# Investigation into the Effects of Tool Geometry and Metal Working Fluids on Tool Forces and Tool Surfaces during Orthogonal Tube Turning of Aluminum 6061 Alloy 

by

Prajwal Swamy Sripathi

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Approved by
Lewis N Payton, Chair, Associate Research Professor of Mechanical Engineering
J T Black, Professor Emeritus of Industrial and Systems Engineering Robert L Jackson, Associate Professor of Mechanical Engineering


#### Abstract

Orthogonal Metal Cutting has evolved as a significant way of analyzing the mechanics involved in the art of metal cutting. An orthogonal tube turning apparatus was constructed and validated. The instrument was used to investigate the effects of back rake angle, uncut chip thickness and cutting environments on the tool forces generated during tube turning. Surface roughness was used to parameterize tool surface finish for cutting each factor level combination of the experiment. This work empirically documents the variation of tool forces and tool surface roughness under the influence of various cutting parameters. Force ratios and shear plane angles are calculated using the classical metal cutting equations, analyzing the behavioral patterns and interdependence of cutting forces, tool surface roughness and shear angle.


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$\mathrm{F}_{\mathrm{c}} \quad$ Cutting Force; Force component acting in direction of motion of tool.
$F_{t} \quad$ Thrust Force; Force component acting in direction nomal to shear plane.
F Frictional Force upon Chip
N Normal Force upon Chip
$\mu \quad$ Friction Co efficient
$\mathrm{F}_{\mathrm{s}} \quad$ Shear Force on the Plane
$\mathrm{F}_{\mathrm{n}} \quad$ Normal Force on the Plane
t Uncut Chip Thickness (also referred to as Feed Rate)
$t_{c} \quad$ Cut Chip Thickness
$\mathrm{t} / \mathrm{t}_{\mathrm{c}} \quad$ Chip Thickness Ratio
$\mathrm{A}_{\mathrm{s}} \quad$ Area of the Shear Plane
$\tau_{\mathrm{s}} \quad$ Shear Stress on the Shear Plane
$\alpha \quad$ Rake Angle
$\beta \quad$ Friction Angle
$\varphi \quad$ Shear Plane Angle
$\psi \quad$ Shear Front Angle
V Cutting Velocity
Vc Chip Velocity
Vs Shear Velocity
HPs Specific Horse Power

## CHAPTER 1

## INTRODUCTION

The process of material removal is one of the most extensively used mechanical processes in the industry. The material removal is by a cutting edge in oblique machining processes such as drilling, milling, turning, shaping where in most of these cases the cutting edge is not perpendicular to the cutting motion. In order to simplify the mathematical models, a two force component process called orthogonal machining has been developed and used extensively by metal cutting researchers. M.E.Merchant [1] in 1944 defined the orthogonal tube turning process as characterized by following assumptions,

- The plane of the cutting tool is parallel to the plane of the material being cut.
- The cutting velocity vector and the cutting edge are perpendicular, with the width of the cutting tool more than the width of the work piece.
- The plane of the cutting edge is perpendicular to the direction of motion, generating a plane surface as the work moves beyond the tool with a constant depth of cut.
- The cutting edge is perfectly sharp and has no contact on the clearance face.
- There is relative motion between work and tool with continuous chip formation with no built up edge formation.
- The shear and normal stress along the shear plane and the tool are uniform.

Researchers use orthogonal machining for research purposes since it is easy to model and obtain the required forces. Orthogonal machining is usually performed [2] on

1. Metal plates at low speed
2. Tube turning at moderate speed
3. Plate turning at high speed

Figure 1 shows the motion of the tool and the force system involved in the oblique machining. It can be modified to form a tube turning orthogonal system as in Figure 2 for the ease of understanding, modeling and analyzing the force components.


Figure 1: Oblique Machining [2]
$F_{c}=$ Cutting Force; $F_{t}=$ Thrust Force; $F_{r}=$ Radial Force; $V=$ Velocity of Cut; $\mathrm{t}=$ Uncut Chip Thickness; $\mathrm{t}_{\mathrm{c}}=$ Cut Chip Thickness; $\mathrm{V}_{\mathrm{c}}=$ Cut Chip Velocity.

The process chip formation is influenced by various parameters including workpiece material, cutting tool material, feed rate, cutting speed, tool rake angle, depth
of cut and cutting environment. Extensive research has been carried out in order to understand the effects of these parameters on the cutting forces and tool wear.


Figure 2: Orthogonal Tube Turning (Top View)

Orthogonal tube turning experiments have also been carried out to measure the variables such as chip geometry, chip thickness, cutting forces, cutting temperatures from which one can calculate shear plane angle, strain and strain rate.


Figure 3: Orthogonal Metal Cutting Model

Historically, numerous models have been proposed for the parametric evaluation of the mechanisms of chip formation detailed in Figure. 2 including the force system involved in cutting process, the shear plane angle, $\varphi$ and the tool wear. None of the models successfully explains the variation of tool forces and tool wear mechanism under the influence of different cutting parameters. The following work will address the construction and validation of an orthogonal tube turning set up on a 2 axis HAAS TL 42 lathe at Auburn University in order to explore the effects of cutting parameters like rake angle $\alpha$, feed rate and cutting environment on the tool forces,surface roughness and shear angle.

## CHAPTER 2

## SCOPE AND OBJECTIVES

The main aim of the experiment was to develop a better understanding of the force system involved in the Orthogonal Tube Turning process, which seems to be the least well studied of the orthogonal turning experimental setups. The variation of these forces under different cutting environments and the progressive tool surface roughness were studied to develop an alternative yet efficient cooling system at the tool chip interface where almost all the energy produced by the plastic deformation of the material is converted into heat. The objectives of the experiment included:

1) A comprehensive review of the available orthogonal turning processes to include:
a. Previous force measurements.
b. Previous tool surface measurements.
2) Construct an experimental set up capable of accomplishing following goals:
a. Measure the cutting forces generated during tube turning.
b. Measure the tool surface roughness under different cutting conditions.
c. Calculate the chip thickness ratio and onset of shear plane angle.
d. Validate statistical repeatability and statistical sensitivity of the experiments.
e. Achieve a statistical sampling power of $95 \%$ with 5 replications.
3) Develop a better understanding of the orthogonal tube turning process.
4) Design an experiment using ANOVA with the orthogonal tube turning equipment.
5) Compare resulting data to previous model.

## CHAPTER 3

## LITERATURE REVIEW

## Overview

The principle of orthogonal machining is to observe variations in the metal cutting process for different parameters during the using a 2 dimensional geometry rather than the regular 3 dimensional geometry called oblique machining used in manufacturing environments. Orthogonal machining geometries can be attained utilizing a mill, a shaper or a lathe. In the lathe orthogonal machining can be done on a tube at normal speeds and on a disc at very high speeds with the tool feed in the direction of facing. The tool in both cases is wider than the piece being machined.

The tube to be machined is fastened firmly within the chuck. The tool is mounted on a dynamometer which is used for tube machining to measure the forces involved in the machining. The tool feeds perpendicular to the tube wall to generate a cutting force and a normal (or thrust) force. The tool's direction of motion eliminates the radial force or brings it down to near zero. The tube can be created from a solid through a grooving operation in order to increase the rigidity. This allows the use of a tailstock to support the center of the workpiece. This set-up is commonly done with high tensile strength materials such as steel, sacrificing long duration runs. Figure 3 shows a schematic of orthogonal tube turning on a lathe [2]. The jaws may be insulated to protect the work.


Figure 4: Orthogonal Tube Turning [2]

Dr. M.E. Merchant's [1] classic force diagram for orthogonal machining is depicted in Figure 4. In Figure 4, the cutting force $\mathrm{F}_{\mathrm{c}}$ is the force generated by the motion of the work piece with respect to the tool and thrust force $F_{t}$ is the force generated perpendicular to the point of contact of the tool and work piece. Fc and Ft form the resultant force R . These forces are measured with the dynamometer. The resultant force can be resolved into two components; the shearing force along the onset of shear plane, $\mathrm{F}_{\mathrm{s}}$, and a force normal to the onset of shear plane, $\mathrm{F}_{\mathrm{n}}$. The resultant force can also be resolved into F , the force parallel to the rake face and N , a force normal to the tool face. The onset of shear plane angle is represented as $\varphi$ and the friction angle as $\beta$ [3]. The cutting force and the thrust force are easily captured by the dynamometer setup shown in Figure 3.

Figure 5 summarizes the papers reviewed chronologically within this chapter by broad subject area for the reader. This should facilitate area reviews by future researchers as well. The papers reviewed within this work helped frame and support the objectives of this thesis. A detailed discussion of the many orthogonal machining models is precluded here but available through other sources [3, 22].


Figure 5: Merchant Circle diagram illustrating the Orthogonal Force System


Figure 6: Summary of papers by keywords for this literature review

## Chronological Review of Papers

The forces involved in machining processes are affected by parameters like feed, cutting speed, tool rake angle, depth of cut and cutting environment. An instrument designed to collect Orthogonal Tube Turning data must yield results that are consistent with the published literature observations as the experimentalist varies the cutting parameters (feed, tool rake, etc) and environment (dry, wet, etc).

Lee and Shaffer [4] in 1951 developed a slip line theory in which the chip formation is considered where the forces exerted by the tool are transmitted to the shear plane and in two dimensions; shear plane is the cut along which the tangential velocity is discontinuous. By applying this theory a plastic zone is assumed to exist within the chip bounded by shear plane, tool face and an imaginary boundary across which no stress is transmitted. This state can be represented on a Mohr's circle where the circle passes through the origin and the radius of the circle is equal to the shear strength since it assumes that the shear stress and normal stress are zero along the imaginary boundary. The angle between the slip line and the tool face depends on the friction on the tool face. It is assumed that sticking happens when the friction angle is larger than $45^{\circ}$.

Rowe and Smart [5] in 1963 conducted experiments to show the importance of oxygen in dry machining environment. To examine this, machining was carried out in a vacuum chamber and was compared against oxygen environment. They used an $18^{\circ}$ rake, $6^{\circ}$ clearance high speed steel tool and a depth of cut $0.003 \mathrm{inch} / \mathrm{rev}$ on $0.15 \%$ carbon steel. Experiments revealed that the pure oxygen provides lower cutting forces when compared to a vacuum chamber or a normal atmosphere. It is also explained that a jet of
oxygen directed at the cutting tool edge decreases the cutting force as against the atmospheric air.

Kovacevic, Cherukathota and Mazurkiewicz [6] in 1994 evaluated the effectiveness of high pressure water jet assisted cooling system in terms of cutting force, surface finish and tool wear during milling a stainless steel tubing. Water jets were delivered at high pressure through a nozzle onto a tool chip interface through the tool rake face. The tool forces tend to decrease drastically with the increase in water pressure. A smooth tool chip contact surface was achieved with the help of water jet cooling because of the absence of high shearing forces as compared to flood coolant. The reduction in tool wear was observed due to the reduced tool chip interface resulting from the fragmentation of the chip by the impinging jet.

Klocke and Eisenblatter [7] in 1997 presented the dry machining techniques for cast iron, steel, super alloys and titanium. The work presented a deterministic way of using the cutting parameters to reduce heat generated at the tool chip interface by reducing the friction. The control of chip formation was found to be of prime importance as it has significant effects on machining temperature.

Huang and Chen [8] in 1999 found that the temperature and force involved in machining increased with the increase in depth of cut and contact length of the tool/chip interface. They also found that the change in force due to the change in contact length of the tool chip interface is accompanied by the change in shear angle to match the change in resultant force. It is further explained that the shear angle becomes small as the deformation of the chip reduces thus reducing the cutting forces.

Sreejith and Ngoi [9] in 1999 presented the significance of dry machining in the near future and the cutting tool requirements for the same. It is stated that the cutting fluids has been greatly reduced due to the increase in use of mist coolant lubrication which is found to cause serious respiratory effects on the operator. This study insists on the use of cemented carbide, ultra-hard tool materials such as diamond and cubic boron nitride which produces better machined surfaces with remarkable increase in tool life due to the extremely high "hot" hardness of the tool materials.

Marghitu, Bogdan and Nicolae [10] in 2000 proposed a non-linear dynamics approach for the analysis of cutting and thrust force data obtained during orthogonal turning processes. They conducted turning operations on various materials like aluminum, ductile cast iron and grey cast iron. After applying several non-linear dynamic tools to determine the type of time evolution in terms of periodicity or nonperiodicity of the forces, it was concluded that the orthogonal turning of aluminum work pieces is more stable than ductile cast iron and grey cast iron and produces a stable force response.

Grzesik [11] in 2000 investigated the influence of thin hard coatings on frictional behavior during the orthogonal turning process. During the experiment he was able to observe a visual difference at the tool chip contact area for different friction forces and was more pronounced in $\mathrm{TiC} / \mathrm{TiN}$ coatings. The reduction in the friction forces suggested that the energy required in overcoming friction and shearing is less, where as the tangential force decreased intensively with increase in cutting speed. The reduction of friction force is probably due to an intensive thermal softening in the shearing zone. The reduction of contact area at higher speeds can intensify the thermal softening of the
material. Two mechanisms that influence he contact stress were clarified in this research. One is reduction of the contact area and the other is intense thermal softening of the work at the interface. He also concluded that the interplay between mechanical stress at rake and thermal energy between the chip and tool is a key factor influencing the surface temperature of the tool.

Vieira, Machado and Ezugwu [12] in 2001 studied the cooling ability of different cutting fluids in comparison with dry machining. During the machining of AISI 8640 steel bars using carbide inserts an increase in the tool life was achieved under dry machining conditions as compared to other synthetic coolant environments. This was explained by the fact that dry machining generated higher cutting temperature leading to decrease in shear strength of the work material thus reducing the power consumption and eventually causing a reduction in tool wear. However their recorded surface roughness values under various cutting environments showed a random behavior with time.

Paul and Chattopadhyay [13] in 2001 investigated the beneficial effects of cryogenic cooling over dry and wet machining. They used liquid nitrogen jets on the tool wear surface and they found the forces involved in machining were less and the surface finish was better as against dry machining.

Diniz and Micaroni [14] in 2002 conducted experiments to remove the use of cutting fluid from a finish turning process without harming the tool life by increasing the feed and tool nose radius and decreasing the cutting speed. In turning a 1045 steel using carbide inserts under large feeds, tool life for dry cutting gets closer to that of wet turning where in synthetic oil with $6 \%$ concentration in water was used. With the increase in feed, heat generated at the tool chip interface increased, but the surface area on the tool to
dissipate this heat also increased. This also resulted in decrease in specific cutting force. It is further concluded that with the increase in tool nose radius, the surface area dissipating the heat increases making the cooling of cutting zone not so necessary.

Cakir et al [15] in 2004 investigated the effects of cutting fluids to provide quantitative results about the cutting force, thrust force and the surface roughness. A 5\% emulsion type cutting fluid was used as liquid coolant and compressed oxygen, nitrogen and carbon dioxide gas stored in cylinders at their normal temperatures were used. They used tubes ending with nozzles and fitted with suitable pressure regulators to direct the gases and the coolant at the cutting edge of the tool. The response curve of the mean cutting force and the thrust force showed that all gaseous and flood coolant is different from the dry cutting and also increases with increase in feed. Later Cakir analyzed the response of the shear plane angle under varying depth of cut. This showed an appreciable increase in the shear angle in the gaseous and flood coolant environment leading to smaller shear area and reduced cutting forces as compared to dry cutting environment. Although the effect of feed was obvious on the surface roughness of the machined parts the investigation concluded that the dry machining produced the highest value of roughness then wet machining.

Saoubi and Chandrashekaran [16] in 2004 investigated the effect of tool microgeometry and temperature on coated tools. During their investigation they found that machining parameters chosen has an effect on temperature. An increase in cutting speed or feed resulted in the increase in the temperature. It was noted that the maximum temperature moved closer to the tip of the tool as cutting speed increased and away as the feed increased. The material hardness as well had an effect on the temperature. This may
be explained by the fact that harder the materials, smaller will be the plastic deformation zone and the size of tool chip contact length.

Saglam, Yaldiz and Unsacar [17] in 2005 investigated the effect of tool geometry on the cutting forces and tool temperature. During machining large amount of energy is converted into heat energy considerably on the shear plane, rake face and clearance face. In orthogonal machining, the cutting is assumed to be uniform along the cutting edge; hence it is a two dimensional plane strain deformation. The cutting forces are exerted only in the direction of velocity and uncut chip. Rake angle determines the tool/chip contact area. They found that with the increase in the rake angle from $0^{\circ}$ up to $20^{\circ}$ has a positive effect on the tool by increasing the shear plane angle causing the reduction in the force system. But increasing beyond a point affects the tool's performance and accelerates tool wear. Smaller positive rake angles leaves a better finish but excessive positive angle weakens the tool causing tool breakage. The optimal rake angle was obtained as $12^{\circ}$.

Kalyankumar and Choudhury [18] in 2007 investigated the effects of cryogenic cooling on tool wear and high frequency dynamic cutting forces generated during high speed machining of stainless steel. They observed from their experiments that the cutting force decreased with increase in cutting speed since the co-efficient of friction at the tool chip interface decreases and the shear plane angle increases, decreasing the area of shearing. They also found that the increase in feed and depth of cut increased the cutting force. Due to the increase in depth of cut and feed, the material removal rate also increases eventually the rate of plastic deformation and hence the cutting force increases. With the increase in cutting speed, higher cutting temperature and shortened contact area
were observed. As a result the temperature concentration moved towards the tip of the tool resulting in the reduction of tool strength and increased tool wear. They concluded that the cutting force and tool wear was considerably less using the cryogenic environment compared to a dry environment as well as tool wear.

Pujana, Azarolla and Villar [19] in 2008 developed an in-process high speed photography for orthogonal turning to measure strain and strain rates. The work piece was micro-scale grid printed by the process of photochemical milling. They calculated the strain and strain rate manually based on the grid pattern. It was observed that the strain decreased with an increase in cutting speed and shear angle. They also noted that the chip topology for the working conditions they chose were not uniform. The chip formation of 42 CrMo 4 they observed was defined as a random process between serrated, transitional and continuous chip.

