experimental values 96.5Sn3.5Ag alloy

5.11 Model Validation: Isothermal Aging

In case of thermal aging, values of y_0 , k, *t* have been computed. For example from Figure 106, we can say that the error is minimum in the neighborhood of 830 hrs cycles, indicating that prior deployed life, N = 830 hrs is the solution for CABGA 100 I/O Package with SAC 105 solder interconnects. This correlates well with the actual value of 667 hrs from experimental data. Figure 106 to Figure 111 show the plots of minimization error vs. aging duration.



Figure 106: Global Minima for IMC based History Calculation for 100 I/O CABGA, Sn0.3Ag0.7Cu0.1Bi Solder Alloy Interconnects (Error minimum in the vicinity of 830 hrs)



Figure 107: Global Minima for IMC based History Calculation for 100 I/O CABGA, Sn0.2Ag0.7Cu0.1Bi0.1Ni Solder Alloy Interconnects (Error minimum in the vicinity of 830 hrs)



Figure 108: Global Minima for IMC based History Calculation for 100 I/O CABGA, Sn3.5Ag Solder Alloy Interconnects. (Error minimum in the vicinity of 914 hrs)



Figure 109: Global Minima for IMC based History Calculation for 100 I/O CABGA, Sn0.3Ag0.7Cu0.1Bi Solder Alloy Interconnects (Error minimum in the vicinity of 1160 hrs).



Figure 110: Global Minima for IMC based History Calculation for 100 I/O CABGA, Sn0.2Ag0.7Cu0.1Bi0.1Ni solder Alloy Interconnects. (Error minimum in the vicinity of 1355 hrs).



Figure 111: Global Minima for IMC based History Calculation for 100 I/O CABGA, Sn3.5Ag Solder Alloy Interconnects (Error minimum in the vicinity of 1150 hrs).

Computed values of y_0 , k, t have been compared with the experimentally measured values for prognostication of 666 hrs (Table 19) and 1334 hrs (Table 20). Table 19: Comparison of computed values of t, y_0 from prognostication model and experimental result.

Alloy System	Aging Time		Grain Size 'y ₀ '	
	't' (hrs)		(µm)	
	Expt	LM	Expt	LM
	Data	Algo	Data	Algo
Sn0.3Ag0.7Cu0.1Bi	667	830	3.93498	3.6610
Sn0.2Ag0.7Cu0.1Bi0.1Ni	667	829.9	3.912	3.912
Sn3.5AG	667	914.9	6.123	6.1

Table 20: Comparison of computed values of t, y_0 from prognostication model and experimental result

Alloy System	Aging Time		Grain Size 'y ₀ '	
	't' (hrs)		(µm)	
	Expt	LM	Expt	LM
	Data	Algo	Data	Algo
Sn0.3Ag0.7Cu0.1Bi	1333	1160	3.93498	3.6610
Sn0.2Ag0.7Cu0.1Bi0.1Ni	1333	1355	3.912	3.912
Sn3.5Ag	1333	1150	6.123	6.10

Based on the values computed from algorithm, it is possible to predict the IMC at different intervals of time. Figure 112 to Figure 114 show the comparison between the predicted versus the experimental values of phase size. The experimental data and model show good correlation.



Figure 112: Prognostication of grain size from algorithm (based on g0, a and b) vs. grain size from experimental values Sn0.3Ag0.7Cu0.1Bi alloy



Figure 113: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. grain size from experimental values Sn0.2Ag0.7Cu0.1Bi0.1Ni alloy



Figure 114: Prognostication of grain size from algorithm (based on g_0 , a and b) vs. grain size from experimental values 96.5Sn3.5Ag alloy

5.12 Implementation Of PHM Technique

The PHM technique presented in the study may be implemented using condition monitoring devices, which can be cross-sectioned to interrogate the system state and determine the failure progression of the assembly. Consider an electronic assembly which has been deployed in the field application. The assembly needs to be redeployed in the same environment.

The condition monitoring devices in the system will then, be withdrawn at periodic intervals in the deployed environment. The condition monitoring devices will be cross-sectioned and their grain size data will be extracted. This data will be analyzed using Levenberg's-Marquardt Algorithm and methodologies discussed earlier, to find out the initial grain size (g₀) and the prior time of deployment (N, or t) for which the component has been deployed. The rate of change of phase growth parameter, (dS/dN), will be computed using the computed values of damage proxies or leading indicators-of-

failure. The rate of change of phase growth parameter (dS/dN) can be correlated to timeto-1%-failure [Lall 2004, 2005, 2006]. Residual Life (RL) can be calculated using the equation, $RL = N_{1\%} - N$.

5.13 Summary and Conclusions

A methodology has been presented to calculate the prior damage in electronics subjected to cyclic and isothermal thermo-mechanical loads. The time duration for which the component has been deployed and initial grain size is been estimated using Levenberg-Marquardt Algorithm with Trust Regions. Methodology has been demonstrated using various leading-indicators of failure including, phase growth and intermetallic thickness. The presented approach uses non-linear least-squares based method of estimating prior stress history, and residual life, by interrogating system-state prior to redeployment. The prior stress histories have been calculated for both cyclic thermo-mechanical loads and isothermal loads. Computed results have been correlated with the experimental data for various aging times and thermal cycles for several packaging architectures. The correlations indicate that the leading indicators based PHM technique can be used to interrogate the system state and thus estimate the Residual-Life of a component. The presented approach of computing residual life can be implemented prior to appearance of any macro-indicators of damage like crack. Methodology presented using condition monitoring components to find out the residual life is promising because these components experience the same environment as actual component.

CHAPTER 6 SUMMARY AND FUTURE WORK

6.1 **D-PACK: Thermo-Mechanical Reliability**

The thermo-mechanical reliability of a new architecture (D-PackTM) has been evaluated using finite element models. Slice models were created for different configurations (Partial Interposer, Full Interposer), solders (eutectic Sn-Pb, SAC) in ANSYS and subjected to two thermal cycles from 0°C to 100°C (20 min dwell / ramps). The reliability was assessed from the point of view of fatigue in solder joints as well as capacitor dielectric cracking.

Volumetrically averaged visco-plastic strain energy density (across a layer of critical elements) was used as a metric to calculate the damage in solder joints due to cyclic temperature loading. Based on empirical relations for life prediction available in literature, cycles to failure was calculated using the energy approach and the predictions were compared with experimental data. The predictions based on finite element methodology have been validated with experimental data.

The maximum principal stress generated in the dielectric was also observed during the simulation. Based on the S-N curves available from fatigue testing for $BaTiO_3$ (dielectric in D-Pack), it was concluded that the stresses generated in D-Pack were well within safety limits to last for more than 10^5 cycles.

On account of relatively small joint height, it was expected that most of the damage would be accommodated by the D-pack joints, which is in line with the finite element predictions, as well as failure analysis of tested assemblies. Based on the examination of hysteresis loop plots (for D-Pack solder joints) from finite element, it can be concluded that partial configuration with SAC solder would perform better than other configurations tested. In order to enhance the thermal reliability it would be worthwhile to explore the effect of increasing the solder joint thickness.

Also, the partial interposer configuration tested during this study was assembled without any joints at the outer periphery. Since it would be reasonable to assume that the intended field application would certainly involve usage of periphery I/Os, it would be interesting to experimentally test assemblies with tall solder joints (for interconnections), and to explore if there is any reliability improvement / degradation over the partial interposer configuration (without any periphery joints).

6.2 **Prognostics and Health Management Implementation**

A damage pre cursors based methodology for prognostication-of-electronics including assessment of residual-life, has been developed and demonstrated under single stresses of thermal cycling and steady-state temperature. The damage pre-cursors enable assessment of system damage-state significantly prior to appearance of any macroindicators of damage. Phase growth rate and interfacial intermetallic layers growth rate have been identified as valid proxies for determination of residual life in electronic structures. The theoretical basis for the selection of prognostic parameters has been justified based on particle growth induced by volume diffusion. Mathematical relationships have been developed between phase growth, derivatives of phase growth, intermetallic growth for interrogation of residual life and damage state. A methodology has been presented to calculate the prior damage in electronics subjected to cyclic and isothermal thermo-mechanical loads.

Components analyzed include various packaging architectures including, plastic ball-grid arrays, chip-array ball-grid arrays, tape-array ball-grid arrays, flex-substrate ball-grid arrays with different pad morphologies, assembled with four different lead-free solder alloys (SAC 405, SnAgCuBi, SnAgCuBiNi, Sn3.5Ag). Packages have been subjected to known levels of thermo-mechanical loads, withdrawn at discrete time intervals and have been cross-sectioned, polished and viewed under a Scanning Electron Microscope. The evolution of damage has been characterized using leading indicators of failure like phase growth and inter-metallic coarsening.

A separate test matrix has been used to interrogate the system state and validate the proposed methodology. The time duration for which the component has been deployed and initial grain size is been estimated using Levenberg-Marquardt Algorithm with trust regions. The presented approach uses non-linear least-squares based method of estimating prior stress history, and residual life, by interrogating system-state prior to redeployment. The prior stress histories have been calculated for both cyclic thermomechanical loads and isothermal loads. Computed results have been correlated with the experimental data for various aging times and thermal cycles for several packaging architectures. A framework for implementation of the prognostication approach has been discussed including, sacrificial devices, which can be examined to determine the damage state of the assembly from time to time. The correlations indicate that the leading indicators based PHM technique can be used to interrogate the system state and thus estimate the Residual-Life of a component. The presented approach of computing residual life can be implemented prior to appearance of any macro-indicators of damage like crack. Methodology presented using condition monitoring components to find out the residual life is promising because these components experience the same environment as actual component.

6.3 Future Work

It is known that high temperature storage of a component prior to field deployment leads to reduction in cyclic life. It would be insightful to conduct an experimental test to quantify the amount of reliability degradation on account of high temperature storage (isothermal aging).

One approach would be to assemble about 15 test boards (each board populated with 15 devices) and to subject them to sequential stress environments (say Treatment I and Treatment II). For example, a test board will be initially subjected to isothermal aging at a given temperature (say 125 °C) and then subjected to thermal cycling (-40°C to 125°C) and failure distribution data be recorded. Table 21 shows a proposed test matrix.