Stanford, Lister and Kibble [20] in 2008 studied the effects of cutting forces and tool wear under different cutting conditions. The behavior of the responses were derived by using a 4\% dilution semi synthetic flood coolant, compressed air (20\% oxygen at 0.27 MPa ), Nitrogen gas ( $6 \%$ oxygen at 0.27 MPa ) and liquid nitrogen and eventually compared against dry cutting. Plain carbon steel with UTS of 217 MPa was machined on a CNC turning center with a constant depth of cut of 1.2 mm and a feed rate of $0.1 \mathrm{inch} /$ rev under different cutting environments. Results show that the cutting force and the thrust force decreases with the use of flood coolant and liquid nitrogen as compared to the other gaseous environments and dry machining. Also the use of flood coolants showed a significant increase in the shear plane angle as compared to dry and gaseous environment cutting. It was observed that compressed air and nitrogen environment
produced significantly thicker chips which can be confirmed by smaller shear angle and longer shear plane. Stanford et al further discusses the behavior of the crater wear and flank wear and concludes that although all the environments show significant wear, the dry cutting environment produces the highest level of wear. According to their experiments the best performing environment with considerably less wear is produced when flood coolant is used and lowest density of work piece adherence at the crater face and the flank edge is achieved. It is also explained that the use of nitrogen environment would assist in the reduction of notch wear reducing oxidation and providing better finish of the machined component.

One of the early advantages which drove metal cutting research was an interest in the power required by a machine to remove a certain "swept volume". Using the classic Merchant force diagram for example, total energy per unit time can be calculated by the product of primary cutting force, $\mathrm{F}_{\mathrm{c}}$, and the velocity of the cut, V . Due to the fact that many parameters can be varied during the cutting process that affects the total energy consumed, this energy is normalized by dividing it by the rate at which the material is removed. The material removal rate for a tube is the product of area being cut and the velocity perpendicular to the area at which the material is removed. Considering the thickness of uncut chip, $t$ and the width of the tube wall, the energy per unit time or specific energy, $u$, is calculated by,

$$
u=\frac{F_{c} \cdot V}{t \cdot w \cdot V}=\frac{F_{c}}{t \cdot w}
$$

Specific energy can be partitioned into 4 components (a) Shear energy per unit volume, (b) Friction energy per unit volume, (c) Kinetic energy per unit volume and (d) Surface energy per unit volume. Specific energies can be used to calculate the power/volume/time
(specific horsepower) and are available for most engineering material. They are a measure of the difficulty involved in machining a particular material and are sometimes used to model a given material's machinability.

## Summary

The parametric effects upon measured results discussed within this literature review are summarized in Table 1. Any newly constructed instrument must yield results consistent with these historical results.

| Parameter | Change | Cutting Force | Thrust Force | Chip Thickness | Wear | Shear Angle |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Feed, t | Increase | Increase | Increase | Increase | Increase | Increase |
| Rake Angle <br> $(0-20)$ | Increase | Decrease | Decrease | Decrease | Decrease | Increase |
| Negative Rake <br> Angle (<0) | Increase | Increase | Increase | Increase | Increase | Decrease |
| Cutting Speed, v | Increase | Decrease | Decrease | Decrease | Increase | Decrease |
| Width of Cut, w | Increase | Increase | Increase | Increase | Increase | Decrease |
| Compressed Air | On | Increase | Increase | Increase | Decrease | Increase |
| Metal Working <br> Fluid | On | Decrease | Decrease | Decrease | Decrease | Increase |
| Contact Length | Increase | Increase | Increase | Increase | Increase | Increase |

Table 1: Summary of Variation of Response with Input Parameters.

## CHAPTER 4

## DESCRIPTION OF EQUIPMENT

This chapter documents the materials, equipment and software used to conduct the experimental research. Below is the list of the machine tools and instruments used to construct an orthogonal tube turning setup, the materials used in the experiments and further to carryout the data analysis.

- HAAS Two Axis Lathe (Model TL-2)
- KISTLER Three Component Dynamometer (Type 9257A)
- KISTLER Charge Amplifier (Model 5004)
- NATIONAL INSTRUMENTS DAQ device (NI USB-6008, with Digital I/O channels and a 32-bit counter)
- LABVIEW 8.2 Data Acquisition Software
- HSS Stick Tools ( $3 / 4 " \times 3 / 4 " \times 5$ "), ground to appropriate angles
- Aluminum 6061 Alloy Tubing (3" OD with wall thickness $1 / 8$ ")
- Nitrogen Cylinder supplied by Air Gas with Pressure Regulator
- VORTEC Cold Air Gun
- Commercial Spray Coolant Generator
- TaiCaan XYRIS series Surface Profiler with a LT-8010 Sensor head, LT-V201 Camera Unit and a LT-8105 Controller unit
- HARIG 618 AUTOMATIC Surface Grinder


Figure 7: HAAS Two Axis Lathe
The final experimental setup consists of a HAAS two axis lathe with a conventional tool post being replaced by a custom tool post to hold the HSS tool in a way that the force in the radial direction is reduced to zero. A three component KISTLER dynamometer is mounted on a steel plate which in turn is mounted onto the lathe bed in position of the conventional tool post. A custom made Aluminum tool post is fastened onto the Dynamometer so that the complete load on the tool holder will be transmitted to the dynamometer. An aluminum 6061 alloy tube is held firmly in the chuck for machining.

## Control Validation of the Two Axis HAAS Lathe

The HAAS (Model TL-2) lathe features an option where the spindle rotations are input in revolutions per minute and feed is input in inches per revolution. Validation of feed in a lathe is of prime importance yet difficult with feed being in inches per revolution; hence to make it easier, the spindle speed was multiplied with feed to convert feed in terms of inches per minute.

A feed rate of 0.001 inches per revolution was chosen with a rpm of 100 . The feed in terms of inches per minute is $0.1 \mathrm{inch} /$ minute. To validate the X -Axis, the lathe was run and the time taken for the tool post to travel 0.1 inches were recorded with the help of a stop watch. The lathe took 60,60 and 61 seconds on the first, second and third trial respectively. For Z-Axis, same steps were followed and the time taken for carriage to move 0.1 inches were recorded. The lathe took 62,60 and 61 seconds respectively. Considering the fact that the stopwatch is being operated by a human, human error has to be taken into account during switching on and off the stopwatch and hence conclude that the lathe is validated for the expected feed rate. The lathe has an inbuilt feature to adjust the RPM according to the work piece radius in order to maintain the specified SFM.


Figure 8: KISTLER 9257A 3 Component Dynamometer
A calibrated 3 axis dynamometer collected the force data exterted on the tool in cutting, normal and radial directions.


Figure 9: KISTLER Charge Amplifiers (Model 5004)
Dual mode charge amplifiers were used to amplify the piezo electic output of the dynamometer.


Figure 10: National Instruments USB 6008
The output signal from the amplifiers is converted to digital voltage signals using a NI USB 6008 module and LabVIEW 8.2 software.


Figure 11: Vortec Cold Air Gun
A cold air gun usually used for spot cooling when machining plastics is used to achieve cold compressed air environment in this experiment.


Figure 12: Kool Mist Spray Coolant Generator
A spray coolant generator capable of producing a mist environment with the mixture of compressed air and water soluble synthetic coolant is used. Manufacturers recommended settings were used through out.


Figure 13: TaiCaan XYRIS Series Surface Profiler with a LT-8010 Sensor head, LT-
V201 Camera Unit and a LT-8105 Controller unit.
Unit was graciously loaded to Auburn University by XYRIS4000CL Taicaan and John McBride at the University of Southampton. This Confocal Laser Profilometer was used for measuring the surface roughness of the tool


Figure 14: Overall Network Schematic of the Experimental Set up

The forces exerted on the tool are effectively delivered to the dynamometer which sends the piezo-electric signals to the charge amplifiers. The charge amplifiers amplify the signals and are traferred to a digital input/output DAQ system. The DAQ system converts the voltage signals to the force signals with the aid of labview computer software which displays the variation of forces with time.

## CHAPTER 5 <br> CONSTRUCTION OF THE ORTHOGONAL TUBE TURNING APPARATUS

The Auburn University instrument was designed with an objective to study the response of the tool force system, tool surface roughness and the shear angle behavior under the influence of various cutting parameters and environments during the orthogonal tube turning process on a HAAS two axis CNC lathe modified to carry out orthogonal tube turning. The basic geometry of the tube turning is as shown in Figure 19.


Figure 15: Geometry of Orthogonal Tube Turning

The KISTLER 3 component dynamometer is mounted on a steel plate and in turn is bolted down onto the lathe in the position of the tool post. A custom made tool holder machined using an aluminum alloy with a slot exactly sufficient to seat a $3 / 4$ inch tool is mounted onto the dynamometer in way that the total base area of the tool post is seated completely on the dynamometer surface to achieve total load transfer from the tool to the dynamometer. The tool holder consists of top and bottom blocks with bolts to clamp down the tool. The bottom block is bolted down to the dynamometer where as the top block is adjustable using four $21 / 2$ inch long, $1 / 4-20$ bolts at each edge to facilitate the tool change as shown in Figure 21.


Figure 16: Dynamometer and Tool Holder Mounting Assembly


Front View


Figure 17: Top block of the Tool Holder.


Figure 18: Bottom block of the Tool Holder.
The $\mathrm{x}, \mathrm{y}$ and z output from the dynamometer which is in the form of an electric charge were connected to KISTLER 5004 charge amplifiers for signal amplification. The sensitivity and the linearity of the charge amplifiers are adjusted according to the manufacturer's calibration certificate (Appendix A). The amplifiers convert the electric charge from the piezoelectric transducer into a higher voltage, more sensible output. The
output voltages from the charge amplifiers are then connected to the National Instruments (NI) USB - 6008 which has 12 digital input/output (DIO) channels and a 32-bit counters with a full speed USB interface.


Figure 19: Charge Amplifiers and USB DAQ system module connected to the
LABVIEW 8.2 system software

The software interface for NI USB - 6008 is LABVIEW which reads out the force signals. The outputs of the Kistler Amplifiers are converted into cutting and normal force data by the software. The block diagram of the Lab View program used to convert the electrical signals to the force data is shown in Figure 24.


Figure 20: Block Diagram of the program in LABVIEW 8.2 Software
The DAQ assistant receives the signals from the amplifiers which are sent to the filtering block. These filtered signals are recorded in a measurement file and a waveform chart is displayed.


Figure 21: Dry Machining

## Enviromental Controls

As mentioned in the literature review, it is desirable for a number of reasons to study the environmental effects upon the cutting process. Four different environments have been prepared initially for experiments at Auburn University using dry (or hard) turning with no applied gases or coolants, cold compressed air, gaseous nitrogen and commercially available water based spray coolants.

The dry machining is done at the atmospheric temperature without the aid of any apparatus to dissipate the heat generated at the tool chip interface. The tool mounted on the tool holder plunges into the material in the direction of the axis of the spindle rotation. A canned cycle for constant feed was used and the total material to be cut was calculated so that the tool cuts exactly for 60 seconds under all different feeds. This is the basic setup described by Figures (19) and (25).


Figure 22: Turning at Cold Compressed Air Environment with Vortex Air Gun
To achieve a cold compressed air environment a Vortex air gun with a nozzle is used to direct the cold air generated by the air gun to the tool chip interface. The Vortex air gun is designed to keep plastics cold and hard during machining so that they do not melt into the harder, hot tool. The inlet of the air gun is connected to a compressed air main bus through a pressure regulator. The compressed air enters the cylindrical generator which is proportionately larger than the hot tube where it causes the air to rotate. This rotating air is forced down on the inner walls of the hot tube at speeds reaching $1,000,000 \mathrm{rpm}$. At the end of the hot tube, a small portion of this air exits through a needle valve as hot air exhaust. The remaining air is forced back through the center of the incoming air stream at a slower speed. The heat in the slow moving air is transferred to the fast moving incoming air. This super cooled air flows through the center of the generator and exits through the cold air exhaust port. The nozzle connected to the exhaust port directs the cold air over the cutting zone. The pressure of the compressed air before it enters the cold air gun is maintained at 75 psi . Temperatures down to -70 degrees Fahreinheit are routinely achieved at the outlet to the nozzle.


Figure 23: Turning at Nitrogen Gas Environment

A Nitrogen cylinder with a suitable pressure regulator was used to generate a continuous directed flow of nitrogen gas at high pressure over the cutting zone at the tool chip interface. The outlet from the pressure regulator was connected to a suitable nozzle and clamped to a magnetic stand which can be seated on the lathe bed conveniently to adjust the direction of the gas flow. The pressure at the regulator was maintained at 75 psi and the outlet nozzle used for the nitrogen is same as the one used to direct cold compressed air at the cutting zone.


Figure 24: Turning at Spray Coolant Environment

A commericially available, popular cool mist environment was obtained using a spray coolant generator which basically consists of a steel tank with a siphon line immersed in the tank. The outlet of the siphon is connected to the valve fitted with an inlet and an outlet port. The inlet line is connected to the compressed air line fitted with a suitable pressure regulator maintained at 75 psi . The tank is filled with 1:40 ratio commericially available synthetic coolant and water. The compressed air entering the valve creates the suction in the siphon and a mist of spray coolant and compressed air is sprayed over the cutting zone. The coolant tank as supplied by the manufacturer has two outlet ports for the spray coolant and both the outlets are connected to separate nozzle and directed at the tool chip interface from either sides as shown in Figure 29. These are the manufacturer's recommended "ideal" settings. All components in the system were "new" out of the box and undamaged.

The continuous chips obtained during all different runs under various environments and various cutting parameters are collected and stored for analysis purposes as will be described later.

## Tool Surface Roughness Measurements:

The average surface roughness of a tool face can be mapped using a confocal laser profilometer. A tool to be scanned was placed under the scanner so that the laser beam is projected above the surface of the tool and travels 3 mm in the x -direction so as to just stop at the edge of the tool and jump to the next line for scanning. Adjusting the area of the surface to be profiled is aided by a camera to position and preview the area to be scanned. The tool path of the laser over the profiled surface is as shown in figure 26.


Figure 25: Area being scanned on top face of a $3 / 4 \times 3 / 4 \times 5$ inch tool


Figure 26: Laser Beam Path

The TAICAAN software used was programmed to scan 101 points in x direction ( 3 mm ) and 101 points in y direction $(3 \mathrm{~mm}$ ) resulting in 10201 data points for each tool profiled. The number of points to be scanned can be varied depending upon the accuracy of the roughness value needed. The resolution of the instrument is evaluated as $0.1 \mu \mathrm{~m}$ according to manufacturer specifications.

The readout represents the height of the surface being profiled (in mm ) from the tip of the laser probe. This profile data was used to calculate the root mean square deviation of the profile from the mean line. Suppose $z_{1}, z_{2}, z_{3} \ldots z_{n}$ represents the height variation of the surface from the laser tip, Root mean square deviation is defined as,

$$
R_{q}=\sqrt{\frac{\mathrm{z}_{1}^{2}+\mathrm{z}_{2}^{2}+\mathrm{z}_{3}^{2} \cdots \cdots \cdots \cdots \mathrm{z}_{n}^{2}}{n}}
$$

The ' $\mathrm{R}_{\mathrm{q}}$ ' value calculated as above is a direct measure of the surface roughness. The same tool after being used for 300 seconds on a tube turning setup was used to map the profile again. The used tool is placed below the laser beam. With the aid of the camera unit, the position of the tool is adjusted to scan the same $3 \mathrm{~mm} \times 3 \mathrm{~mm}$ area scanned for the unused tool. This was achieved through carefully positioning the tool by observing the light spot at the edge of the tool as shown in figure below. Before scanning the tool, the laser path is previewed using the camera multiple times to make sure the laser beam travel path is not crossing the edge of the tool and is over the light spot where tool wear is expected to be remarkable.


Figure 27: Enlarged camera view of the cutting edge.

This way the tool is profiled and subsequently the root mean square deviation is calculated. After obtaining the average surface roughness for new tool $\left(\left(\mathrm{R}_{\mathrm{q}}\right)_{\text {new }}\right)$ and for the used tool $\left(\left(\mathrm{R}_{\mathrm{q}}\right)\right.$ used $)$ the effective surface roughness of the tool face is calculated as the difference in the surface roughness values of used and new tool.

$$
\Delta R_{q}=\left(R_{q}\right)_{\text {new }}-\left(R_{q}\right)_{\text {used }}
$$

## CHAPTER 6

## INSTRUMENT VALIDATION AND SAMPLE SIZE DETERMINATION

Having constructed the Orthogonal Tube Turning (OTT) instrument, it is necessary to validate the instrument for repeatability, sensitivity and standard deviation in order to design and determine the statistical power of the response data. The instrument repeatability requires one set of tests to establish that for a given set of conditions, the same result is returned. A second series of tests to validate that the instrument is capable of measuring an actual change is then required in order to prove the instrument is not always returning the same (potentially false) result. Finally, in order to determine the confidence one can place in the results at a given factor level combination of experimentation, one must establish the standard deviation of the instrument.