Singh [2006] has developed multivariate regression based models for life prediction of BGA packages. The input data for model building was collected from published literature and accelerated test reliability database based on the harsh environment testing of BGA packages by the researchers at the NSF Center for Advanced Vehicle Electronics (CAVE). The general form of the equation used in this study is

$$N_{1\%} = f \begin{cases} Die size, die to body ratio, ball count, ball diameter, pitch, pcb pad diameter, solder mask definition, pcb finish, encapsulant mold compound filler content and deltaT \end{cases}$$

Test Boards	Treatment I	Treatment II
(Each Board	Aging Time (hrs)	Thermal Cycles
populated with 15 packages)	(@temp)	(-40°C to 125°C)
2 (Two)	No Treatment	Till Failure
2 (Two)	100 hrs (@125 °C)	Till Failure
2 (Two)	200 hrs (@125 °C)	Till Failure
2 (Two)	400 hrs (@125 °C)	Till Failure
2 (Two)	100 hrs (@150 °C)	Till Failure
2 (Two)	200 hrs (@150 °C)	Till Failure
2 (Two)	400 hrs (@150 °C)	Till Failure

Table 21 : Proposed Test Matrix to quantify the effect of Sequential Stresses

Based on the data obtained from the proposed sequential stress experiment, it would be possible to incorporate additional variables (aging temperature and duration) in the multi-variable statistical regression model to compensate for the effects of high temperature storage prior to deployment in a cyclic field environment. The proposed model would be of the form shown below.

$$\mathbf{N}_{1\%} = f \left\{ \begin{array}{l} \text{Die size, die to body ratio, ball count, ball} \\ \text{diameter, pitch, pcb pad diameter, solder mask} \\ \text{definition, pcb finish, encapsulant mold} \\ \text{compound filler content, deltaT, aging} \\ \text{temperature and aging duration} \end{array} \right\}$$

BIBLIOGRAPHY

- Anand, L., "Constitutive Equation for the Rate-dependent Deformation of Metals at Elevated Temperatures," Transactions of ASME, Journal of Engineering Materials and Tech., Vol. 104, No. 1, pp.12-17, 1985.
- Allen, D., "Probabilities Associated with a Built-in-Test System, Focus on False Alarms", Proceedings of AUTOTESTCON, IEEE Systems Readiness Technology Conference, pp. 643-645, September 22-25, 2003.
- Allen, S., L., Notis, Mr., R., Chromik, R., R., Vinci, R., P., "Microstructural Evolution in Lead-free Solder Alloys: Part I. Cast Sn–Ag–Cu eutectic", Journal of Materials Research, Vol. 19, No. 5, pp. 1417–1424, May 2004^a.
- Allen, S., L., Notis, Mr., R., Chromik, R., R., Vinci, R., P., Lewis, D., J., Schaefer, R., "Microstructural Evolution in Lead-free Solder Alloys: Part II. Directionally solidified Sn–Ag–Cu, Sn–Cu, Sn–Ag", Journal of Materials Research, Vol. 19, No. 5, pp. 1425, May 2004^b.
- Al-Qutayri, M.A., Sheperd, R., "Go No-Go Testing of Analogue Macros", IEEE Proceedings-G, Vol. 139, No.4, pp. 534-540, Aug. 1992.
- Anderson, N., and Wilcoxon, R., "Framework for Prognostics of Electronic Systems", Proceedings of International Military and Aerospace Avionics COTS Conference, Seattle, WA, Aug 3-5, 2004.

- ASTM Standard E606-80, "Manual on Low-Cycle fatigue Testing", ASTM Spec. Tech. Publ. 465, Constant Amplitude Low-Cycle Fatigue Testing, 1969.
- Becker, K., C., Byington, C., S., Forbes, N., A., Nickerson, G., W., "Predicting and Preventing Machine Failures", The Industrial Physicist, Vol. 4, Issue 4, pp. 20 – 23, 1998.
- Baldwin, C., J. Kiddy, T. Salter, P. Chen, and J. Niemczuk, "Fiber Optic Structural Health Monitoring System: Rough Sea Trials Testing of the RV Triton," MTS/IEEE Oceans 2002, Volume 3, pp. 1807-1814, October 2002.
- Bangs, E. R., and Beal, R. E., Wel. J. Res. Supp., 54, p. 377, 1978.
- Barke, D., Chiu, W., K., "Structural Health Monitoring in the Railway Industry: A Review", Structural Health Monitoring, Vol. 4, No. 1, pp. 81-93, 2005.
- Bond, L., J., "Predictive Engineering for Aging Infrastructure," SPIE 3588, pp 2-13, 1999.
- Callister, Jr., W., Materials Science and Engineering: An Introduction, Wiley, New York, 1985.
- Chandramouli, R., Pateras, S., "Testing Systems on a Chip", IEEE Spectrum, Vol. 33, No. 11, pp. 42-47, Nov. 1996.
- Chang, P., C., Flatau, A., and Liu, S.,C., "Review Paper: Health Monitoring of Civil Infrastructure", Structural Health Monitoring, Vol.2, No.3, pp. 257-267, 2003.
- Chang, J., Wang, L., Dirk, J., Xie, X., "Finite Element Modeling Predicts the Effect of Voids on Thermal Shock Reliability and Thermal Resistance of Power Devices," Welding Journal, pp. 63s – 70s, March 2006.
- Clech, J., P., "Solder Reliability Solutions: A PC based design-for-reliability tool", 151

Proceedings of Surface Mount International Conference, San Jose, CA, pp. 136-151, Sept. 8-12, 1996.

- Clech., J., P., "Flip-chip / CSP Assembly Reliability and Solder Volume Effects", Proceedings of the Surface Mount International Conference, San Jose, CA, August 25-27, pp. 315-324, 1998.
- Coffin, L., F., "Fatigue in Machines and Structures Power Generation, Fatigue and Microstructure", American Society for Metals, Metals Park, Ohio, pp. 1 27, 1979.
- Coffin, L. F., "A Study of the Effects of Cyclic Thermal Stresses on a Ductile Metal", Transactions of ASME, Vol. 76, pp. 931-950, 1954.
- Humenik, J., N., Oberschmidt, J., M., Wu, L., L., Paull, S., G., "Low Inductance Decoupling Capacitor for the Thermal Conduction Modules of the IBM Enterprise System/9000 Processors", Vol.35, No. 5, pp. 935 – 942, September 1992.
- Dasgupta, A., Oyan, C., Barker, D., Pecht, M., "Solder Creep-Fatigue Analysis by an Energy-Partitioning Approach" ASME Journal of Electronic Packaging, Vol. 114, No. 2, pp 152-160, June 1992.
- Darveaux, R., Banerjee, K., Constitutive Relations for Tin-based Solder Joints", IEEE Transactions on Components, Hybrids, and Manufacturing Technology, Vol. 15, No.6, pp. 1013 – 1024, August 1992.
- Darveaux, R., "How to use Finite Element Analysis to Predict Solder Joint Fatigue Life",Proceedings of the VIII International Congress on Experimental Mechanics,Nashville, Tennessee, June 10-13, pp. 41-42, 1996.

- Darveaux, R., "Solder Joint Fatigue Life Model", Proc. TMS Annual Meeting, Orlando, FL, pp. 213-218, 1997.
- Darveaux, R., "Effect of Simulation Methodology on Solder Joint Crack Growth Correlation", Proceedings of the 50th Electronic Components and Technology Conference, Las Vegas, Nevada, pp.1048-1058, May 21-24, 2000.
- Davidson, E., E., "Electrical Design of a High Speed Computer Package", IBM Journal Research and Development, Vol. 26, No. 3, pp. 349 – 361, 1982.
- DeWolf, J., T. Robert G. Lauzon, Michael P. Culmo, Monitoring Bridge Performance, Structural Health Monitoring, Vol. 1, No. 2, pp. 129-138, 2002.
- Drees, R., and Young, N., "Role of BIT in Support System Maintenance and Availability", IEEE A&E Systems Magazine, pp. 3-7, August 2004.
- Dutta, I., A Constitutive Model for Creep of Lead-Free Solders Undergoing Strain-Enhanced Microstructural Coarsening: A First Report, Journal of Electronic Materials, Vol 32, No. 4, pp. 201-207, 2003a.
- Dutta, I., Park, C., and Choi, S., Creep and Microstructural Evolution in Lead-Free Microelectronic Solder Joints, Proceedings of InterPACK '03, Paper Number IPACK2003-35209, pp.1-6, Maui, HI, July 6-11, 2003b.
- Dutta, I., Impression Creep Testing and Microstructurally Adaptive Creep Modeling of Lead Free Solder Interconnects, TRC, October 25-27, 2004.
- Dyne, S., Collins, P., Tunbridge, D., Satellite Mechanical Health Monitoring, IEEE Colloquium on Advanced Vibration Measurements, Techniques and Instrumentation for the Early Prediction of Failure, London, UK , pp. 4/1- 4/8, May 8, 1992.

Engelmaier, W., "Functional Cycles and Surface Mounting Attachment Reliability",

ISHM Technical Monograph Series, pp. 87-114, 1984.

- Engelmaier, W., "Effects of Power Cycling on Leadless Chip Carrier Mounting Reliability and Technology", presented at Proceedings of International Electronic Packaging, San Diego, California, November 1982.
- Engelmaier, W., "Functional Cycling and Surface Mounting Attachment Reliability",IHSM Tech Monograph Ser. 6984-002, International Society for Hybrid Microelectronics, Silver Spring, Maryland, pp. 87-114, October 1984.
- Fernando,G.,F., Hameed, A.,Winter, D., Tetlow, J. Leng, R. Barnes, G. Mays, and G. Kister ,"Structural Integrity Monitoring of Concrete Structures via Optical Fiber Sensors: Sensor Protection Systems ", Structural Health Monitoring 2003 2: 123-135.
- Frear, D. R., "Microstructural Evolution During Thermomechanical Fatigue of 62Sn-36Pb-2Ag, and 60Sn-40Pb Solder Joints", IEEE Transactions on Components Hybrids and Manufacturing Technology, Vol 13. No 4, pp. 718-726, December 1990.
- Gao, R. X., Suryavanshi, A., "BIT for Intelligent System Design and Condition Monitoring", IEEE Transactions on Instrumentation and Measurement, Vol. 51, Issue: 5, pp. 1061-1067, October 2002.
- Geissinger, J., Harvey, P., M., Kieschke, R., R., "Electronic Package with Integrated Capacitor", US Patent No. 7064412, June 2006.
- Greitzer, F., L., Kangas, L., J., Terrones, K., M., Maynard, M., A., Wilson, B., W., Pawlowski, r., A., Sisk, R., D., Brown, N., B., "Gas Turbine Engine 154

Health Monitoring and Prognostics", International Society of Logistics (SOLE) Symposium, Las Vegas, Nevada, August 30 – September 2, 1999.