## Repeatability Test

For the purpose of instrument repeatability, three data sets were considered each with five runs carried out on different days over a period of time at dry environment with a $0^{\circ}$ rake angle tool and a constant feed of 0.001 inch. The standard spindle rpm was used and the force data was saved in a MS Excel file for analysis. The dynamometer records a response reading for every 0.01 seconds, so for 60 seconds of cut a total of 6000 readings are recorded. The initial 10 seconds are disregarded during which the tool is deflected during the onset of the force occurs and response curve stabilizes. Table 3 and Table 4
shows the average and the standard deviation values of the thrust force and the cutting force data under each run.

| Thrust Force Data |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Run <br> No. | Data Set 1 |  | Data Set 2 |  | Data Set 3 |  |
|  | Mean | Std <br> Deviation | Mean | Std <br> Deviation | Mean | Std <br> Deviation |
| Run 1 | 178.7172 | 6.6239 | 185.3432 | 3.1193 | 175.1395 | 3.5045 |
| Run 2 | 175.5777 | 7.9548 | 177.0952 | 7.7615 | 17.6127 | 3.3581 |
| Run 3 | 175.7445 | 6.5045 | 178.2868 | 2.1636 | 173.0687 | 6.6251 |
| Run 4 | 173.5154 | 4.3147 | 176.9404 | 2.1055 | 177.4118 | 3.0499 |
| Run 5 | 178.1167 | 1.8644 | 174.6758 | 1.7307 | 177.2100 | 1.7704 |

Table 2: Thrust Force Data for Instrument Validation

| Cutting Force Data |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Run <br> No. | Data Set 1 |  | Data Set 2 |  | Data Set 3 |  |  |
|  | Mean | Std <br> Deviation | Mean | Std <br> Deviation | Mean | Std <br> Deviation |  |
| Run 1 | 172.4828 | 6.9405 | 179.2302 | 4.0760 | 168.4391 | 3.0778 |  |
| Run 2 | 171.1007 | 7.5971 | 172.5878 | 7.3604 | 166.7893 | 3.3153 |  |
| Run 3 | 174.1149 | 6.3800 | 176.8490 | 2.3010 | 178.2868 | 6.2337 |  |
| Run 4 | 170.2533 | 4.4802 | 173.8834 | 2.1370 | 168.8458 | 3.0956 |  |
| Run 5 | 175.4985 | 1.9894 | 171.2168 | 1.8795 | 169.6373 | 1.9405 |  |

Table 3: Cutting Force Data for Instrument Validation

The mean and standard deviation values of the cutting force and thrust force is used to conduct a 2 sample $t$-test using the MINITAB 15 statistical software to determine the repeatability of the instrument. The test was conducted with a null hypothesis that the two means were equal. The t-test was conducted for force values between two data sets with different combination available between the three data sets for an average time interval of 50 seconds. The comparison between different data set combinations and their respective p -values are given in Table 5 . The p -values of the t -tests under all different combinations conclude that the cutting force and thrust force responses are equal at $95 \%$ confidence interval and hence the data sets are repeatable since all tests were conducted under the same cutting conditions.

| Data Set <br> Combination | $\mathrm{P}-$ Value |  | $95 \%$ Confidence <br> Interval |  | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Thrust | Cutting | Thrust | Cutting |  |
| Data 1 vs. Data2 | 0.337 | 0.281 | Equal | Equal | Repeatable |
| Data 1 vs. Data3 | 0.615 | 0.354 | Equal | Equal | Repeatable |
| Data 2 vs. Data3 | 0.219 | 0.124 | Equal | Equal | Repeatable |

Table 4: Repeatability Test Analysis

## $\underline{\text { Sensitivity Test }}$

The experiment was conducted at the same dry environment using a $0^{\circ}$ rake tool under two different feeds of 0.001 and 0.002 inches in order to force variation in the response. Three different data sets were collected with each data set comprising of five replicates. The mean of the thrust and cutting force data for an average cutting time of 50 seconds is recorded and is shown in Table 6 and Table 7.

| Thrust Force Data (N) |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Run No. | Data Set 1 |  | Data Set 2 |  | Data Set 3 |  |  |
|  | $0.001 "$ |  |  |  |  |  |  |
|  | $0.002 "$ |  |  |  |  |  |  |
| D1F2 | $0.001 "$ | $0.002 "$ | $0.001 "$ | $0.002 "$ |  |  |  |
| D2F1 | D2F2 | D3F1 | D3F2 |  |  |  |  |
| Run 1 | 178.7172 | 248.7989 | 185.3432 | 241.3228 | 175.1395 | 240.6577 |  |
| Run 2 | 175.5777 | 240.2342 | 177.0952 | 240.373 | 170.6697 | 239.6734 |  |
| Run 3 | 175.7445 | 236.3356 | 178.2868 | 233.2487 | 173.0687 | 240.4760 |  |
| Run 4 | 173.5154 | 239.5938 | 176.9404 | 240.9454 | 172.2748 | 235.7926 |  |
| Run 5 | 178.1167 | 240.2020 | 174.6758 | 237.1459 | 173.2100 | 237.4057 |  |

Table 5: Thrust Force Data for Sensitivity Test

| Cutting Force Data (N) |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Run No. | Data Set 1 |  | Data Set 2 |  | Data Set 3 |  |  |
|  | $0.001 "$ | $0.002 "$ | $0.001 "$ | $0.002 "$ | $0.001 "$ | $0.002 "$ |  |
|  | D1F2 | D2F1 | D2F2 | D3F1 | D3F2 |  |  |
| Run 1 | 172.4828 | 268.7188 | 179.2302 | 265.6712 | 168.4391 | 259.0863 |  |
| Run 2 | 171.1007 | 265.9970 | 172.5878 | 266.5099 | 166.7893 | 266.4834 |  |
| Run 3 | 174.1149 | 266.5493 | 176.8490 | 264.6484 | 178.2868 | 270.369 |  |
| Run 4 | 170.2533 | 265.4674 | 173.8834 | 266.5676 | 168.8458 | 262.2706 |  |
| Run 5 | 175.4985 | 268.2023 | 171.2168 | 260.7075 | 169.6373 | 265.3257 |  |

Table 6: Cutting Force Data for Sensitivity Test

MINITAB was again utilized to compare paring of data. The $t$-tests conducted on the data sets under various combinations show that the change in feed has an influence over the cutting and thrust force response and the two means of the data sets are not equal thereby rejecting the null hypothesis. The P -values are calculated and is presented in the Table 8. This shows that the instrument is capable of detecting a change in the cutting parameter and hence was determined to be sensitive to change in variables.

| Data Set <br> Combination | P - Value |  | 95 \% Confidence Interval |  | Remarks |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Thrust | Cutting | Thrust | Cutting |  |
| D1F1 vs. D1F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |
| D1F1 vs. D2F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |
| D1F1 vs. D3F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |
| D2F1 vs. D1F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |
| D2F1 vs. D2F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |
| D2F1 vs. D3F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |
| D3F1 vs. D1F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |
| D3F1 vs. D2F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |
| D3F1 vs. D3F2 | 0.000 | 0.000 | Not Equal | Not Equal | Sensitive |

Table 7: Sensitivity Test Analysis
Standard Deviation of the Instrument
The standard deviation of the instrument is given by the sum of the sensitivity of the dynamometer and the sensitivity of the NI USB 6008. The sensitivity of the dynamometer is estimated to be $+/-10 \mathrm{~N}$ by the manufacturer (KISTLER) and the sensitivity of the USB module is +/- 1 N (National Instruments). So the standard deviation of the instrument can be determined as 11 N under normal atmospheric conditions. The standard deviation values of the thrust force and cutting force presented in Table 3 and Table 4 is compared with the standard deviation of the instrument and was found to be less than 11 N which is a good measure for the accuracy and sensitivty of the experimental set up.

## Determination of Sample Size

The sample size necessary to obtain reportable results is of prime importance during the planning stage of the experiments. Sample size is dictated by how accurate
you must be, or how large a margin of error you can tolerate. The larger your sample size, the more sure you can be that their averages truly reflect the population. Power analysis can either be done before or after the data is collected. A power analysis was conducted prior to the research study to determine an appropriate sample size to achieve adequate power.

Statistical power is the capability of the analysis to detect a difference which actually exists between two sets of data or the ability that the test will reject a false null hypothesis to avoid Type II error. A Type II error is the error of not rejecting a null hypothesis when it is not true and increases with decreases with increase in power.

Using the previously collected data from the repeatability and sensitivity analysis, the minimum number of replicates necessary to achieve a statistical power of $95 \%$ was calculated using the MINITAB software. The output of the software is shown in Figure 30 and is evaluated that a sample size of 5 yields in achieving $95 \%$ statistical power which is more than our target power.


Figure 28: Power Curve to achieve 95\% Statistical Power

## CHAPTER 7

## STATISICAL DESIGN OF EXPERIMENT (DOE)

The orthogonal tube turning experiment was mainly designed to study the variation of tool forces, tool surface roughness and shear angle with varying input parameters. The input parameters were decided based upon the literature, trial runs and experience. The different parameters involved in the experiments are presented in Table 9 and are further discussed in this chapter.

| Parameter | Value |
| :--- | :---: |
| Spindle RPM, $\mathrm{N}_{\mathrm{s}}$ | 640 rpm |
| Tool Material | HSS T-56 |
| Sample Material | Aluminum -6061 (54.5 HRB) |
| Width of Cut (tube wall), w | 0.125 inches |
| Environment | Dry, Cold Compressed Air, Nitrogen <br> and Spray Coolant. |
| Tool Rake Angle, $\alpha$ | $-10^{\circ}, 0^{\circ}, 15^{\circ} 30^{\circ}$ |
| Uncut Chip Thickness, $\mathrm{t}_{1}$ | $0.001,0.002,0.003,0.004,0.005$ inches |
| Total Time for each Run | 60 seconds |
| Cutting Speed, v | 500 SFPM |

Table 9: Input Parameters for Tube Turning Experiment

The spindle RPM was calculated based on a cutting speed of 500 sfpm considering the hardness and the geometrical dimensions of the alloy and was determined to be 640 RPM according to the Metals Handbook [21]. RPM calculations are shown in Appendix B.

The properties of Aluminum 6061-T6 are well documented and considering the ease of availability and cost, this alloy was selected for all the experimental purposes. The tube used in this set up was a 3 inch diameter 6061 alloy with a wall thickness of 0.125 inch. Usually the tubes were machined to be a maximum of 9 inches long to avoid the deflection of the work from the chuck. It was decided to use hollow tubes with no supporting tailstock in order to permit long periods of heavy chip cutting.

The effects of atmospheric temperature and humidity are neglected while measuring the responses or while calculating the results, although it should be noted that the lab temperarture and humidity are well controlled by the environmental system. A piece of HSS tool stock with $3 / 4$ inch $\times 3 / 4$ inch $\times 5$ inches is used for all the cutting operations on the lathe. The work piece was machined along the circumference of the tube using the HSS tool. Precise rake angles are ground into the tools as discussed later.

The hardness of Aluminum 6061 was measured using a Rockwell Hardness Tester HR 150A. The indentation for plastic deformation was by $1 / 16$ " ball and a HRB scale was used. The standard and the sample were tested alternately to find the deviation from the exact value and the data is presented in Table 2. The average hardness of the sample is determined to be 54.5 HRB , as would normally be expected of a T6 tempered piece of aviation grade general purpose aluminum (AL 6061). All aluminum was obtained from the same manufacturer and the same production batch.

| Standard $=91.0$ B Scale |  |
| :--- | :--- |
| Indenter $=1 / 16$ inch ball |  |
| Major Load $=100 \mathrm{Kg}$, Minor Load $=10 \mathrm{Kg}$ |  |
| Standard $=90.5$ | Standard $=91.0$ |
| Specimen 1 Trial 1 $=54.5$ | Specimen 2 Trial 2 $=54.5$ |
| Standard $=90.5$ | Standard $=91.0$ |
| Specimen 1 Trial 2 $=54.5$ | Specimen 3 Trial 1 $=54.0$ |
| Standard $=91.0$ | Standard $=91.5$ |
| Specimen 2 Trial 1 $=55.0$ | Specimen 3 Trial 2 $=54.5$ |
|  | Standard $=91.5$ |

Table 9: Evaluation of Hardness of Aluminum 6061
In order to compare the behavior of the responses under various environments, four different cutting environments were chosen. Dry machining with out the aid of any kind of cooling mechanism, Cold compressed air environment obtained by a vortex air gun to direct a continuous supply of cold air at the tool chip interface, Nitrogen environment with the aid of the gas cylinder fitted with a suitable pressure regulator and lastly Cool Mist Environment using a spray coolant generator fitted with a splitter and directed onto the tool chip interface. An argon environment was disregarded after the trial runs since no significant changes in the responses were observed.

Historically, the variation of the tool forces and the tool wear is largely attributed to the tool rake angle. In order to investigate the influence of the tool geometry, four different rake angles were selected and the tools were machined to $-10^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$ so as to obtain data over a wide range of varying rake angles. The $0^{\circ}$ tool is commonly used in industries because of their superior tool life and rigidity [22]. The selected rake angles are machined onto the HSS tools using a surface grinder. The normal range of tool rake angles ( -5 to 15 degrees) is well represented by the 0 and 15 degree tools. The
-10 and +30 degree tools represent an extreme outer range and are not commonly used values except within academia.

Traditionally, the selection of feed is also of prime importance as this decides the variation of tool forces significantly and also determines the chip thickness ratio. During the trial runs the possible optimum feeds were determined to be $0.001,0.002,0.003$, 0.004 and 0.005 inches/revolution. Any feed after 0.005 inch/rev led to an increase in the disfiguration of the chip and a feed of 0.008 inch/rev resulted in smoke which could have burnt the tool or would have caused severe damage to the machine tool if carried out. Traditionally, lathe operators consider a $0.005 \mathrm{inch} /$ rev cut as a "heavy" roughing cut. A finishing cut of $0.0005 / \mathrm{rev}$ to $0.0010 / \mathrm{rev}$ is quite common in industry because of the superior finish produced.

The HSS tools are machined using a HARIG 618 Automatic surface grinder as in Figure 19 to the required rake angles. An angular milling machine vice which can be swiveled to 45 degrees in both the directions was used. The angular vise is held on the magnetic bed of the grinding machine. The tool is held in the vice and is swiveled to the required angle. A dial gauge is run over the surface of the vice to make sure that the vice is gripped parallel to the machine reference. The tool is then machined with a slow feed rate and depth of cut to achieve high quality surface and reduce surface roughness. The vice is swiveled to prepare multiple $-10^{\circ}, 0^{\circ}, 15^{\circ}$ and $30^{\circ}$ tools. During the trial runs it was also established that up to a certain limit the length of the tool protruding out of the tool holder does not make any significant difference with the responses measured (i.e., the tool is stiff). The clearance angle of all the tools was measured to be $15^{\circ}$.


Figure 29: Machining a 30 degree tool on a HARIG 618 Automatic Surface Grinder


Figure 30: Selected Rake Angles machined on a square section HSS tool

The Aluminum tubing measuring 72 inches as obtained by the supplier is cut into tubes of 9 inch length on a Horizontal band saw and the faces are sanded on a vertical belt sander to make them flat and burrs if any are removed using a deburring tool. A small experiment was conducted during the trial runs to determine if there is any
significant change in the force response based on the length of the tube protruding outside the chuck. It is concluded that the length of this protrusion has very negligible effect on the forces and hence can be disregarded.

The experiments are designed at various factor level combinations as shown in Table 10. Each factor level combination comprises of 5 replicates leading to 100 runs under each environment which amounts to 400 runs over a range of four different environments, four different rake angle and five different feeds.

The cutting force and thrust force responses at all possible factor level combination is recorded. Each factor level combination uses a new tool machined to required rake angle. So assuming that the material is being cut for a total of 60 seconds under each cut, every tool was used for 300 seconds to obtain 5 replicates. The used tool was then stored for surface roughness analysis using the confocal laser profilometer. The aluminum chips obtained under each run was labeled accordingly and stored for chip thickness measurement to aid in shear angle calculations.

| Design of Experiment |  |  |
| :--- | :---: | :---: |
| Environment | Rake Angle | Feed (inches) |
| Dry | $-10^{\circ}$ | 0.001 |
| Cold Compressed Air | $0^{\circ}$ | 0.002 |
| Nitrogen | $15^{\circ}$ | 0.003 |
| Spray Coolant | $30^{\circ}$ | 0.004 |

Table 10: Factor Level Combinations of the Principal Experiment.

## CHAPTER 8

## RESULTS AND DISCUSSION

The designed experiment as discussed in Chapter 7 consists of large number of runs at various factor level combinations. Four different cutting environments, four different rake angles and five different feeds were used resulting in 80 different factor level combinations each with five replicates amounting to 400 total runs. The cutting force and thrust force data are initially saved as MS excel files for ease of calculations. A typical graph of variation of cutting tool forces with time is as shown below.


Figure 31: Variation of Tool forces with time.

Further the used tools are measured for surface roughness estimation using a laser confocal profilometer and the data is saved in .txt format. The uncut chip thickness is measured at 5 different locations along the continuous chip and is saved for shear angle calculations. The observed experimental data are tabulated to facilitate further calculations as in Table 11.

| Run | Rake Angle | Feed | Run | Thrust Force, Ft (N) | Cutting Force, Fc (N) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -10 | 0.001 | Run 1 | 177.7517 | 175.9930 |
| 2 | -10 | 0.002 | Run 1 | 251.7904 | 263.4748 |
| 3 | -10 | 0.003 | Run 1 | 310.3103 | 335.1369 |
| 4 | -10 | 0.004 | Run 1 | 356.3264 | 412.3702 |
| 5 | -10 | 0.005 | Run 1 | 407.1834 | 474.6960 |

Table 11: Example Thrust Force and Cutting Force Raw Data (Appendix C)

Based on the observed cutting force and thrust force data, the friction force (F), normal force ( N ), shearing force along the shear plane (Fs) and a force normal to the shear plane $\left(\mathrm{F}_{\mathrm{n}}\right)$ is calculated and the corresponding force ratios are derived.