- Gupta, P., Doraiswami, R., Tummala, R., "Effect of Intermetallic compounds on reliability of Sn-Ag-Cu flip chip solder interconnects for different Substrate Pad finishes and Ni/Cu UBM", 2004 Electronic Components and Technology Conference, Las Vegas, Nevada, June. 2004.
- Hariharan, G., "Models For Thermo-Mechanical Reliability Trade-Offs for Ball Grid Array and Flip Chip Packages in Extreme Environments", Masters Dissertation, Auburn University, Auburn, AL, May 2007.
- Harmon, G. G., "Metallurgical Failure Modes of Wire Bonds', 12th Annual Proceedings, Reliability Physics, pp. 131-141, 1974.
- Harris, P., G., Chaggar, K., S., "The role of intermetallic compounds in lead-free soldering", Solder Surface Mount Technology, Vol. 10, No. 3, pp. 38-52, 1998.
- Hassan, A., Agarwal, V. K., Nadeau-Dostie, B., Rajski, J., "BIST of PCB Interconnects Using Boundary – Scan Architecture", IEEE Transactions on Computer-Aided Design, Vol. 11, No. 10, pp. 1278-1288, October 1992.
- Henderson, D., W., King, E. K., Korhonen T., M., Korhonen M., A., Lehman L., P., Cotts E., J., Kang, S., K., Lauro, P., Shih, D., Y., Goldsmith, C., Puttlitz, K., J., "The Microstructure of Sn in near eutectic Sn–Ag–Cu alloy Solder Joints and its role in Thermomechanical Fatigue", Journal of Materials Research, Vol. 19, No. 6, pp. 1608–1612, June 2004.
- Hess, A., "The Joint Strike Fighter (JSF) Prognostics and Health Management", JSF Program Office, National Defense Industrial Association, 4th Annual Systems

Engineering Conference, 22-25 October 2001

- Hess, A., "Prognostics, from the need to reality-from the Fleet users and PHM System Designer / Developers Perspectives", Joint Strike Fighter Program Office, Arlington VA, USA, IEEE Aerospace Conference Proceedings, vol. 6, pp. 2791-2797, 2002.
- Ho, C., W., Chance, D., A., Bajorek, C., H., Acosta, R., E., "The Thin-Film Module as a High-Performance Semiconductor Package," IBM Journal Research and Development Vol. 26, No.3, 286-296, 1982.
- Hwang, J. S., "Solder Joint Failure Phenomena", Proceedings of the National Electronic Packaging and Production Conference, NEPCON East '88, pp. 305-322, 1988.
- Jarrell, D., Sisk, D., Bond, L., "Prognostics and Condition Based Maintenance (CBM) A Scientific Crystal Ball", Pacific Northwest National Laboratory, Richland, WA, International Congress on Advanced Nuclear Power Plants (ICAPP), paper #194 June 2002.
- Jung, K., Conrad, H., "Microstructure Coarsening During Static Annealing of 60Sn40Pb Solder Joints: I Stereology", Journal of Electronic Materials, Oct 2001.
- Kang, S., K., Lauro, P., Shih, D., Y., Henderson, D., W., Gosselin, T., Bartelo, J., Cain, S., R., Goldsmith, C., Puttlitz, K., J., Hwang, T., K., "Evaluation of Thermal Fatugue and Failure Mechanisms of Sn-Ag-Cu Solder Joints with Reduced Ag Contents", 2004 Electronic Components and Technology Conference, pp. 661 – 667, 2004.
- Kang, S., K., Lauro, P., Shih, D., Y., Henderson, D., W., Puttlitz, K., J., "Microstructure and Mechanical Properties of Lead-free Solders and Solder Joints used

in Microelectronic Applications", IBM Journal of Research and Development, Vol. 49, No. 4/5, pp. 607 – 619, July / September 2005.

Kay P., J., MacKay, C., A., Trans. Inst. Met. Fin., Vol. 54, p. 68, 1976.