The cutting forces, shear angle, friction angle and shear stress calculations are based on the classical equations presented in Table 12 as first developed by Merchant (1).

| Data | Symbol | Units | Equations |
| :--- | :---: | :---: | :--- |
| Chip Thickness Ratio | $\mathrm{r}_{\mathrm{c}}$ | none | $r_{c}=\frac{t_{1}}{t_{2}}$ |
| Friction Force | F | N | $F=F_{c} \cdot \sin \alpha+F_{t} \cdot \cos \alpha$ |
| Normal Force | N | N | $N=F_{c} \cdot \cos \alpha-F_{t} \cdot \sin \alpha$ |
| Friction Co-efficient | $\mu$ | none | $\mu=\frac{F}{N}$ |
| Shear Force on Shear <br> Plane, Merchant | $\left(\mathrm{F}_{\mathrm{s}}\right) \mathrm{M}$ | N | $\left(F_{s}\right) M=F_{c} \cdot \cos \phi-F_{t} \cdot \sin \phi$ |
| Normal Force on <br> Shear Plane, Merchant | $\left(\mathrm{F}_{\mathrm{n}}\right) \mathrm{M}$ | N | $\left(F_{n}\right) M=F_{c} \cdot \sin \phi-F_{t} \cdot \cos \phi$ |
| Area of Shear Plane | $\mathrm{A}_{\mathrm{s}}$ | inch |  |
|  |  | $A_{s}=\frac{t_{1} \cdot w}{\sin \phi}$ |  |
| Shear Stress on Shear <br> Plane | $\tau_{\mathrm{s}}$ | MPa | $\tau_{s}=\frac{F_{s}}{A_{s}}$ |
| Shear Plane Angle | $\varphi$ | degree | $\phi=\arctan \left(\frac{r \cos \alpha}{1-r \sin \alpha}\right)$ |
| Friction Angle | $\beta$ | $\operatorname{degree}$ | $\beta=\arctan \left[\frac{F}{N}\right]$ |

Table 12: Equations used to calculate results from the Force Response and Chip Thickness Data (also discussed in Appendix D)

Table 13 and Table 14 show examples of the various forces, force ratios and shear stress calculations. The complete set of experimental force calculations, surface roughness, shear angle and shear stress calculations are presented in Appendix D and Appendix E. All calculations are the factor level average of the 5 replicates meaning that the average of each of the run is averaged to obtain the following data.

| Run <br> No. | Friction <br> Force (F) | Normal <br> Force (N) | F/N <br> Ratio | Fs <br> (Merchant) | Fn <br> (Merchant) | Fs/Fn <br> (Merchant) |
| ---: | :---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 144.4904 | 204.1855 | 0.7076 | 154.0374 | -155.9893 | -0.9875 |
| 2 | 184.1773 | 177.2929 | 1.0388 | 177.2929 | -184.1773 | -0.9626 |
| 3 | 177.9254 | 180.9517 | 0.9833 | 180.9517 | -177.9254 | -1.0170 |
| 4 | 189.0791 | 181.1614 | 1.0437 | 181.1614 | -189.0791 | -0.9581 |
| 5 | 194.3560 | 185.0437 | 1.0503 | 185.0437 | -194.3560 | -0.9521 |

Table 13: Example of Force Ratio Calculations from Appendix (E)

| Run No. | Roughness (microns) | t/tc | Phi (degrees) | Beta (degrees) | As (in2) | $\tau_{\text {s }}(\mathrm{Mpa})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 154.942318 | 0.121892 | 6.704454207 | 35.2848498 | 0.001070683 | 254.3531778 |
| 2 |  |  |  | 46.09109792 |  |  |
| 3 |  |  |  | 44.5168538 |  |  |
| 4 |  |  |  | 46.22510005 |  |  |
| 5 |  |  |  | 46.40603269 |  |  |
| 6 | 161.1517652 | 0.162259 | 8.83393002 | 33.70095615 | 0.001627911 | 248.960118 |
| 7 |  |  |  | 43.80856404 |  |  |
| 8 |  |  |  | 44.03211179 |  |  |
| 9 |  |  |  | 43.9692226 |  |  |
| 10 |  |  |  | 43.64414797 |  |  |

Table 14: Example of Surface Roughness, Shear Angle and Shear Stress Calculation Data from Appendix F

## Variation of Thrust Force ( $\mathrm{F}_{\mathrm{t}}$ ) with Environment, Rake angle and Feed

Statistical analysis of the thrust force $\left(\mathrm{F}_{\mathrm{t}}\right)$ was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that environment has a relatively less effect on this result. The thrust force decreases greatly with increasingly positive rake angles. The thrust force increases sharply as the depth of cut or feed is increased.


Figure 32: Main Effect Plot for Thrust Force response (Minitab 15)


Figure 33: Interaction Plot for Thrust Force response (Minitab 15)


Table 15: ANOVA Table for Thrust Force response (Minitab 15)

The Analysis of Variance (ANOVA) of the thrust force response indicates that the Rake Angle has by far the dominant effect on this force with an F-statistic of 54,313. The feed factor is second in significance with an F-statistic of 15,874 . The interaction of the rake angle and feed outperforms the environment in terms of the F-statisic.

This result can be interpreted as follows. A sharper tool plunges into the work and can form a chip piece with considerably less force required than a blunt tool. The thrust force increases with the increase in feed. Turning using a sharper tool is more likely to reduce the thrust force than just decreasing the feed. The main effects of environment achieve significance but are less than the effect of rake angle and feed on the thrust force. It can also be observed from the main effect plot that the drop in thrust force is more rapid from $0^{\circ}$ to $15^{\circ}$ as compared to other trends.

## Variation of Cutting Force ( $\mathrm{F}_{\mathrm{c}}$ ) with Environment, Rake angle and Feed

Statistical analysis of the Cutting force $\left(\mathrm{F}_{\mathrm{c}}\right)$ was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that environment has a relatively less effect on Cutting force but decreases considerably with increasing positive rake angles. The cutting force greatly increases as the depth of cut or feed is increased.


Figure 34: Main Effect Plot for Cutting Force response (Minitab 15)


Figure 35: Interaction Plot for Cutting Force response (Minitab 15)

## General Linear Model: Cutting Force versus Environment, Rake Angle, Feed



Table 16: ANOVA Table for Cutting Force response (Minitab 15)

The Analysis of Variance (ANOVA) of the cutting force response indicates that the significant main effect of feed on this force with an F-statistic of 53125. The rake angle is the next most significant factor with an F-statistic of 16774. The effect of environment outperforms the interaction of feed and rake angle in terms of the F-statistic

The cutting force is the force in the direction of the work motion against the tool. The increase in feed demands more energy for the plastic deformation of the material thus consuming more power leading to larger cutting force responses. The simple effect also shows the decrease in cutting force with decrease in feed. Turning at a lower feed is more likely to reduce the cutting force than just using a sharper tool. The main effects of environment achieve significance but are less than the individual effect of rake angle and feed on the cutting force. It is also to be noted that the increase in cutting force is close to linear with the increase in feed.

## Variation of Friction Force (F) with Environment, Rake angle and Feed

Statistical analysis of the Friction force (F) was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that cold compressed air environment showed a reduction in the friction force as compared to other environments. Friction force decreases greatly with increasing positive rake angles. The friction force greatly increases as the depth of cut or feed is increased.


Figure 36: Main Effect Plot of Friction Force data (Minitab 15)


Figure 37: Interaction Plot for Friction Force data (Minitab 15)


Table 17: ANOVA Table for Friction Force (Minitab 15)

The calculated friction force response was subjected to Analysis of Variance (ANOVA) and the result shows a significant main effect of rake angle upon the force response with an F-statistic of 878 . The feed factor is second in significance with an Fstatistic of 363 . The environment has very little effect on the friction force response when compared to rake angle and feed in terms of F-statistic.

The pattern of the findings during the analysis of the friction force is same as the ones observed for thrust force response. A rapid decrease in friction force values occur for a rake angle between $0^{\circ}$ to $15^{\circ}$. The friction force is considerably less when cutting using a sharper tool. Also the increase in feed causes an increase in friction force due to the increase in energy consumed to cause the plastic deformation of the work piece.

## Variation of Normal Force (N) with Environment, Rake angle and Feed

Statistical analysis of the Normal force ( N ) was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that the Environment has very little effect on the normal force response as compared to the other parameters. A considerable decrease in normal force is observed with the increasing positive rake angles. The Normal force greatly increases as the depth of cut or feed is increased.


Figure 38: Main Effect Plot of Normal Force response (Minitab 15)


Figure 39: Interaction Plot for Normal Force response (Minitab 15)


Table 18: ANOVA Table for Normal Force response (Minitab 15)
The calculated normal force response was subjected to Analysis of Variance and the result shows that feed has by far the dominant effect on this force with an F-statistic of 1683. The tool rake angle is second in significance with an F-statistic of 766. Environment does have very little effect on the normal force response but is negligible when compared to individual effects of rake angle and feed.

The pattern of the findings during the analysis of the normal force is same as the ones observed for cutting force response. The increase in feed causes an increase in normal force due to the increase in energy consumed to cause the plastic deformation of the work piece. It is also to be noted that the combined effect of environment, rake angle and feed fails to achieve significance on the normal force response with an F-statistic of 1.40 and $\mathrm{p}>0.001$. The main effect curve for increase in normal force with increase in feed is close to linear however rake angle too has a considerable effect resulting in reduced normal force when using a sharper tool.

## Variation of F/N Ratio with Environment, Rake angle and Feed

Statistical analysis of the F/N Ratio was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that the Environment has almost constant effect on this force ratio. $\mathrm{F} / \mathrm{N}$ ratio is found to abruptly decrease with the increasing rake angle. An appreciable decrease in $\mathrm{F} / \mathrm{N}$ ratio is observed with the increase in depth of cut or feed.


Figure 40: Main Effect Plot of F/N Ratio (Minitab 15)


Figure 41: Interaction Plot for F/N Ratio (Minitab 15)

## General Linear Model: F/N Ratio versus Environment, Rake Angle, Feed



Table 19: ANOVA Table for F/N Ratio (Minitab 15)

Analysis of Variance (ANOVA) of F/N Ratio indicates that the rake angle has by far the dominant effect on this force ratio with an F-statistic of 57. The environment and feed fail to attain significance on $\mathrm{F} / \mathrm{N}$ ratio with their p values being greater than $0.001 . \mathrm{d}$

Also the effect of the interaction between environment, rake angle and feed has no significance on the $\mathrm{F} / \mathrm{N}$ ratio. The interaction plot obtained shows that with a $30^{\circ}$ rake angle tool a much lower $\mathrm{F} / \mathrm{N}$ ratio is obtained than compared to a $0^{\circ}$, $15^{\circ}$ or a $-10^{\circ}$ tool. Also a drastic decrease in $\mathrm{F} / \mathrm{N}$ ratio is observed between rake angles of $0^{\circ}$ to $15^{\circ}$.

## Variation of Shear Force along Shear Plane ( $\mathrm{F}_{\mathbf{s}}$ ) with Environment, Rake and Feed

Statistical analysis of the Shear force along the shear plane $\left(\mathrm{F}_{\mathrm{s}}\right)$ was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that the effect of environment on the shear force is nearly a constant. Shear force decreases appreciably with increasing positive rake angles. The Shear force greatly increases as the depth of cut or feed is increased.


Figure 42: Main Effect Plot of Shear Force along Shear Plane (Minitab 15)


Figure 43: Interaction Plot for Shear Force along Shear Plane (Minitab 15)

General Linear Model: Fs (Merchant) versus Environment, Rake Angle, Feed


Table 20: ANOVA Table for Shear Force along Shear Plane (Minitab 15)

Analysis of Variance (ANOVA) of the shear force response indicates that feed has a significant main effect of feed upon the force response with an F-statistic of 1689. The tool rake angle is the next most dominant factor with an F-statistic of 522.

Turning at a lower speed is more likely to decrease the shear force than using a sharper tool. Also the effect of interaction between environment, rake angle and feed failed to achieve significance with F -statistic being 1.48 and a p value $>0.001$. Negligible drop in shear force is observed between $-10^{\circ}$ and $0^{\circ}$ rake angle where as a drop in nearly 100 N is observed between a $0^{\circ}$ and a $30^{\circ}$ tool. Environment does have an effect on the shear force but the effect is negligible when compared to individual effects of tool rake angle and feed.

## Variation of Normal Force along Shear Plane ( $\mathbf{F}_{\mathbf{n}}$ ) with Environment, Rake an Feed

Statistical analysis of the Normal force along the shear plane $\left(\mathrm{F}_{\mathrm{n}}\right)$ was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that the Environment has very little effect on the normal force response. A considerable decrease in normal force is observed with the increasing positive rake angles. The normal force along shear plane increases considerably as the depth of cut or feed is increased.


Figure 44: Main Effect Plot of Normal Force along Shear Plane (Minitab 15)


Figure 45: Interaction Plot for Normal Force along Shear Plane (Minitab 15)


Table 21: ANOVA Table for Normal Force along Shear Plane (Minitab 15)

Analysis of Variance of the Normal force along the shear plane indicates that the rake angle has a significant effect on this force with an F-statistic of 1689. The rake angle factor is second in significance with an F-statistic of 592. Environment has an effect on the normal force along the shear plane but is negligible compared to individual effects of rake angle and feed.

Turning using a sharper tool is more likely to reduce the nomal force than just decreasing the feed although a considerable decrease in force is observed with the decrease in feed. Also the effect of cutting environment is prominent for the normal force on the shear plane and is found be the same for nitrogen and spray coolant environment.

## Variation of Fs/Fn Ratio with Environment, Rake and Feed

Statistical analysis of the $\mathrm{F}_{\mathrm{s}} / \mathrm{F}_{\mathrm{n}}$ Ratio was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that the Environment has varying effect on this force ratio. $\mathrm{F}_{\mathrm{s}} / \mathrm{F}_{\mathrm{n}}$ ratio is found to increase with the increasing rake angle. A fairly constant response is obtained due to the increase in the feed.


Figure 46: Main Effect Plot for Fs/Fn Ratio (Minitab 15)


Figure 47: Interaction Plot for Fs/Fn Ratio (Minitab 15)

## General Linear Model: Fs/Fn (Merchant) versus Environment, Rake Angle, Feed



Table 22: ANOVA Table for Fs/Fn Ratio (Minitab 15)

Analysis of Variance (ANOVA) of $\mathrm{F}_{\mathrm{s}} / \mathrm{F}_{\mathrm{n}}$ Ratio indicates that the rake angle has by far the dominant effect on this force ratio with an F-statistic of 350 . The environment and feed fail to attain significance on $\mathrm{F}_{\mathrm{s}} / \mathrm{F}_{\mathrm{n}}$ ratio with their p values being greater than 0.001 .

Also the effect of the interaction between environment, rake angle and feed has no significance on the $\mathrm{F}_{\mathrm{s}} / \mathrm{F}_{\mathrm{n}}$ ratio. The interaction plot obtained shows that with a $30^{\circ}$ rake angle tool a much lower $\mathrm{F}_{\mathrm{s}} / \mathrm{F}_{\mathrm{n}}$ ratio is obtained than compared to a $0^{\circ}, 15^{\circ}$ or a $-10^{\circ}$ tool. Also a drastic decrease in $\mathrm{F}_{\mathrm{s}} / \mathrm{F}_{\mathrm{n}}$ ratio is observed between rake angles of $0^{\circ}$ to $15^{\circ}$.

## Variation of Shear Plane Angle ( $\varphi$ ) with Environment, Rake and Feed

Statistical analysis of the Shear angle $(\varphi)$ was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicate that environment and feed has very little effect on the shear angle. Shear angle increases greatly with increasing rake angles. Also an increase in feed results in considerable rise in the shear plane angle value.


Figure 48: Main Effect Plot for Shear Plane Angle (Minitab 15)


Figure 49: Interaction Plot for Shear Plane Angle (Minitab 15)

General Linear Model: Phi (degrees) versus Environment, Rake Angle, Feed


Table 23: ANOVA Table for Shear angle ( $\varphi$ ) (Minitab 15)

Analysis of Variance (ANOVA) of Shear angle indicates that the rake angle has by far the dominant effect on this force ratio with an F-statistic of 3,897 . The feed factor is second in significance with an F-statistic of 1,165 . The individual effect of environment and the interaction effect of environment and rake angle are also found to have appreciable effect on the shear angle with their significant F-statistic values.

The shear plane angle is found to be lowest when machining under a nitrogen atmosphere when compared to other environments and is as shown in the main effects plot in figure 48. It can also be observed that the shear plane angle increases with increase in both rake angle and feed. A $30^{\circ}$ rake angle tool is found to produce higher shear angle than compared to a $-10^{\circ}, 0^{\circ}$ or a $15^{\circ}$ tool.

## Variation of Friction Angle ( $\beta$ ) with Environment, Rake and Feed

Statistical analysis of the Friction angle ( $\beta$ ) was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that the effect of environment and feed on the friction angle is nearly a constant. Friction angle decreases appreciably with increasing positive rake angles.


Figure 50: Main Effect Plot for Friction Angle (Minitab 15)


Figure 51: Interaction Plot for Friction Angle (Minitab 15)

| Factor | Type |  | Levels | Values |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Environment | fixed | d 4 |  | Dry, Cold C | mpressed Air | Air |  |  |
| Rake Angle | fixed | d 4 |  | -10, 0, 15, 30 |  |  | gen, Cool Mist |  |
| Feed | fixed | d 5 |  | 001, 0.002 | , 0.003, 0 | 0.004, 0.005 |  |  |
| Analysis of | rian | nce for Fri | tion | Angle (be | a), using | Adjusted | SS for | Tests |
| Source |  |  | DF | Seq SS | Adj SS | Adj MS | F | P |
| Environment |  |  | 3 | 173.48 | 173.48 | 57.83 | 0.97 | 0.405 |
| Rake Angle |  |  | 3 | 14983.93 | 14983.93 | 4994.64 | 84.21 | 0.000 |
| Feed |  |  | 4 | 759.27 | 759.27 | 189.82 | 3.20 | 0.013 |
| Environment* | Rake A | Angle | 9 | 410.15 | 410.15 | 45.57 | 0.77 | 0.646 |
| Environment* | eed |  | 12 | 383.82 | 383.82 | 31.98 | 0.54 | 0.888 |
| Rake Angle*F | eed |  | 12 | 394.25 | 394.25 | 32.85 | 0.55 | 0.878 |
| Environment* | Rake A | Angle*Feed | 36 | 1423.97 | 1423.97 | 39.55 | 0.67 | 0.930 |
| Error |  |  | 320 | 18979.97 | 18979.97 | 59.31 |  |  |
| Total |  |  | 399 | 37508.82 |  |  |  |  |
| $S=7.70145$ | $\mathrm{R}-\mathrm{Sq}$ | $q=49.40 \%$ | R-S | $q(a d j)=3$ | $6.91 \%$ |  |  |  |

Table 24: ANOVA Table for Friction Angle (Minitab 15)

Analysis of Variance (ANOVA) of Friction angle indicates that the rake angle has by far the dominant effect on this force ratio with an F-statistic of 84 . The environment and feed fail to attain significance on friction angle $(\beta)$ with their p values being greater than 0.001.

The interaction plot obtained shows that with a $30^{\circ}$ rake angle tool a much lower friction angle is obtained than compared to a $0^{\circ}, 15^{\circ}$ or a $-10^{\circ}$ tool. Also a drastic decrease in friction angle is observed between rake angles of $0^{\circ}$ to $15^{\circ}$.It is evident from the above exsperiment that the friction angle is soley dependent on rake angle.

## Variation of Shear Stress ( $\tau_{\mathbf{s}}$ ) with Environment, Rake and Feed

Statistical analysis of the Shear Stress $\left(\tau_{\mathrm{s}}\right)$ was conducted using the GLM (general linear module) of MINITAB 15. The main effects plot indicates that machining under nitrogen environment results in reduced shear stress as compared to other environments. The effect of rake angle factor is variable on the shear stress however a decrease in feed causes a significant decrease in the shear stress.


Figure 52: Main Effect Plot for Shear Stress (Minitab 15)


Figure 53: Interaction Plot for Shear Stress (Minitab 15)

## General Linear Model: Shear Stress versus Environment, Rake Angle, Feed



Table 25: ANOVA Table for Shear Stress (Minitab 15)
Analysis of Variance (ANOVA) of the shear stress response indicates that feed has a significant main effect upon the response with an F-statistic of 48. The tool rake angle is the next most dominant factor with an F-statistic of 36.

The interaction between the environment, rake angle and feed is found to have prominence over the shear stress. Also the shear stress is found to decrease with the increase in feed due to the decrease in shear force and increase in shear area leading to increase in shear plane angle [23].

## Variation of Tool Surface Roughness with Environment, Rake and Feed

The visual observations, study and literature, all states that the variation of environment, rake angle and feed will have an influence on the tool surface. It can be observed from the main effects plot that the tool wear is found to be the least under nitrogen environment than compared to dry, cold compressed air or spray coolant environment.


Figure 54: Main Effect Plot for Tool Surface Roughness (Minitab 15)


Figure 55: Interaction Plot for Tool Surface Roughness (Minitab 15)

The dry cutting environment produced an average surface roughness of 102 microns, with cold compressed air environment producing a surface roughness of 75 microns. The spray coolant environment resulted in a tool surface roughness of 70 microns as against nitrogen environment resulting in an average tool surface roughness of 55 microns.

Tool surface roughness is also found to be higher for the $-10^{\circ}$ and $30^{\circ}$ tool when compared to a $0^{\circ}$ or a $15^{\circ}$ tool which showed significantly less surface roughness under all environments. Increase in tool surface roughness is observed with the increase in feed and is highest for a 0.005 inch feed. Also it is to be noted that the tool surface roughness is found to increase with the increase in thrust force and cutting force.

Appendix G provides detailed examples of each calculated value which was discussed in the chapter.

## Variation of Tool Surface Roughness with Normal Force



Figure 56: Variation of Tool surface roughness with Normal Force

The plot of variation of Tool surface roughness with normal force as shown in Figure 56 for a $0^{\circ}$ and a $15^{\circ}$ tool under all cutting environment shows that tool surface roughness increases with the increase in normal force. It is also to be noted that a $15^{\circ}$ tool has always generated less force compared to a $0^{\circ}$ tool under all four cutting environments. The tool surface roughness in the case of Nitrogen environment is less than the cool mist environment for both $0^{\circ}$ and $15^{\circ}$ tool rake angles. It is evident that nitrogen environment showed reduced tool surface roughness due to the decrease in shear angle and reduction
in tool chip contact length. During the experiments it was also observed that the gases applications generally proved better results than dry machining.

## CHAPTER 9

## CONCLUSIONS

Based on a through analysis of the experimental results and observations the following conclusions are made about the variation of tool forces, tool surface roughness and the behavior of the shear angle with the change in input parameters.

1. The cutting force and the thrust force increases significantly with increase in feed. This can be explained by the fact that a feed rate increase will increase the amount of energy required to cause the plastic deformation of the material, resulting in increased tool forces.
2. The cutting force and thrust force decreases marginally with the increase in rake angle from $-10^{\circ}$ to $0^{\circ}$ but decreases rapidly with the increase in rake angle from $0^{\circ}$ to $30^{\circ}$. This can be explained by the fact that the tool chip contact area decreases with the increase in rake angle leading to the decrease in tool forces.
3. Reduced cutting force and thrust force are achieved using cold compressed air environment as compared to dry environment. The nitrogen environment produced a marginal decrease in forces as compared to spray coolant environment. It can be concluded that a tube turning set up with a nitrogen environment is the best environment for prolonging tool life at 500 sfpm during Orthogonal Tube Turning of AL 6061-T6.
4. Onset of Shear angle is found to be influenced by all the factor levels and is found to be the least at nitrogen environment. An increase in onset of shear angle is observed with an increase in rake angle and feed.
5. Tool surface roughness increases with the increase in feed from 0.001 inch to 0.005 inch. The surface roughness is also found to be significantly less when using a $0^{\circ}$ or a $15^{\circ}$ rake angle tool when compared to a $-10^{\circ}$ or a $30^{\circ}$ tool.
6. Environment is found to have a significant effect on the tool surface roughness. The surface roughness in the nitrogen environment is found to be significantly less than all the other machining environments. The dry cutting environment produced an average surface roughness of 102 microns, with cold compressed air environment producing a surface roughness of 75 microns. The spray coolant environment resulted in a tool surface roughness of 70 micros as against nitrogen environment resulting in a average tool roughness of 55 microns.

## CHAPTER 10

## SCOPE FOR FUTURE WORK

A recent CIRP working paper reports the survey by a leading tool manufacturer indicating the following factors

- A correct cutting tool is selected less than $50 \%$ of the time.
- A tool is used at the rated cutting speed only $58 \%$ of the time.
- Only $38 \%$ of tools are used up to their full life capability

Viktor P Astakhov [24] states that today's Industry is completely dependent on empirical data provided by cutting tool and machine tool manufacturers as well as data provided through handbooks and workshops by Professional Engineering Associations. There is a lack of agreement in the data as it does not originate from the same source and there is no unified Metal Cutting Theory. Non availability of reliable tool life and optimum cutting parameters data for various tool and work material combinations leads to the reduced life of cutting tool and machine tools, so it is of prime importance to develop a realistic theory that governs the mechanism of metal cutting more deterministically and more accurately.

1. Additional models, other than the 1945 Merchant Model, can be compared to the data obtained in this thesis.
2. Cryogenic nitrogen is being investigated routinely as a cutting enviorment. It was not done during this experiment due to time and cost constraints. The forces, shear angle and tool surface roughness data under the various environments carried out can be compared with the cryogenic environment to more accurately determine the variation of responses with environment.
3. The complete insight of the behavior of the cutting forces, onset of shear plane angle, friction angle, shear stress and tool surface roughness with the variation in the feed, rake angle, cutting speed and environment is yet to be established by providing correction factors to the classical equations if necessary.
4. A simulation of the orthogonal tube turning can be carried out using an analysis package like ANSYS or NASTRAN to develop an optimum cutting condition in terms of tool forces and tool surface roughness.

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## APPENDIX A

The calibration certificate for the Kistler 9257 A dynamometer is given below.


## APPENDIX B

The spindle speed was calculated considering the material hardness and the geometrical dimensions of the alloy as shown below.

Alloy: Aluminum 6061
Hardness: 54.5 HRB
Diameter: 3 inches
Wall thickness: 0.125 inches
Considering a feed of $0.002 \mathrm{inch} / \mathrm{rev}$ to $0.005 \mathrm{inch} / \mathrm{rev}$ from "Machinery's Handbook" $27^{\text {th }}$ Edition, pp 1038 for an Aluminum 6061 alloy being machined by a HSS tool the speed is 500 feet/minute.

Volume Swept by the tool in 1 revolution $=2 \times \pi \times 1.5=9.426$ inches

$$
=0.7855 \text { feet. }
$$

## Cutting Speed

$\qquad$
Volume Swept by the tool in 1 revolution

$$
=\frac{500 \frac{\text { feet }}{\text { minute }}}{0.7855 \frac{\text { feet }}{\text { rev }}}=\mathbf{6 3 6 . 5 3 7 2} \mathbf{~ R P M}
$$

The spindle speed was approximated as 640 RPM for the ease of calculations.

## APPENDIX C

The below table gives the Thrust Force, Cutting Force and Cut Chip thickness data for all the 80 different factor level combinations.

| Run No. | Environment | $\boldsymbol{\alpha}$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Dry | -10 | 0.001 | Run 1 | 177.7517 | 175.993 | 0.0079 |
| 2 | Dry | -10 | 0.001 | Run 2 | 184.1773 | 177.2929 | 0.00833 |
| 3 | Dry | -10 | 0.001 | Run 3 | 177.9254 | 180.9517 | 0.00834 |
| 4 | Dry | -10 | 0.001 | Run 4 | 189.0791 | 181.1614 | 0.00808 |
| 5 | Dry | -10 | 0.001 | Run 5 | 194.356 | 185.0437 | 0.00837 |
| 6 | Dry | -10 | 0.002 | Run 1 | 251.7904 | 263.4748 | 0.01248 |
| 7 | Dry | -10 | 0.002 | Run 2 | 257.8228 | 268.7747 | 0.01263 |
| 8 | Dry | -10 | 0.002 | Run 3 | 258.6709 | 267.5613 | 0.01207 |
| 9 | Dry | -10 | 0.002 | Run 4 | 262.6206 | 272.2441 | 0.01229 |
| 10 | Dry | -10 | 0.002 | Run 5 | 264.2924 | 277.1065 | 0.01216 |
| 11 | Dry | -10 | 0.003 | Run 1 | 310.3103 | 335.1369 | 0.0177 |
| 12 | Dry | -10 | 0.003 | Run 2 | 327.1769 | 341.8487 | 0.01766 |
| 13 | Dry | -10 | 0.003 | Run 3 | 304.3356 | 340.2505 | 0.01742 |
| 14 | Dry | -10 | 0.003 | Run 4 | 313.9446 | 347.0742 | 0.0176 |
| 15 | Dry | -10 | 0.003 | Run 5 | 301.7063 | 335.4178 | 0.01719 |
| 16 | Dry | -10 | 0.004 | Run 1 | 356.3264 | 412.3702 | 0.02054 |
| 17 | Dry | -10 | 0.004 | Run 2 | 350.0089 | 402.2674 | 0.02122 |
| 18 | Dry | -10 | 0.004 | Run 3 | 370.2052 | 419.0703 | 0.02041 |
| 19 | Dry | -10 | 0.004 | Run 4 | 364.9769 | 409.6705 | 0.02143 |
| 20 | Dry | -10 | 0.004 | Run 5 | 375.6279 | 424.4903 | 0.02065 |
| 21 | Dry | -10 | 0.005 | Run 1 | 407.1834 | 474.696 | 0.02355 |
| 22 | Dry | -10 | 0.005 | Run 2 | 410.9808 | 475.7449 | 0.02417 |
| 23 | Dry | -10 | 0.005 | Run 3 | 404.456 | 467.8064 | 0.02412 |
| 24 | Dry | -10 | 0.005 | Run 4 | 415.8704 | 479.9004 | 0.02454 |
| 25 | Dry | -10 | 0.005 | Run 5 | 416.2005 | 483.9898 | 0.02425 |
| 26 | Dry | 0 | 0.001 | Run 1 | 178.7172 | 172.4828 | 0.00647 |
| 27 | Dry | 0 | 0.001 | Run 2 | 175.5777 | 171.1007 | 0.00624 |
| 28 | Dry | 0 | 0.001 | Run 3 | 175.7445 | 174.1149 | 0.0063 |
| 29 | Dry | 0 | 0.001 | Run 4 | 173.5154 | 170.2533 | 0.00651 |
| 30 | Dry | 0 | 0.001 | Run 5 | 170.9717 | 172.3044 | 0.00647 |
| 31 | Dry | 0 | 0.002 | Run 1 | 223.7989 | 255.7188 | 0.01126 |
| 32 | Dry | 0 | 0.002 | Run 2 | 218.0048 | 250.2855 | 0.01114 |


| Run No. | Environment | $\alpha$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 33 | Dry | 0 | 0.002 | Run 3 | 219.3895 | 254.1104 | 0.01158 |
| 34 | Dry | 0 | 0.002 | Run 4 | 226.1762 | 264.9091 | 0.01145 |
| 35 | Dry | 0 | 0.002 | Run 5 | 220.2374 | 255.4329 | 0.01138 |
| 36 | Dry | 0 | 0.003 | Run 1 | 293.5401 | 323.8849 | 0.01375 |
| 37 | Dry | 0 | 0.003 | Run 2 | 304.5111 | 329.6172 | 0.0141 |
| 38 | Dry | 0 | 0.003 | Run 3 | 297.467 | 329.553 | 0.01405 |
| 39 | Dry | 0 | 0.003 | Run 4 | 292.9392 | 325.1263 | 0.01384 |
| 40 | Dry | 0 | 0.003 | Run 5 | 292.05 | 323.1182 | 0.01385 |
| 41 | Dry | 0 | 0.004 | Run 1 | 360.526 | 414.8286 | 0.01746 |
| 42 | Dry | 0 | 0.004 | Run 2 | 363.5965 | 399.0163 | 0.01774 |
| 43 | Dry | 0 | 0.004 | Run 3 | 377.5881 | 399.5048 | 0.01746 |
| 44 | Dry | 0 | 0.004 | Run 4 | 361.6405 | 411.0423 | 0.01735 |
| 45 | Dry | 0 | 0.004 | Run 5 | 373.5652 | 403.9943 | 0.0179 |
| 46 | Dry | 0 | 0.005 | Run 1 | 319.7004 | 460.565 | 0.02348 |
| 47 | Dry | 0 | 0.005 | Run 2 | 327.1955 | 450.0505 | 0.02348 |
| 48 | Dry | 0 | 0.005 | Run 3 | 327.1843 | 459.6015 | 0.02314 |
| 49 | Dry | 0 | 0.005 | Run 4 | 329.8673 | 448.3882 | 0.02324 |
| 50 | Dry | 0 | 0.005 | Run 5 | 323.936 | 458.4112 | 0.02357 |
| 51 | Dry | 15 | 0.001 | Run 1 | 58.8858 | 127.9112 | 0.00547 |
| 52 | Dry | 15 | 0.001 | Run 2 | 65.4667 | 120.879 | 0.00556 |
| 53 | Dry | 15 | 0.001 | Run 3 | 69.0838 | 114.2018 | 0.00562 |
| 54 | Dry | 15 | 0.001 | Run 4 | 66.4581 | 122.6205 | 0.00522 |
| 55 | Dry | 15 | 0.001 | Run 5 | 66.4237 | 120.155 | 0.00527 |
| 56 | Dry | 15 | 0.002 | Run 1 | 107.4316 | 201.9459 | 0.01054 |
| 57 | Dry | 15 | 0.002 | Run 2 | 113.0798 | 200.5681 | 0.0106 |
| 58 | Dry | 15 | 0.002 | Run 3 | 114.3104 | 199.1714 | 0.01055 |
| 59 | Dry | 15 | 0.002 | Run 4 | 118.0056 | 204.2604 | 0.01019 |
| 60 | Dry | 15 | 0.002 | Run 5 | 118.1204 | 201.6331 | 0.01074 |
| 61 | Dry | 15 | 0.003 | Run 1 | 131.4321 | 261.1614 | 0.01455 |
| 62 | Dry | 15 | 0.003 | Run 2 | 142.362 | 262.1011 | 0.01446 |
| 63 | Dry | 15 | 0.003 | Run 3 | 153.4347 | 268.9463 | 0.01457 |
| 64 | Dry | 15 | 0.003 | Run 4 | 148.8125 | 262.3391 | 0.01459 |
| 65 | Dry | 15 | 0.003 | Run 5 | 151.5232 | 265.1171 | 0.01466 |
| 66 | Dry | 15 | 0.004 | Run 1 | 199.523 | 355.5064 | 0.01961 |
| 67 | Dry | 15 | 0.004 | Run 2 | 201.9163 | 354.7528 | 0.01952 |
| 68 | Dry | 15 | 0.004 | Run 3 | 207.3945 | 347.9605 | 0.0196 |
| 69 | Dry | 15 | 0.004 | Run 4 | 201.1935 | 339.4066 | 0.0194 |
| 70 | Dry | 15 | 0.004 | Run 5 | 212.3329 | 348.3219 | 0.0195 |
| 71 | Dry | 15 | 0.005 | Run 1 | 214.2508 | 410.0906 | 0.02203 |
| 72 | Dry | 15 | 0.005 | Run 2 | 224.6541 | 411.051 | 0.02271 |
| 73 | Dry | 15 | 0.005 | Run 3 | 227.3489 | 405.2153 | 0.02242 |
| 74 | Dry | 15 | 0.005 | Run 4 | 223.9582 | 407.5608 | 0.02251 |
| 75 | Dry | 15 | 0.005 | Run 5 | 233.539 | 412.6333 | 0.02249 |
| 76 | Dry | 30 | 0.001 | Run 1 | 63.2424 | 116.0273 | 0.00565 |
| 77 | Dry | 30 | 0.001 | Run 2 | 63.6391 | 116.4696 | 0.00554 |
| 78 | Dry | 30 | 0.001 | Run 3 | 63.6573 | 117.28 | 0.00562 |
| 79 | Dry | 30 | 0.001 | Run 4 | 64.9941 | 118.6791 | 0.00552 |