- Kim, J., H., Choi, B., Kim, H., Ryu, W., Yun, Y., H., Ham, S., H., Kim, S., H., Lee, Y.,H., "Separated Role of On-chip and On-PCB Decoupling Capacitors for Reduction of Radiated Emission on Printed Circuit Boards", EMC, 2001.
- Knecht, S., and L. Fox, "Constitutive Relation and Creep-Fatigue Life Model for Eutectic Tin-Lead Solder", IEEE Transactions on Components, Hybrids, and Manufacturing Technology, Vol. 13, No.2, pp. 424 – 433, June 1990.
- Kok, R., Furlong, C., Development and Characterization of MEMS Inertial System for Health Monitoring of Structures, Experimental Techniques, Vol. 29, No. 6, pp 46-53, November-December 2005.
- Kolarik, V., Lubaszewski, M., Courtois, B., "Towards Self- Checking Mixed-Signal Integrated Circuits", Proceedings of European Solid State Circuits Conference, Seville, pp.202-205, 1993.
- Korhonen T., M., Lehman L., P., Korhonen M., A., Henderson, D., W., "Isothermal Fatigue Behavior of the Near-Eutectic Sn–Ag–Cu Allo between -25°C and 125°C ", Journal of Electronic Materials, Vol. 36, No. 2, pp. 173 – 178, 2007.
- Kotlowitz, R. W. and Engelmaier, W., "Impact of Lead Comlpaince on the Solder Attachment Reliability of Leaded Surface Mounted Devices", Proceedings of 1986 International Electronics Packaging Society Conference, San Diego, CA, pp. 841-865, November 17-19, 1986.
- Lala, P. K., "Fault Tolerant and Fault Testable Hardware Design", Prentice Hall, 1985.
- Lau, J. H., Solder Joint Reliability: Theory and Applications, Van Nostrand Reinhold, 1991.
- Lall, P., Pecht, M. and Hakim, E, Influence of Temperature on Microelectronic and System Reliability, CRC Press, Inc., Sep. 1997.
- Lall, P., Islam, N., Suhling, J. and Darveaux, R., "Model for BGA and CSP Reliability in Automotive Underhood Applications", Proceedings of 53rd Electronic Components and Technology Conference, New Orleans, LA, pp.189 –196, May 27-30, 2003.
- Lall, P., Islam, M. N., Singh, N., Suhling, J.C., Darveaux, R., "Model for BGA and CSP Reliability in Automotive Underhood Applications", IEEE Transactions on Components and Packaging Technologies, Vol. 27, No. 3, pp. 585-593, September 2004^a.
- Lall, P., Islam, N., Rahim, K., Suhling, J., Gale, S., "Leading Indicators-of-Failure for Prognosis of Electronic and MEMS Packaging", Proceedings of the 54th IEEE Electronic Components and Technology Conference, Las Vegas, Nevada, pp. 1570-1578, June 1 - 4, 2004^b.
- Lall, P., Singh, N, Suhling, J., Strickland, M. and Blanche, J., "Thermo-mechanical reliability tradeoffs for deployment of area array packages in harsh environments", IEEE Transactions on Components and Packaging Technologies, Vol. 28, Issue 3, pp. 457-466, September 2005.
- Lall, P., Hande, M., Bhat, C., Islam, M., Suhling, J.C., Lee, J., "Feature Extraction and Damage-Precursors for Prognostication of Lead-Free Electronics",

Electronic Components and Technology Conference, San Diego, California, pp. 718-727, 2006^a.

- Lall, P., Islam, N., Rahim, K., Suhling, J. C., "Prognostics and Health management of Electronic Packaging", IEEE Transactions on Components and Packaging Technologies, Vol. 29, No. 3, pp. 666-677, September 2006^b.
- Lall, P., Hande, M., Bhat, C., Islam, M., Suhling, J.C., Lee, J., "Prognostics Health Monitoring (PHM) for Prior-Damage Assessment in Electronics Equipment under Thermo-Mechanical Loads", Electronic Components and Technology Conference, Reno, Nevada, pp. 1097-1111, 2007^a.
- Lall, P., Hande, M., Bhat, C., Islam, M., Suhling, J.C., Lee, J., "Feature Extraction and Damage-Precursors for Prognostication of Lead-Free Electronics", Microelectronics Reliability Journal, Volume 47, pp. 1907–1920, December 2007^b.
- Li, Y., "Accurate Predictions of Flip Chip BGA Warpage", Proceedings of the 53rd Electronic Components and Technology Conference, pp.549 – 553, 2000.
- Lifshitz, I.M., and Slyozov, V. V., Journal of Physical Chemistry Solids, 19, pp-35-50,1961.
- Lourakis, M., I., A., "A brief Description of the Levenberg-Marquardt algorithm implemented by Levmar", Foundation of Research & Technology Hellas (Forth), Greece, pp. 1- 6, Feb 11, 2005.
- Maalej, M., S. F. U. Ahmed, K. S. C. Kuang, P. Paramasivam Fiber Optic Sensing for Monitoring Corrosion-Induced Damage, Structural Health Monitoring, Vol. 3, No. 2, pp.165-176, 2004.

- MacKay S., W., Levine, C., A., "Solder Sealing Semiconductor Packages", IEEE Transactions on Components, Hybrids, and Manufacturing Technology, Vol. CHMT-9, No. 2, pp. 195 – 201, June 1986.
- Madsen, K., Nielsen, H., B., Tingleff, O., "Methods for Non-Linear Least Squares Problems", Technical University of Denmark, Lecture notes, available at http://www.imm.dtu.dk/courses/02611/nllsq.pdf, 2nd Edition, pp. 1-30, 2004.
- Manson, S.S. and Hirschberg, M.H., Fatigue: An Interdisciplinary Approach, Syracuse University Press, Syracuse, NY, pp. 133, 1964.
- Manson, S., S., "Thermal Stress and Low-Cycle Fatigue", McGraw-Hill Book Company, New York, 1960.
- Mallik, D., Radhakrishnan, K., He, J., Chiu, C., Kamgaing, T., Searls, D., Jackson, D., "Advanced Package Technologies for High Performance Systems", Intel Technology Journal, Vol. 09, Issue 04, pp. 259-271, 2005.
- Mezhiba, A., V., Friedman, E., G., "Scaling Trends of On-Chip Power Distribution Noise," IEEE Transactions on Very Large Scale Integration (VLSI) Systems, Vol. 12, Issue 4, pp. 386–394, April 2004.
- Mishra, S., and Pecht, M., "In-situ Sensors for Product Reliability Monitoring", Proceedings of SPIE, Vol. 4755, pp. 10-19, 2002.
- Morris, Jr., J. W., Tribula, D., Summers, T. S. E., and Grivas D., "The role of Microstructure in Thermal Fatigue of Pb/Sn Solder Joints, in Solder Joint Reliability", edited by J. H. Lau, Von Nostrand Reinhold, New York, pp. 225-265, 1991.
- Munns, T. E., R. M. Kent, "Structural Health Monitoring: Degradation 160

Mechanism and System Requirements", Digital Avionics Systems Conferences, pp. 6C2/1-6C2/8, Vol. 2, 2000.