| Run No. | Environment | $\boldsymbol{\alpha}$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 80 | Dry | 30 | 0.001 | Run 5 | 62.9518 | 115.4918 | 0.00545 |
| 81 | Dry | 30 | 0.002 | Run 1 | 81.252 | 188.0265 | 0.00951 |
| 82 | Dry | 30 | 0.002 | Run 2 | 81.1605 | 176.7414 | 0.0096 |
| 83 | Dry | 30 | 0.002 | Run 3 | 88.0791 | 178.6659 | 0.00958 |
| 84 | Dry | 30 | 0.002 | Run 4 | 90.344 | 181.2736 | 0.00927 |
| 85 | Dry | 30 | 0.002 | Run 5 | 91.9134 | 182.55 | 0.00933 |
| 86 | Dry | 30 | 0.003 | Run 1 | 92.8429 | 236.4955 | 0.01134 |
| 87 | Dry | 30 | 0.003 | Run 2 | 99.4893 | 239.5004 | 0.01155 |
| 88 | Dry | 30 | 0.003 | Run 3 | 98.1772 | 238.2484 | 0.01113 |
| 89 | Dry | 30 | 0.003 | Run 4 | 98.0449 | 242.13 | 0.01143 |
| 90 | Dry | 30 | 0.003 | Run 5 | 100.0638 | 239.2623 | 0.01156 |
| 91 | Dry | 30 | 0.004 | Run 1 | 136.5777 | 316.4789 | 0.0115 |
| 92 | Dry | 30 | 0.004 | Run 2 | 140.2462 | 323.6529 | 0.01152 |
| 93 | Dry | 30 | 0.004 | Run 3 | 143.6655 | 315.2217 | 0.01569 |
| 94 | Dry | 30 | 0.004 | Run 4 | 141.0172 | 322.3968 | 0.01583 |
| 95 | Dry | 30 | 0.004 | Run 5 | 141.963 | 316.2296 | 0.0156 |
| 96 | Dry | 30 | 0.005 | Run 1 | 90.2882 | 333.6152 | 0.01761 |
| 97 | Dry | 30 | 0.005 | Run 2 | 93.9447 | 333.7997 | 0.01768 |
| 98 | Dry | 30 | 0.005 | Run 3 | 91.8477 | 339.6543 | 0.01733 |
| 99 | Dry | 30 | 0.005 | Run 4 | 101.1709 | 335.6297 | 0.01756 |
| 100 | Dry | 30 | 0.005 | Run 5 | 99.2913 | 343.7709 | 0.01766 |
| 101 | Compressed Air | -10 | 0.001 | Run 1 | 197.7884 | 182.1416 | 0.00933 |
| 102 | Compressed Air | -10 | 0.001 | Run 2 | 201.2496 | 185.7809 | 0.00958 |
| 103 | Compressed Air | -10 | 0.001 | Run 3 | 199.8761 | 184.3276 | 0.00919 |
| 104 | Compressed Air | -10 | 0.001 | Run 4 | 199.5928 | 186.4235 | 0.00951 |
| 105 | Compressed Air | -10 | 0.001 | Run 5 | 200.8335 | 187.2002 | 0.00975 |
| 106 | Compressed Air | -10 | 0.002 | Run 1 | 256.1353 | 262.1515 | 0.01296 |
| 107 | Compressed Air | -10 | 0.002 | Run 2 | 259.7657 | 260.5958 | 0.01365 |
| 108 | Compressed Air | -10 | 0.002 | Run 3 | 261.4814 | 264.5966 | 0.01346 |
| 109 | Compressed Air | -10 | 0.002 | Run 4 | 268.5294 | 271.2766 | 0.01356 |
| 110 | Compressed Air | -10 | 0.002 | Run 5 | 269.8701 | 274.0365 | 0.01359 |
| 111 | Compressed Air | -10 | 0.003 | Run 1 | 293.3559 | 324.7656 | 0.0165 |
| 112 | Compressed Air | -10 | 0.003 | Run 2 | 296.6442 | 324.1789 | 0.0164 |
| 113 | Compressed Air | -10 | 0.003 | Run 3 | 302.8356 | 329.6997 | 0.01657 |
| 114 | Compressed Air | -10 | 0.003 | Run 4 | 299.3754 | 331.8196 | 0.01632 |
| 115 | Compressed Air | -10 | 0.003 | Run 5 | 310.1497 | 340.834 | 0.01661 |
| 116 | Compressed Air | -10 | 0.004 | Run 1 | 339.8878 | 395.3502 | 0.01964 |
| 117 | Compressed Air | -10 | 0.004 | Run 2 | 347.7198 | 397.9039 | 0.01972 |
| 118 | Compressed Air | -10 | 0.004 | Run 3 | 354.7987 | 405.5534 | 0.01951 |
| 119 | Compressed Air | -10 | 0.004 | Run 4 | 358.8273 | 405.5811 | 0.01965 |
| 120 | Compressed Air | -10 | 0.004 | Run 5 | 359.2857 | 410.5226 | 0.01973 |
| 121 | Compressed Air | -10 | 0.005 | Run 1 | 402.3728 | 459.5607 | 0.02311 |
| 122 | Compressed Air | -10 | 0.005 | Run 2 | 396.068 | 466.8819 | 0.02345 |
| 123 | Compressed Air | -10 | 0.005 | Run 3 | 407.5286 | 474.8292 | 0.02309 |
| 124 | Compressed Air | -10 | 0.005 | Run 4 | 402.6982 | 477.0524 | 0.0237 |
| 125 | Compressed Air | -10 | 0.005 | Run 5 | 399.2012 | 472.631 | 0.02363 |
| 126 | Compressed Air | 0 | 0.001 | Run 1 | 162.9359 | 165.2332 | 0.00768 |


| Run No. | Environment | $\boldsymbol{\alpha}$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 127 | Compressed Air | 0 | 0.001 | Run 2 | 162.1041 | 165.1499 | 0.00737 |
| 128 | Compressed Air | 0 | 0.001 | Run 3 | 162.9914 | 165.581 | 0.00727 |
| 129 | Compressed Air | 0 | 0.001 | Run 4 | 165.6891 | 166.338 | 0.00737 |
| 130 | Compressed Air | 0 | 0.001 | Run 5 | 166.8184 | 168.7141 | 0.00771 |
| 131 | Compressed Air | 0 | 0.002 | Run 1 | 219.5647 | 261.0481 | 0.01325 |
| 132 | Compressed Air | 0 | 0.002 | Run 2 | 213.2506 | 254.2292 | 0.01335 |
| 133 | Compressed Air | 0 | 0.002 | Run 3 | 215.2732 | 254.5406 | 0.01311 |
| 134 | Compressed Air | 0 | 0.002 | Run 4 | 220.1807 | 259.7471 | 0.01298 |
| 135 | Compressed Air | 0 | 0.002 | Run 5 | 213.1102 | 256.4842 | 0.01278 |
| 136 | Compressed Air | 0 | 0.003 | Run 1 | 306.661 | 331.6338 | 0.01537 |
| 137 | Compressed Air | 0 | 0.003 | Run 2 | 304.5306 | 333.9596 | 0.01518 |
| 138 | Compressed Air | 0 | 0.003 | Run 3 | 298.4483 | 337.417 | 0.01564 |
| 139 | Compressed Air | 0 | 0.003 | Run 4 | 309.4737 | 345.7519 | 0.01527 |
| 140 | Compressed Air | 0 | 0.003 | Run 5 | 302.9238 | 342.2661 | 0.01543 |
| 141 | Compressed Air | 0 | 0.004 | Run 1 | 371.3089 | 412.5695 | 0.02037 |
| 142 | Compressed Air | 0 | 0.004 | Run 2 | 379.8773 | 415.9003 | 0.02058 |
| 143 | Compressed Air | 0 | 0.004 | Run 3 | 378.5803 | 417.6269 | 0.01986 |
| 144 | Compressed Air | 0 | 0.004 | Run 4 | 374.1755 | 407.4259 | 0.02045 |
| 145 | Compressed Air | 0 | 0.004 | Run 5 | 377.5255 | 403.7149 | 0.0196 |
| 146 | Compressed Air | 0 | 0.005 | Run 1 | 322.9589 | 463.6449 | 0.02241 |
| 147 | Compressed Air | 0 | 0.005 | Run 2 | 328.9528 | 459.787 | 0.02253 |
| 148 | Compressed Air | 0 | 0.005 | Run 3 | 337.3287 | 459.4949 | 0.02239 |
| 149 | Compressed Air | 0 | 0.005 | Run 4 | 328.9954 | 454.964 | 0.02239 |
| 150 | Compressed Air | 0 | 0.005 | Run 5 | 337.7602 | 463.6962 | 0.02234 |
| 151 | Compressed Air | 15 | 0.001 | Run 1 | 61.5124 | 113.1831 | 0.00548 |
| 152 | Compressed Air | 15 | 0.001 | Run 2 | 63.2416 | 114.0435 | 0.00556 |
| 153 | Compressed Air | 15 | 0.001 | Run 3 | 64.4127 | 116.2906 | 0.00542 |
| 154 | Compressed Air | 15 | 0.001 | Run 4 | 65.1112 | 117.1496 | 0.0053 |
| 155 | Compressed Air | 15 | 0.001 | Run 5 | 66.058 | 117.3281 | 0.00537 |
| 156 | Compressed Air | 15 | 0.002 | Run 1 | 105.2246 | 197.447 | 0.00976 |
| 157 | Compressed Air | 15 | 0.002 | Run 2 | 104.2617 | 190.4033 | 0.01001 |
| 158 | Compressed Air | 15 | 0.002 | Run 3 | 112.199 | 195.5409 | 0.00965 |
| 159 | Compressed Air | 15 | 0.002 | Run 4 | 114.3065 | 199.6868 | 0.00969 |
| 160 | Compressed Air | 15 | 0.002 | Run 5 | 119.2931 | 200.8401 | 0.00975 |
| 161 | Compressed Air | 15 | 0.003 | Run 1 | 134.4895 | 254.2782 | 0.0138 |
| 162 | Compressed Air | 15 | 0.003 | Run 2 | 143.1355 | 265.2779 | 0.01368 |
| 163 | Compressed Air | 15 | 0.003 | Run 3 | 142.515 | 265.0369 | 0.01354 |
| 164 | Compressed Air | 15 | 0.003 | Run 4 | 144.0262 | 265.7019 | 0.0135 |
| 165 | Compressed Air | 15 | 0.003 | Run 5 | 145.1991 | 268.8831 | 0.01379 |
| 166 | Compressed Air | 15 | 0.004 | Run 1 | 167.0502 | 323.9666 | 0.01654 |
| 167 | Compressed Air | 15 | 0.004 | Run 2 | 163.5994 | 323.5697 | 0.01638 |
| 168 | Compressed Air | 15 | 0.004 | Run 3 | 165.446 | 323.5697 | 0.01631 |
| 169 | Compressed Air | 15 | 0.004 | Run 4 | 172.0612 | 329.7176 | 0.01671 |
| 170 | Compressed Air | 15 | 0.004 | Run 5 | 167.4072 | 326.1765 | 0.01645 |
| 171 | Compressed Air | 15 | 0.005 | Run 1 | 159.3689 | 363.3295 | 0.01976 |
| 172 | Compressed Air | 15 | 0.005 | Run 2 | 167.9498 | 372.6552 | 0.01953 |
| 173 | Compressed Air | 15 | 0.005 | Run 3 | 169.5887 | 372.6489 | 0.01964 |


| Run No. | Environment | $\boldsymbol{\alpha}$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 174 | Compressed Air | 15 | 0.005 | Run 4 | 167.1795 | 376.4682 | 0.01979 |
| 175 | Compressed Air | 15 | 0.005 | Run 5 | 170.1 | 375.4764 | 0.01981 |
| 176 | Compressed Air | 30 | 0.001 | Run 1 | 29.9759 | 89.3659 | 0.00359 |
| 177 | Compressed Air | 30 | 0.001 | Run 2 | 33.7425 | 91.2695 | 0.00387 |
| 178 | Compressed Air | 30 | 0.001 | Run 3 | 32.2379 | 95.873 | 0.00374 |
| 179 | Compressed Air | 30 | 0.001 | Run 4 | 35.996 | 95.9412 | 0.00373 |
| 180 | Compressed Air | 30 | 0.001 | Run 5 | 38.689 | 94.1467 | 0.00381 |
| 181 | Compressed Air | 30 | 0.002 | Run 1 | 44.4358 | 149.7706 | 0.00755 |
| 182 | Compressed Air | 30 | 0.002 | Run 2 | 47.7565 | 152.4468 | 0.00754 |
| 183 | Compressed Air | 30 | 0.002 | Run 3 | 50.2597 | 155.6077 | 0.00705 |
| 184 | Compressed Air | 30 | 0.002 | Run 4 | 50.2975 | 155.8898 | 0.00742 |
| 185 | Compressed Air | 30 | 0.002 | Run 5 | 51.8714 | 156.5935 | 0.00704 |
| 186 | Compressed Air | 30 | 0.003 | Run 1 | 63.5885 | 215.6585 | 0.00967 |
| 187 | Compressed Air | 30 | 0.003 | Run 2 | 61.2472 | 210.745 | 0.00965 |
| 188 | Compressed Air | 30 | 0.003 | Run 3 | 64.6666 | 211.8868 | 0.00977 |
| 189 | Compressed Air | 30 | 0.003 | Run 4 | 69.2517 | 216.0162 | 0.0097 |
| 190 | Compressed Air | 30 | 0.003 | Run 5 | 70.628 | 217.1014 | 0.00964 |
| 191 | Compressed Air | 30 | 0.004 | Run 1 | 92.6672 | 285.7289 | 0.01352 |
| 192 | Compressed Air | 30 | 0.004 | Run 2 | 88.1638 | 279.4771 | 0.01333 |
| 193 | Compressed Air | 30 | 0.004 | Run 3 | 86.1354 | 277.423 | 0.01349 |
| 194 | Compressed Air | 30 | 0.004 | Run 4 | 86.2464 | 281.964 | 0.01342 |
| 195 | Compressed Air | 30 | 0.004 | Run 5 | 91.2761 | 287.9853 | 0.01348 |
| 196 | Compressed Air | 30 | 0.005 | Run 1 | 109.3864 | 328.9997 | 0.01762 |
| 197 | Compressed Air | 30 | 0.005 | Run 2 | 107.6019 | 325.5716 | 0.01754 |
| 198 | Compressed Air | 30 | 0.005 | Run 3 | 108.0435 | 331.8501 | 0.01757 |
| 199 | Compressed Air | 30 | 0.005 | Run 4 | 112.4562 | 336.0007 | 0.01767 |
| 200 | Compressed Air | 30 | 0.005 | Run 5 | 102.807 | 322.619 | 0.01777 |
| 201 | Nitrogen | -10 | 0.001 | Run 1 | 206.6564 | 195.5815 | 0.00968 |
| 202 | Nitrogen | -10 | 0.001 | Run 2 | 207.1426 | 192.6893 | 0.0095 |
| 203 | Nitrogen | -10 | 0.001 | Run 3 | 202.68 | 194.1392 | 0.00924 |
| 204 | Nitrogen | -10 | 0.001 | Run 4 | 217.7624 | 200.6148 | 0.00938 |
| 205 | Nitrogen | -10 | 0.001 | Run 5 | 214.5732 | 198.1373 | 0.00967 |
| 206 | Nitrogen | -10 | 0.002 | Run 1 | 287.6712 | 281.1819 | 0.01354 |
| 207 | Nitrogen | -10 | 0.002 | Run 2 | 287.13 | 282.1961 | 0.01346 |
| 208 | Nitrogen | -10 | 0.002 | Run 3 | 292.2072 | 285.1416 | 0.01364 |
| 209 | Nitrogen | -10 | 0.002 | Run 4 | 284.7899 | 279.5205 | 0.01352 |
| 210 | Nitrogen | -10 | 0.002 | Run 5 | 289.2702 | 279.558 | 0.01318 |
| 211 | Nitrogen | -10 | 0.003 | Run 1 | 383.9224 | 395.708 | 0.01845 |
| 212 | Nitrogen | -10 | 0.003 | Run 2 | 373.3497 | 398.0761 | 0.01843 |
| 213 | Nitrogen | -10 | 0.003 | Run 3 | 382.5961 | 385.8474 | 0.01838 |
| 214 | Nitrogen | -10 | 0.003 | Run 4 | 382.5391 | 391.1423 | 0.01855 |
| 215 | Nitrogen | -10 | 0.003 | Run 5 | 379.7901 | 396.6776 | 0.01825 |
| 216 | Nitrogen | -10 | 0.004 | Run 1 | 368.9621 | 439.3335 | 0.0205 |
| 217 | Nitrogen | -10 | 0.004 | Run 2 | 373.8964 | 424.6515 | 0.02083 |
| 218 | Nitrogen | -10 | 0.004 | Run 3 | 381.3443 | 437.8459 | 0.02043 |
| 219 | Nitrogen | -10 | 0.004 | Run 4 | 390.1037 | 439.4337 | 0.02089 |
| 220 | Nitrogen | -10 | 0.004 | Run 5 | 377.0451 | 433.2095 | 0.02045 |


| Run No. | Environment | $\boldsymbol{\alpha}$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 221 | Nitrogen | -10 | 0.005 | Run 1 | 395.6619 | 495.5847 | 0.02189 |
| 222 | Nitrogen | -10 | 0.005 | Run 2 | 373.1608 | 478.6916 | 0.02219 |
| 223 | Nitrogen | -10 | 0.005 | Run 3 | 378.8455 | 472.3057 | 0.02183 |
| 224 | Nitrogen | -10 | 0.005 | Run 4 | 382.9149 | 474.1717 | 0.02223 |
| 225 | Nitrogen | -10 | 0.005 | Run 5 | 392.4226 | 487.8136 | 0.02217 |
| 226 | Nitrogen | 0 | 0.001 | Run 1 | 164.5504 | 184.5599 | 0.00813 |
| 227 | Nitrogen | 0 | 0.001 | Run 2 | 163.1026 | 182.9984 | 0.00817 |
| 228 | Nitrogen | 0 | 0.001 | Run 3 | 159.9201 | 178.6047 | 0.00812 |
| 229 | Nitrogen | 0 | 0.001 | Run 4 | 161.9422 | 182.6511 | 0.00825 |
| 230 | Nitrogen | 0 | 0.001 | Run 5 | 163.0827 | 181.1829 | 0.00806 |
| 231 | Nitrogen | 0 | 0.002 | Run 1 | 233.1829 | 271.1694 | 0.01107 |
| 232 | Nitrogen | 0 | 0.002 | Run 2 | 234.9983 | 266.0591 | 0.01385 |
| 233 | Nitrogen | 0 | 0.002 | Run 3 | 242.5081 | 275.9159 | 0.01366 |
| 234 | Nitrogen | 0 | 0.002 | Run 4 | 236.4188 | 270.1852 | 0.01361 |
| 235 | Nitrogen | 0 | 0.002 | Run 5 | 237.9905 | 274.003 | 0.01357 |
| 236 | Nitrogen | 0 | 0.003 | Run 1 | 279.5769 | 346.4283 | 0.01688 |
| 237 | Nitrogen | 0 | 0.003 | Run 2 | 279.0627 | 343.8411 | 0.01675 |
| 238 | Nitrogen | 0 | 0.003 | Run 3 | 281.6154 | 342.3731 | 0.01656 |
| 239 | Nitrogen | 0 | 0.003 | Run 4 | 275.8128 | 342.3738 | 0.01689 |
| 240 | Nitrogen | 0 | 0.003 | Run 5 | 279.2154 | 342.2708 | 0.01653 |
| 241 | Nitrogen | 0 | 0.004 | Run 1 | 334.6459 | 425.5195 | 0.01958 |
| 242 | Nitrogen | 0 | 0.004 | Run 2 | 331.8301 | 416.7075 | 0.01971 |
| 243 | Nitrogen | 0 | 0.004 | Run 3 | 335.0354 | 424.1981 | 0.01964 |
| 244 | Nitrogen | 0 | 0.004 | Run 4 | 328.8234 | 420.35 | 0.01964 |
| 245 | Nitrogen | 0 | 0.004 | Run 5 | 326.9944 | 424.9836 | 0.0197 |
| 246 | Nitrogen | 0 | 0.005 | Run 1 | 430.5991 | 484.6631 | 0.02352 |
| 247 | Nitrogen | 0 | 0.005 | Run 2 | 427.0402 | 488.0082 | 0.02404 |
| 248 | Nitrogen | 0 | 0.005 | Run 3 | 417.6366 | 483.0138 | 0.02342 |
| 249 | Nitrogen | 0 | 0.005 | Run 4 | 424.0487 | 490.4496 | 0.02468 |
| 250 | Nitrogen | 0 | 0.005 | Run 5 | 417.0269 | 487.2506 | 0.02383 |
| 251 | Nitrogen | 15 | 0.001 | Run 1 | 78.6877 | 132.4233 | 0.00646 |
| 252 | Nitrogen | 15 | 0.001 | Run 2 | 77.7225 | 130.8423 | 0.00596 |
| 253 | Nitrogen | 15 | 0.001 | Run 3 | 78.8442 | 129.2723 | 0.00632 |
| 254 | Nitrogen | 15 | 0.001 | Run 4 | 76.9546 | 133.4419 | 0.00612 |
| 255 | Nitrogen | 15 | 0.001 | Run 5 | 77.8638 | 129.4782 | 0.00641 |
| 256 | Nitrogen | 15 | 0.002 | Run 1 | 150.1096 | 221.7002 | 0.01123 |
| 257 | Nitrogen | 15 | 0.002 | Run 2 | 152.0043 | 220.2428 | 0.01148 |
| 258 | Nitrogen | 15 | 0.002 | Run 3 | 156.324 | 228.9791 | 0.01119 |
| 259 | Nitrogen | 15 | 0.002 | Run 4 | 149.3831 | 219.0391 | 0.01152 |
| 260 | Nitrogen | 15 | 0.002 | Run 5 | 149.2316 | 219.1011 | 0.01164 |
| 261 | Nitrogen | 15 | 0.003 | Run 1 | 167.8966 | 291.6661 | 0.01467 |
| 262 | Nitrogen | 15 | 0.003 | Run 2 | 163.8237 | 284.3597 | 0.01483 |
| 263 | Nitrogen | 15 | 0.003 | Run 3 | 166.1155 | 286.7002 | 0.01511 |
| 264 | Nitrogen | 15 | 0.003 | Run 4 | 169.8913 | 290.2186 | 0.01501 |
| 265 | Nitrogen | 15 | 0.003 | Run 5 | 170.3016 | 295.5275 | 0.01529 |
| 266 | Nitrogen | 15 | 0.004 | Run 1 | 241.7012 | 380.6288 | 0.02117 |
| 267 | Nitrogen | 15 | 0.004 | Run 2 | 243.4664 | 381.1891 | 0.02134 |