- Nielsen, H., B, "Damping Parameter in Marquardt's Method", Technical Report, IMM-REP-1999-05, Technical University of Denmark, Available at http://www.imm.dtu.dk/~hbn, pp. 1-16, 1999.
- Nimkar, N. D., Bhavnani, S. H. and Jaeger R. C., "Benchmark Heat Transfer Data for Microstructured Surfaces for Immersion-Cooled Microelectronics", IEEE Transactions on Components and Packaging Technologies, Accepted for future publication, Issue 99, 2005.
- Norris, K.C., Landzberg, A.H, "Reliability of Controlled Collapse Interconnections", IBM Journal of Research Development, Vol. 13, pp. 266-271, 1969.
- Pang, H., L., J., Tan, K., H., Shi, X., Q., Wang, Z., P., "Microstructure and intermetallic growth effects on shear and fatigue strength of solder joints subjected to thermal cycling aging", Materials Science and Engineering A, Vol. 307, no. 1-2, pp. 42-50, 2001.
- Pao, Y., H., "A Fracture Mechanics Approach to Thermal Fatigue Life Prediction of Solder Joints", IEEE Transactions on Components, Hybrids, and Manufacturing Technology, Vol. 15, No.4, pp. 559 – 570, August 1992.
- Paris, P., C., Erdogan, F., A., "A Critical Analysis of Crack Propogation Laws", Journal of Basic Engineering, Vol. 85, pp. 528 - 534, 1960.
- Paris, P., C., Gomez, M. P., Anderson, W., P., "A Rational Analytical Theory of Fatigue", The Trend in Engineering, Vol.13, pp. 9 - 14, 1961.
- Prymak, J., D., Randall, M., "Monolithic Multi-layer Capacitor with Improved 161

Lead-out Structure", United States Patent No. 6906907, June 2005.

- Ramakrishnan, A., Syrus, T., and M. Pecht, "Electronic Hardware Reliability, Avionics Handbook", CRC Press, Boca Raton, Florida, pp. 22-1 to 22-21, December 2000.
- Rosenthal, D., and Wadell, B., "Predicting and Eliminating Built-in Test False Alarms", IEEE Transactions on Reliability, Vol. 39, No 4, pp. 500-505, October 1990.
- Sayama, T., Takayanagi, T. and Mori, T., "Analysis of Grain Growth Process in Sn/Pb Eutectic Solder Joint", EEP-Vol. 26-1, Advances in Electronic Packaging-1999, Volume 1, ASME, 1999.
- Sayama, T., Takayanagi, T., Nagai, Y., Mori, T., and Yu, Q., "Evaluation of Microstructural Evolution and Thermal Fatigue Crack Initiation in Sn-Ag-Cu Solder Joints", ASME InterPACK, Paper Number IPACK2003-35096, pp.1-8, 2003.
- Sekhar, A., S., "Identification of a Crack in a Rotor System using a Model-based Wavelet Approach", Structural Health Monitoring, 2003, pp. 293-308.
- Senkov, O. N., and Myshlev, M. M., Acta Metallurgica, 34, pp. 97-106, 1986.
- Shine, M., C., Fox, L., R., "Fatigue of solder joints in surface mount devices," Low Cycle Fatigue-ASTM Spec. Tech. Publ., Vol. 942, pp. 588-610, 1987.
- Singh, N.C., "Thermo-Mechanical Reliability Models for Life Prediction Of Area Array Packages", Masters Dissertation, Auburn University, Auburn, AL, May 2006.
- Smith, R. W., Hirschberg, M., H., Manson, S., S., NASA Technical Not D-1574, NASA, April 1963.
- Smeulers, J., P., M., Zeelen, R., Bos, A., "PROMIS A Generic PHM Methodology Applied to Aircraft Subsystems", IEEE Aerospace Conference Proceedings,

Vol. 6, pp. 3153 – 3159, 2002.

- Subrahmanyan, R., Wilcox, J., R., Li, C., Y., "A Damage Integral Approach to Thermal Fatigue of Solder Joints" Proceedings of Electronic Components Conference, Houston, Texas, pp. 240 – 252, May 1989.
- Solomon, H. D., "Low Cycle Fatigue of Surface Mounted Chip Carrier Printed Wiring Board Joints", Proceedings of 39th Electronic Components & Technology Conference, IEEE, Huston, TX, pp. 277-292, May, 1989.
- Suhling, J., Gale, H., Johnson, W., Islam, N., Shete, T., Lall, P., Bozack, M., and Evans, J., "Thermal Cycling Reliability of Lead Free Solders For Automotive Applications," IEEE International Society Conference on Thermal Phenomena, pp. 350-357, 2004.
- Suhling, J., Gale, H. S., Johnson, W., Islam, M. N., Shete, T., Lall, P., Bozack, M., Evans, J., Seto, P., Gupta, T. and Thompson, R., "Thermal Cycling Reliability of Lead Free Chip Resistor Solder Joints", Soldering and Surface Mount Technology Journal, Vol. 16, No. 2, pp. 77-87, 2004.
- Syed, A., R., "Creep Crack Growth Prediction of Solder Joints During Temperature Cycling – An Engineering Approach", Transactions of the ASME, Vol. 117, pp. 116–122, June 1995.
- Tanimoto, T., Okazaki, K., "Electrical Degradation Process and Mechanical Performance of Piezoelectric Ceramics for Different Poling Conditions", IEEE CH3080-0-7803-0465-9/92, pp. 504 – 507, 1992.
- Tavernelli, J. F., Coffin, Jr., L., F., Transactions of ASME, Vol. 51, pp.438, 1959.