| Run No. | Environment | $\boldsymbol{\alpha}$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 268 | Nitrogen | 15 | 0.004 | Run 3 | 236.7358 | 376.3736 | 0.02151 |
| 269 | Nitrogen | 15 | 0.004 | Run 4 | 240.0703 | 388.8308 | 0.02168 |
| 270 | Nitrogen | 15 | 0.004 | Run 5 | 247.0985 | 389.9095 | 0.02121 |
| 271 | Nitrogen | 15 | 0.005 | Run 1 | 223.7015 | 430.0145 | 0.02171 |
| 272 | Nitrogen | 15 | 0.005 | Run 2 | 222.2084 | 427.8287 | 0.02216 |
| 273 | Nitrogen | 15 | 0.005 | Run 3 | 229.9665 | 428.6029 | 0.02209 |
| 274 | Nitrogen | 15 | 0.005 | Run 4 | 230.929 | 429.1843 | 0.02194 |
| 275 | Nitrogen | 15 | 0.005 | Run 5 | 233.4081 | 433.5332 | 0.02206 |
| 276 | Nitrogen | 30 | 0.001 | Run 1 | 34.2568 | 91.7117 | 0.00406 |
| 277 | Nitrogen | 30 | 0.001 | Run 2 | 34.379 | 93.6644 | 0.00414 |
| 278 | Nitrogen | 30 | 0.001 | Run 3 | 36.4733 | 95.4205 | 0.00396 |
| 279 | Nitrogen | 30 | 0.001 | Run 4 | 37.0401 | 96.0515 | 0.00403 |
| 280 | Nitrogen | 30 | 0.001 | Run 5 | 31.39 | 92.8399 | 0.00367 |
| 281 | Nitrogen | 30 | 0.002 | Run 1 | 57.6798 | 158.8456 | 0.00755 |
| 282 | Nitrogen | 30 | 0.002 | Run 2 | 58.8684 | 169.1589 | 0.00755 |
| 283 | Nitrogen | 30 | 0.002 | Run 3 | 64.8787 | 166.0229 | 0.00761 |
| 284 | Nitrogen | 30 | 0.002 | Run 4 | 64.8416 | 167.4373 | 0.00754 |
| 285 | Nitrogen | 30 | 0.002 | Run 5 | 54.8339 | 171.6381 | 0.00753 |
| 286 | Nitrogen | 30 | 0.003 | Run 1 | 70.0972 | 213.5992 | 0.01228 |
| 287 | Nitrogen | 30 | 0.003 | Run 2 | 74.4158 | 219.5313 | 0.01212 |
| 288 | Nitrogen | 30 | 0.003 | Run 3 | 76.2422 | 218.8497 | 0.01257 |
| 289 | Nitrogen | 30 | 0.003 | Run 4 | 74.3471 | 217.4577 | 0.01227 |
| 290 | Nitrogen | 30 | 0.003 | Run 5 | 83.6924 | 224.6447 | 0.01268 |
| 291 | Nitrogen | 30 | 0.004 | Run 1 | 76.5872 | 261.6407 | 0.01532 |
| 292 | Nitrogen | 30 | 0.004 | Run 2 | 76.7912 | 262.8484 | 0.01655 |
| 293 | Nitrogen | 30 | 0.004 | Run 3 | 82.3925 | 270.9511 | 0.01568 |
| 294 | Nitrogen | 30 | 0.004 | Run 4 | 85.1815 | 271.8372 | 0.0167 |
| 295 | Nitrogen | 30 | 0.004 | Run 5 | 83.8936 | 269.3505 | 0.01676 |
| 296 | Nitrogen | 30 | 0.005 | Run 1 | 195.738 | 376.7756 | 0.01659 |
| 297 | Nitrogen | 30 | 0.005 | Run 2 | 191.2584 | 369.0897 | 0.01658 |
| 298 | Nitrogen | 30 | 0.005 | Run 3 | 198.9184 | 369.0897 | 0.01651 |
| 299 | Nitrogen | 30 | 0.005 | Run 4 | 197.3296 | 364.3208 | 0.01687 |
| 300 | Nitrogen | 30 | 0.005 | Run 5 | 186.2928 | 369.2408 | 0.01652 |
| 301 | Cool Mist | -10 | 0.001 | Run 1 | 195.7094 | 196.7856 | 0.00929 |
| 302 | Cool Mist | -10 | 0.001 | Run 2 | 196.3354 | 192.175 | 0.00955 |
| 303 | Cool Mist | -10 | 0.001 | Run 3 | 204.0934 | 201.2071 | 0.00931 |
| 304 | Cool Mist | -10 | 0.001 | Run 4 | 201.2784 | 193.76 | 0.00956 |
| 305 | Cool Mist | -10 | 0.001 | Run 5 | 208.4875 | 202.2933 | 0.00952 |
| 306 | Cool Mist | -10 | 0.002 | Run 1 | 297.3487 | 290.4151 | 0.01465 |
| 307 | Cool Mist | -10 | 0.002 | Run 2 | 300.1617 | 291.3465 | 0.01463 |
| 308 | Cool Mist | -10 | 0.002 | Run 3 | 289.5194 | 286.3318 | 0.01472 |
| 309 | Cool Mist | -10 | 0.002 | Run 4 | 289.8274 | 286.5597 | 0.01462 |
| 310 | Cool Mist | -10 | 0.002 | Run 5 | 287.2581 | 293.0959 | 0.01475 |
| 311 | Cool Mist | -10 | 0.003 | Run 1 | 359.714 | 375.0335 | 0.01655 |
| 312 | Cool Mist | -10 | 0.003 | Run 2 | 359.7902 | 373.8692 | 0.01676 |
| 313 | Cool Mist | -10 | 0.003 | Run 3 | 349.0415 | 367.1384 | 0.01673 |
| 314 | Cool Mist | -10 | 0.003 | Run 4 | 356.6663 | 364.5413 | 0.01685 |


| Run No. | Environment | $\boldsymbol{\alpha}$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 315 | Cool Mist | -10 | 0.003 | Run 5 | 349.8105 | 362.813 | 0.01679 |
| 316 | Cool Mist | -10 | 0.004 | Run 1 | 375.2386 | 428.8634 | 0.0223 |
| 317 | Cool Mist | -10 | 0.004 | Run 2 | 386.0774 | 429.459 | 0.02259 |
| 318 | Cool Mist | -10 | 0.004 | Run 3 | 373.0587 | 428.976 | 0.02229 |
| 319 | Cool Mist | -10 | 0.004 | Run 4 | 374.3297 | 435.5474 | 0.02246 |
| 320 | Cool Mist | -10 | 0.004 | Run 5 | 376.0092 | 429.0622 | 0.02241 |
| 321 | Cool Mist | -10 | 0.005 | Run 1 | 483.7339 | 534.68 | 0.02549 |
| 322 | Cool Mist | -10 | 0.005 | Run 2 | 490.7619 | 544.2519 | 0.02545 |
| 323 | Cool Mist | -10 | 0.005 | Run 3 | 491.3546 | 544.1311 | 0.02561 |
| 324 | Cool Mist | -10 | 0.005 | Run 4 | 491.4266 | 546.3741 | 0.02552 |
| 325 | Cool Mist | -10 | 0.005 | Run 5 | 491.3052 | 547.4965 | 0.02548 |
| 326 | Cool Mist | 0 | 0.001 | Run 1 | 152.4772 | 175.133 | 0.0075 |
| 327 | Cool Mist | 0 | 0.001 | Run 2 | 152.2068 | 180.9133 | 0.00764 |
| 328 | Cool Mist | 0 | 0.001 | Run 3 | 156.0352 | 179.9308 | 0.00743 |
| 329 | Cool Mist | 0 | 0.001 | Run 4 | 158.5667 | 179.1254 | 0.00756 |
| 330 | Cool Mist | 0 | 0.001 | Run 5 | 156.9991 | 176.181 | 0.00763 |
| 331 | Cool Mist | 0 | 0.002 | Run 1 | 247.4289 | 279.3266 | 0.0135 |
| 332 | Cool Mist | 0 | 0.002 | Run 2 | 243.5632 | 275.3585 | 0.0136 |
| 333 | Cool Mist | 0 | 0.002 | Run 3 | 246.5875 | 278.1679 | 0.01361 |
| 334 | Cool Mist | 0 | 0.002 | Run 4 | 252.9061 | 282.2953 | 0.01338 |
| 335 | Cool Mist | 0 | 0.002 | Run 5 | 252.7687 | 284.098 | 0.01361 |
| 336 | Cool Mist | 0 | 0.003 | Run 1 | 307.5088 | 364.4924 | 0.01765 |
| 337 | Cool Mist | 0 | 0.003 | Run 2 | 304.3039 | 358.126 | 0.01779 |
| 338 | Cool Mist | 0 | 0.003 | Run 3 | 299.7853 | 355.6117 | 0.01761 |
| 339 | Cool Mist | 0 | 0.003 | Run 4 | 298.1503 | 356.1509 | 0.01764 |
| 340 | Cool Mist | 0 | 0.003 | Run 5 | 306.4602 | 362.9809 | 0.01773 |
| 341 | Cool Mist | 0 | 0.004 | Run 1 | 335.8497 | 421.2274 | 0.0214 |
| 342 | Cool Mist | 0 | 0.004 | Run 2 | 335.8612 | 418.2116 | 0.02153 |
| 343 | Cool Mist | 0 | 0.004 | Run 3 | 334.4233 | 418.9726 | 0.02152 |
| 344 | Cool Mist | 0 | 0.004 | Run 4 | 338.8065 | 422.3275 | 0.0217 |
| 345 | Cool Mist | 0 | 0.004 | Run 5 | 338.8065 | 422.8405 | 0.02106 |
| 346 | Cool Mist | 0 | 0.005 | Run 1 | 462.9319 | 556.5036 | 0.02455 |
| 347 | Cool Mist | 0 | 0.005 | Run 2 | 463.8574 | 554.134 | 0.02461 |
| 348 | Cool Mist | 0 | 0.005 | Run 3 | 461.594 | 546.7876 | 0.02471 |
| 349 | Cool Mist | 0 | 0.005 | Run 4 | 456.2306 | 559.0695 | 0.02474 |
| 350 | Cool Mist | 0 | 0.005 | Run 5 | 454.8527 | 541.429 | 0.02464 |
| 351 | Cool Mist | 15 | 0.001 | Run 1 | 61.4443 | 117.727 | 0.00528 |
| 352 | Cool Mist | 15 | 0.001 | Run 2 | 61.1567 | 117.5025 | 0.00547 |
| 353 | Cool Mist | 15 | 0.001 | Run 3 | 62.3705 | 120.783 | 0.00518 |
| 354 | Cool Mist | 15 | 0.001 | Run 4 | 63.5301 | 120.5455 | 0.00548 |
| 355 | Cool Mist | 15 | 0.001 | Run 5 | 64.199 | 121.12 | 0.00558 |
| 356 | Cool Mist | 15 | 0.002 | Run 1 | 85.1025 | 187.8264 | 0.00956 |
| 357 | Cool Mist | 15 | 0.002 | Run 2 | 86.1069 | 189.8 | 0.00932 |
| 358 | Cool Mist | 15 | 0.002 | Run 3 | 86.883 | 189.432 | 0.00938 |
| 359 | Cool Mist | 15 | 0.002 | Run 4 | 82.936 | 185.5118 | 0.00963 |
| 360 | Cool Mist | 15 | 0.002 | Run 5 | 82.9105 | 185.8108 | 0.00946 |
| 361 | Cool Mist | 15 | 0.003 | Run 1 | 153.7815 | 277.4535 | 0.01353 |


| Run No. | Environment | $\boldsymbol{\alpha}$ | Feed | Run | Ft | Fc | tc |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 362 | Cool Mist | 15 | 0.003 | Run 2 | 151.4303 | 274.1256 | 0.01328 |
| 363 | Cool Mist | 15 | 0.003 | Run 3 | 156.5936 | 276.4732 | 0.0136 |
| 364 | Cool Mist | 15 | 0.003 | Run 4 | 157.1355 | 277.2494 | 0.01309 |
| 365 | Cool Mist | 15 | 0.003 | Run 5 | 159.999 | 279.3632 | 0.01303 |
| 366 | Cool Mist | 15 | 0.004 | Run 1 | 187.335 | 341.0167 | 0.01809 |
| 367 | Cool Mist | 15 | 0.004 | Run 2 | 181.2863 | 342.5107 | 0.01822 |
| 368 | Cool Mist | 15 | 0.004 | Run 3 | 188.967 | 347.3744 | 0.01788 |
| 369 | Cool Mist | 15 | 0.004 | Run 4 | 181.3638 | 342.7891 | 0.01809 |
| 370 | Cool Mist | 15 | 0.004 | Run 5 | 186.9441 | 347.3383 | 0.01775 |
| 371 | Cool Mist | 15 | 0.005 | Run 1 | 202.7457 | 419.7883 | 0.0236 |
| 372 | Cool Mist | 15 | 0.005 | Run 2 | 209.5801 | 414.2354 | 0.02362 |
| 373 | Cool Mist | 15 | 0.005 | Run 3 | 209.4235 | 415.6389 | 0.02341 |
| 374 | Cool Mist | 15 | 0.005 | Run 4 | 211.2018 | 416.244 | 0.02326 |
| 375 | Cool Mist | 15 | 0.005 | Run 5 | 212.4995 | 423.9621 | 0.02362 |
| 376 | Cool Mist | 30 | 0.001 | Run 1 | 51.8232 | 111.6602 | 0.00384 |
| 377 | Cool Mist | 30 | 0.001 | Run 2 | 50.7544 | 109.552 | 0.00388 |
| 378 | Cool Mist | 30 | 0.001 | Run 3 | 51.1189 | 112.6215 | 0.00383 |
| 379 | Cool Mist | 30 | 0.001 | Run 4 | 49.955 | 108.7509 | 0.00388 |
| 380 | Cool Mist | 30 | 0.001 | Run 5 | 50.6559 | 110.5263 | 0.00382 |
| 381 | Cool Mist | 30 | 0.002 | Run 1 | 55.3825 | 166.1258 | 0.007 |
| 382 | Cool Mist | 30 | 0.002 | Run 2 | 57.7285 | 169.0374 | 0.00692 |
| 383 | Cool Mist | 30 | 0.002 | Run 3 | 45.0762 | 158.2031 | 0.00705 |
| 384 | Cool Mist | 30 | 0.002 | Run 4 | 47.4462 | 161.4845 | 0.007 |
| 385 | Cool Mist | 30 | 0.002 | Run 5 | 46.0538 | 157.6917 | 0.00701 |
| 386 | Cool Mist | 30 | 0.003 | Run 1 | 60.3193 | 218.0873 | 0.01036 |
| 387 | Cool Mist | 30 | 0.003 | Run 2 | 63.5088 | 220.3345 | 0.01041 |
| 388 | Cool Mist | 30 | 0.003 | Run 3 | 66.2184 | 223.8298 | 0.01045 |
| 389 | Cool Mist | 30 | 0.003 | Run 4 | 67.4257 | 224.4799 | 0.01022 |
| 390 | Cool Mist | 30 | 0.003 | Run 5 | 69.5599 | 224.3973 | 0.01055 |
| 391 | Cool Mist | 30 | 0.004 | Run 1 | 189.3965 | 327.3907 | 0.01382 |
| 392 | Cool Mist | 30 | 0.004 | Run 2 | 183.8052 | 324.5705 | 0.01378 |
| 393 | Cool Mist | 30 | 0.004 | Run 3 | 187.4379 | 329.6599 | 0.01391 |
| 394 | Cool Mist | 30 | 0.004 | Run 4 | 193.1028 | 328.3061 | 0.01384 |
| 395 | Cool Mist | 30 | 0.004 | Run 5 | 187.2169 | 329.0382 | 0.01342 |
| 396 | Cool Mist | 30 | 0.005 | Run 1 | 103.1147 | 345.305 | 0.01649 |
| 397 | Cool Mist | 30 | 0.005 | Run 2 | 101.9503 | 346.1842 | 0.01632 |
| 398 | Cool Mist | 30 | 0.005 | Run 3 | 94.5451 | 333.1663 | 0.01572 |
| 399 | Cool Mist | 30 | 0.005 | Run 4 | 95.4506 | 334.7357 | 0.01666 |
| 400 | Cool Mist | 30 | 0.005 | Run 5 | 97.1873 | 341.0194 | 0.01643 |

## APPENDIX D

The classical metal cutting equations generally used in the study of the mechanics are as given below.