- Tien, J. K., Hendrix, B. C., Bretz, B. L. And Attarwala, A. I., "Creep-Fatigue Interactions in Solders", Proceedings of 39th Electronic Components & Technology Conference, IEEE, Huston, TX, pp. 259-263, May, 1989.
- Tribula, D.G., Grivas, D., Frear, D., and Morris, J., Journal of Electronic Packaging, 111, pp. 83-89, 1989.
- Tu, P., L., C., Lai, J., K., L., "Effect of intermetallic compounds on the thermal fatigue of surface mount solder joints", IEEE Transactions on Components, Hybrids, and Manufacturing Technology, Vol. 20, No. 1, pp, 87-93, 1997.
- Tummala, R. R., Rymaszewski, E. J. and Klopfenstein, A. G., Microelectronics Packaging Handbook Technology Drivers Part 1, Chapman and Hall, New York, 1997.
- Unsworth, D., A., MacKay, C., A., Trans. Inst. Met. Fin., Vol. 51, p.85, 1973.
- Vianco, P., T., Hlava, P., F., Kilgo, A., J. Electron. Mater., Vol. 23, pp. 583, 1994^a.
- Vianco, P., T., Erickson, K., Hopkins, P., J. Electron. Mater., Vol.23, pp. 721, 1994^b.
- Vianco, P., T., Kilgo, A., Grant, R., J. Electron. Mater. Vol. 24, pp. 1493, 1995.
- Vianco, P., T., Rejent, J., J. Electron. Mater. Vol. 28, pp. 1131, 1999.
- Vianco, P., T., Hlava, P., F., Kilgo, Rejent, J., "Environmentally Friendly Electronics-Lead Free Technology, edited by Hwang, J., UK: Electrochem Pub. Ltd, pp. 436 -483,2001.
- Vianco, P., T., Rejent, J., A., Hlava, P., F., "Solid-State Intermetallic Compound Layer Growth Between Copper and 95.5Sn-3.9Ag-0.6Cu Solder", Journal of Electronic Materials, Vol. 33, No. 9, pp. 991 – 1004, May 2004.
- Vichare. N., M., Pecht, М., G., Prognostics and Health Management of 164

Electronics, IEEE Transaction on Components and Packaging Technologies, Vol 29, No.1, March 2006.

- Vishwanadham, P. and Singh, P., Failure Modes and Mechanisms in Electronic Packages, Chapman and Hall, New York, 1998.
- Wilkinson, C., Humphrey, D., Vermeire, B., Houston, J., "Prognostic and Health Management for Avionics", 2004 IEEE Aerospace Conference Proceedings, Vol. 5, pp. 3435 – 3447, March 2004.
- Williams, T. W., Parker, K. P., "Design for Testability-A Survey", Proceedings of the IEEE, January 1983.
- Wolverton, A., Brazing and Soldering, 13, pp. 33, 1987.
- Wong, B., Helling, D., Clark, R., W., "A Creep-Rupture Model for Two-Phase Eutectic Solders", IEEE Transactions of Components, Hybrids, and Manufacturing Technology, Vol. 11, No.3, pp 284 – 290, September 1988.
- Wong, E., Minz, J., R., Lim, S., K., "Decoupling-Capacitor Planning and Sizing for Noise and Leakage Reduction", IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems, Vol. 26, No. 11, November 2007.
- Xiao, Q., Bailer, H., J., Armstrong, W., D., "Aging Effects on Microstructure and Tensile Property of Sn3.9Ag0.6cu Solder Alloy", Transactions of the ASME, Vol. 126, pp. 208 – 212, June 2004.
- Yamada, S., E., "A Fracture Mechanics Approach to Soldered Joint Cracking", IEEE Transactions on Components, Hybrids, and Manufacturing Technology, Vol. 12, No.1, pp. 99 – 104, March 1989.
- Ye, L., Lai, Z., Liu, J., Tholen, A., "Microstructural Coarsening of Lead Free 165

Solder Joints during Thermal Cycling", 2000 Electronic Components and Technology Conference, pp. 134 – 137, 2000.

- Zahn, B, "Solder Joint Fatigue life model methodology for 63Sn37Pb and 95.5Sn4Ag0.5Cu materials," Proceedings of the Electronics Components and Technology Conference. New Orleans, Louisiana, 2003, pp. 83-94.
- Zorian, Y., "A Structured Testability Approach for Multi Chip Boards Based on BIST and Boundary Scan", IEEE Transactions on Components, Packaging, and Manufacturing Technology-Part B, Vol. 17, No. 3, pp. 283-290, August 1994.

-----, Trans. Inst. Met. Fin., Vol. 57, p. 169, 1979.