Chip Thickness ratio, $r_{c}=\frac{t}{t_{c}}$
Onset of Shear Plane Angle, $\phi=\tan ^{-1}\left[\frac{r_{c} \times \cos \alpha}{1-r_{c} \times \sin \alpha}\right]$

Friction Force, $F=F_{c} \times \sin \alpha+F_{t} \times \cos \alpha$

Normal Force, $N=F_{c} \times \cos \alpha+F_{t} \times \sin \alpha$
Friction Co-efficient, $\mu=\frac{F}{N}$

Resultant Force, $R=\sqrt{F_{c}{ }^{2}+F_{t}{ }^{2}}$
Friction Angle, $\beta=\tan ^{-1}\left[\frac{F}{N}\right]$
Shear Force along the onset of Shear Plane, $F_{s}=F_{c} \times \cos \phi-F_{t} \times \sin \phi$

Normal Force along the onset of Shear Plane, $F_{n}=F_{c} \times \sin \phi-F_{t} \times \cos \phi$
Shear Area, $A_{s}=\frac{t \times w}{\sin \phi}$

Shear Stress, $\tau_{s}=\frac{F_{s}}{A_{s}}=\frac{F_{s} \times \sin \phi}{t \times w}$

Horse Power, $H P=\frac{F_{c} \times V}{33,000}$
Material removal Rate, $M R R=\frac{\pi\left(D^{2}-D_{1}^{2}\right)}{4} \times t \times w$
Specific Horse Power, $H P_{s}=\frac{H P}{M R R}$
Root Mean Square Deviation, $R q=\sqrt{\frac{z_{1}^{2}+z_{2}^{2}+z_{3}^{2} \ldots \ldots \ldots . z_{n}^{2}}{n}}$

$$
\Delta R_{q}=\left(R_{q}\right)_{\text {new }}-\left(R_{q}\right)_{\text {used }}
$$

## APPENDIX E

The Force Ratios calculated from the classical Metal Cutting equations using the raw data obtained from the experiments are tablulated below.

| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 144.4904 | 204.1855 | 0.7076 | 154.0374 | 197.0830 | 0.7816 |
| 2 | 184.1773 | 177.2929 | 1.0388 | 177.2929 | 184.1773 | 0.9626 |
| 3 | 177.9254 | 180.9517 | 0.9833 | 180.9517 | 177.9254 | 1.0170 |
| 4 | 189.0791 | 181.1614 | 1.0437 | 181.1614 | 189.0791 | 0.9581 |
| 5 | 194.356 | 185.0437 | 1.0503 | 185.0437 | 194.3560 | 0.9521 |
| 6 | 202.2132 | 303.195 | 0.6669 | 221.6816 | 289.2657 | 0.7664 |
| 7 | 257.8228 | 268.7747 | 0.9593 | 268.7747 | 257.8228 | 1.0425 |
| 8 | 258.6709 | 267.5613 | 0.9668 | 267.5613 | 258.6709 | 1.0344 |
| 9 | 262.6206 | 272.2441 | 0.9647 | 272.2441 | 262.6206 | 1.0366 |
| 10 | 264.2924 | 277.1065 | 0.9538 | 277.1065 | 264.2924 | 1.0485 |
| 11 | 247.4001 | 383.9302 | 0.6444 | 280.5633 | 360.4074 | 0.7785 |
| 12 | 327.1769 | 341.8487 | 0.9571 | 341.8487 | 327.1769 | 1.0448 |
| 13 | 304.3356 | 340.2505 | 0.8944 | 340.2505 | 304.3356 | 1.1180 |
| 14 | 313.9446 | 347.0742 | 0.9045 | 347.0742 | 313.9446 | 1.1055 |
| 15 | 301.7063 | 335.4178 | 0.8995 | 335.4178 | 301.7063 | 1.1117 |
| 16 | 279.3057 | 467.9808 | 0.5968 | 341.5569 | 424.6841 | 0.8043 |
| 17 | 350.0089 | 402.2674 | 0.8701 | 402.2674 | 350.0089 | 1.1493 |
| 18 | 370.2052 | 419.0703 | 0.8834 | 419.0703 | 370.2052 | 1.1320 |
| 19 | 364.9769 | 409.6705 | 0.8909 | 409.6705 | 364.9769 | 1.1225 |
| 20 | 375.6279 | 424.4903 | 0.8849 | 424.4903 | 375.6279 | 1.1301 |
| 21 | 318.5673 | 538.191 | 0.5919 | 387.0387 | 491.2592 | 0.7879 |
| 22 | 410.9808 | 475.7449 | 0.8639 | 475.7449 | 410.9808 | 1.1576 |
| 23 | 404.456 | 467.8064 | 0.8646 | 467.8064 | 404.4560 | 1.1566 |
| 24 | 415.8704 | 479.9004 | 0.8666 | 479.9004 | 415.8704 | 1.1540 |
| 25 | 416.2005 | 483.9898 | 0.8599 | 483.9898 | 416.2005 | 1.1629 |
| 26 | 178.7172 | 172.4828 | 1.0361 | 142.8156 | 203.2089 | 0.7028 |
| 27 | 175.5777 | 171.1007 | 1.0262 | 171.1007 | 175.5777 | 0.9745 |
| 28 | 175.7445 | 174.1149 | 1.0094 | 174.1149 | 175.7445 | 0.9907 |
| 29 | 173.5154 | 170.2533 | 1.0192 | 170.2533 | 173.5154 | 0.9812 |
| 30 | 170.9717 | 172.3044 | 0.9923 | 172.3044 | 170.9717 | 1.0078 |
| 31 | 223.7989 | 255.7188 | 0.8752 | 213.049 | 264.7417 | 0.8047 |
| 32 | 218.0048 | 250.2855 | 0.871 | 250.2855 | 218.0048 | 1.1481 |


| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 33 | 219.3895 | 254.1104 | 0.8634 | 254.1104 | 219.3895 | 1.1583 |
| 34 | 226.1762 | 264.9091 | 0.8538 | 264.9091 | 226.1762 | 1.1713 |
| 35 | 220.2374 | 255.4329 | 0.8622 | 255.4329 | 220.2374 | 1.1598 |
| 36 | 293.5401 | 323.8849 | 0.9063 | 254.7618 | 355.1952 | 0.7172 |
| 37 | 304.5111 | 329.6172 | 0.9238 | 329.6172 | 304.5111 | 1.0824 |
| 38 | 297.467 | 329.553 | 0.9026 | 329.553 | 297.4670 | 1.1079 |
| 39 | 292.9392 | 325.1263 | 0.901 | 325.1263 | 292.9392 | 1.1099 |
| 40 | 292.05 | 323.1182 | 0.9038 | 323.1182 | 292.0500 | 1.1064 |
| 41 | 360.526 | 414.8286 | 0.8691 | 324.5147 | 443.5673 | 0.7316 |
| 42 | 363.5965 | 399.0163 | 0.9112 | 399.0163 | 363.5965 | 1.0974 |
| 43 | 377.5881 | 399.5048 | 0.9451 | 399.5048 | 377.5881 | 1.0580 |
| 44 | 361.6405 | 411.0423 | 0.8798 | 411.0423 | 361.6405 | 1.1366 |
| 45 | 373.5652 | 403.9943 | 0.9247 | 403.9943 | 373.5652 | 1.0815 |
| 46 | 319.7004 | 460.565 | 0.6941 | 383.5295 | 408.9421 | 0.9379 |
| 47 | 327.1955 | 450.0505 | 0.727 | 450.0505 | 327.1955 | 1.3755 |
| 48 | 327.1843 | 459.6015 | 0.7119 | 459.6015 | 327.1843 | 1.4047 |
| 49 | 329.8673 | 448.3882 | 0.7357 | 448.3882 | 329.8673 | 1.3593 |
| 50 | 323.936 | 458.4112 | 0.7066 | 458.4112 | 323.9360 | 1.4151 |
| 51 | 89.9852 | 108.312 | 0.8308 | 114.9185 | 81.3790 | 1.4121 |
| 52 | 65.4667 | 120.879 | 0.5416 | 120.879 | 65.4667 | 1.8464 |
| 53 | 69.0838 | 114.2018 | 0.6049 | 114.2018 | 69.0838 | 1.6531 |
| 54 | 66.4581 | 122.6205 | 0.542 | 122.6205 | 66.4581 | 1.8451 |
| 55 | 66.4237 | 120.155 | 0.5528 | 120.155 | 66.4237 | 1.8089 |
| 56 | 156.0384 | 167.2594 | 0.9329 | 177.9194 | 143.7650 | 1.2376 |
| 57 | 113.0798 | 200.5681 | 0.5638 | 200.5681 | 113.0798 | 1.7737 |
| 58 | 114.3104 | 199.1714 | 0.5739 | 199.1714 | 114.3104 | 1.7424 |
| 59 | 118.0056 | 204.2604 | 0.5777 | 204.2604 | 118.0056 | 1.7309 |
| 60 | 118.1204 | 201.6331 | 0.5858 | 201.6331 | 118.1204 | 1.7070 |
| 61 | 194.5472 | 218.2454 | 0.8914 | 228.55 | 182.3310 | 1.2535 |
| 62 | 142.362 | 262.1011 | 0.5432 | 262.1011 | 142.3620 | 1.8411 |
| 63 | 153.4347 | 268.9463 | 0.5705 | 268.9463 | 153.4347 | 1.7528 |
| 64 | 148.8125 | 262.3391 | 0.5673 | 262.3391 | 148.8125 | 1.7629 |
| 65 | 151.5232 | 265.1171 | 0.5715 | 265.1171 | 151.5232 | 1.7497 |
| 66 | 284.7362 | 291.7525 | 0.976 | 307.181 | 268.0188 | 1.1461 |
| 67 | 201.9163 | 354.7528 | 0.5692 | 354.7528 | 201.9163 | 1.7569 |
| 68 | 207.3945 | 347.9605 | 0.596 | 347.9605 | 207.3945 | 1.6778 |
| 69 | 201.1935 | 339.4066 | 0.5928 | 339.4066 | 201.1935 | 1.6870 |
| 70 | 212.3329 | 348.3219 | 0.6096 | 348.3219 | 212.3329 | 1.6405 |
| 71 | 313.0896 | 340.6649 | 0.9191 | 352.0655 | 300.2126 | 1.1727 |
| 72 | 224.6541 | 411.051 | 0.5465 | 411.051 | 224.6541 | 1.8297 |
| 73 | 227.3489 | 405.2153 | 0.5611 | 405.2153 | 227.3489 | 1.7823 |
| 74 | 223.9582 | 407.5608 | 0.5495 | 407.5608 | 223.9582 | 1.8198 |
| 75 | 233.539 | 412.6333 | 0.566 | 412.6333 | 233.5390 | 1.7669 |
| 76 | 112.7831 | 68.8614 | 1.6378 | 103.6847 | 81.9232 | 1.2656 |
| 77 | 63.6391 | 116.4696 | 0.5464 | 116.4696 | 63.6391 | 1.8302 |
| 78 | 63.6573 | 117.28 | 0.5428 | 117.28 | -63.6573 | -1.8424 |
| 79 | 64.9941 | 118.6791 | 0.5476 | 118.6791 | -64.9941 | -1.826 |


| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 80 | 62.9518 | 115.4918 | 0.5451 | 115.4918 | 62.9518 | 1.8346 |
| 81 | 164.3796 | 122.2097 | 1.3451 | 167.9031 | 117.3218 | 1.4311 |
| 82 | 81.1605 | 176.7414 | 0.4592 | 176.7414 | 81.1605 | 2.1777 |
| 83 | 88.0791 | 178.6659 | 0.493 | 178.6659 | 88.0791 | 2.0285 |
| 84 | 90.344 | 181.2736 | 0.4984 | 181.2736 | 90.3440 | 2.0065 |
| 85 | 91.9134 | 182.55 | 0.5035 | 182.55 | 91.9134 | 1.9861 |
| 86 | 198.6521 | 158.3897 | 1.2542 | 205.1901 | 149.8231 | 1.3695 |
| 87 | 99.4893 | 239.5004 | 0.4154 | 239.5004 | 99.4893 | 2.4073 |
| 88 | 98.1772 | 238.2484 | 0.4121 | 238.2484 | 98.1772 | 2.4267 |
| 89 | 98.0449 | 242.13 | 0.4049 | 242.13 | 98.0449 | 2.4696 |
| 90 | 100.0638 | 239.2623 | 0.4182 | 239.2623 | 100.0638 | 2.3911 |
| 91 | 276.5192 | 205.7899 | 1.3437 | 266.3191 | 218.8299 | 1.2170 |
| 92 | 140.2462 | 323.6529 | 0.4333 | 323.6529 | 140.2462 | 2.3077 |
| 93 | 143.6655 | 315.2217 | 0.4558 | 315.2217 | 143.6655 | 2.1941 |
| 94 | 141.0172 | 322.3968 | 0.4374 | 322.3968 | 141.0172 | 2.2862 |
| 95 | 141.963 | 316.2296 | 0.4489 | 316.2296 | 141.9630 | 2.2275 |
| 96 | 244.9995 | 243.7751 | 1.005 | 295.7011 | 178.9187 | 1.6527 |
| 97 | 93.9447 | 333.7997 | 0.2814 | 333.7997 | 93.9447 | 3.5531 |
| 98 | 91.8477 | 339.6543 | 0.2704 | 339.6543 | 91.8477 | 3.6980 |
| 99 | 101.1709 | 335.6297 | 0.3014 | 335.6297 | 101.1709 | 3.3175 |
| 100 | 99.2913 | 343.7709 | 0.2888 | 343.7709 | 99.2913 | 3.4622 |
| 101 | 163.155 | 213.7201 | 0.7634 | 161.1101 | 215.2657 | 0.7484 |
| 102 | 201.2496 | 185.7809 | 1.0833 | 185.7809 | 201.2496 | 0.9231 |
| 103 | 199.8761 | 184.3276 | 1.0844 | 184.3276 | 199.8761 | 0.9222 |
| 104 | 199.5928 | 186.4235 | 1.0706 | 186.4235 | 199.5928 | 0.9340 |
| 105 | 200.8335 | 187.2002 | 1.0728 | 187.2002 | 200.8335 | 0.9321 |
| 106 | 206.7219 | 302.6463 | 0.683 | 223.3055 | 290.6258 | 0.7684 |
| 107 | 259.7657 | 260.5958 | 0.9968 | 260.5958 | 259.7657 | 1.0032 |
| 108 | 261.4814 | 264.5966 | 0.9882 | 264.5966 | 261.4814 | 1.0119 |
| 109 | 268.5294 | 271.2766 | 0.9899 | 271.2766 | 268.5294 | 1.0102 |
| 110 | 269.8701 | 274.0365 | 0.9848 | 274.0365 | 269.8701 | 1.0154 |
| 111 | 232.5042 | 370.7724 | 0.6271 | 269.7435 | 344.6286 | 0.7827 |
| 112 | 296.6442 | 324.1789 | 0.9151 | 324.1789 | 296.6442 | 1.0928 |
| 113 | 302.8356 | 329.6997 | 0.9185 | 329.6997 | 302.8356 | 1.0887 |
| 114 | 299.3754 | 331.8196 | 0.9022 | 331.8196 | 299.3754 | 1.1084 |
| 115 | 310.1497 | 340.834 | 0.91 | 340.834 | 310.1497 | 1.0989 |
| 116 | 266.0723 | 448.3648 | 0.5934 | 323.5304 | 408.8442 | 0.7913 |
| 117 | 347.7198 | 397.9039 | 0.8739 | 397.9039 | 347.7198 | 1.1443 |
| 118 | 354.7987 | 405.5534 | 0.8749 | 405.5534 | 354.7987 | 1.1431 |
| 119 | 358.8273 | 405.5811 | 0.8847 | 405.5811 | 358.8273 | 1.1303 |
| 120 | 359.2857 | 410.5226 | 0.8752 | 410.5226 | 359.2857 | 1.1426 |
| 121 | 316.458 | 522.4502 | 0.6057 | 370.3565 | 485.7324 | 0.7625 |
| 122 | 396.068 | 466.8819 | 0.8483 | 466.8819 | 396.0680 | 1.1788 |
| 123 | 407.5286 | 474.8292 | 0.8583 | 474.8292 | 407.5286 | 1.1651 |
| 124 | 402.6982 | 477.0524 | 0.8441 | 477.0524 | 402.6982 | 1.1846 |
| 125 | 399.2012 | 472.631 | 0.8446 | 472.631 | 399.2012 | 1.1839 |
| 126 | 162.9359 | 165.2332 | 0.9861 | 142.1853 | 183.3943 | 0.7753 |


| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 127 | 162.1041 | 165.1499 | 0.9816 | 165.1499 | 162.1041 | 1.0188 |
| 128 | 162.9914 | 165.581 | 0.9844 | 165.581 | 162.9914 | 1.0159 |
| 129 | 165.6891 | 166.338 | 0.9961 | 166.338 | 165.6891 | 1.0039 |
| 130 | 166.8184 | 168.7141 | 0.9888 | 168.7141 | 166.8184 | 1.0114 |
| 131 | 219.5647 | 261.0481 | 0.8411 | 224.903 | 256.4632 | 0.8769 |
| 132 | 213.2506 | 254.2292 | 0.8388 | 254.2292 | 213.2506 | 1.1922 |
| 133 | 215.2732 | 254.5406 | 0.8457 | 254.5406 | 215.2732 | 1.1824 |
| 134 | 220.1807 | 259.7471 | 0.8477 | 259.7471 | 220.1807 | 1.1797 |
| 135 | 213.1102 | 256.4842 | 0.8309 | 256.4842 | 213.1102 | 1.2035 |
| 136 | 306.661 | 331.6338 | 0.9247 | 266.7801 | 364.4864 | 0.7319 |
| 137 | 304.5306 | 333.9596 | 0.9119 | 333.9596 | 304.5306 | 1.0966 |
| 138 | 298.4483 | 337.417 | 0.8845 | 337.417 | 298.4483 | 1.1306 |
| 139 | 309.4737 | 345.7519 | 0.8951 | 345.7519 | 309.4737 | 1.1172 |
| 140 | 302.9238 | 342.2661 | 0.8851 | 342.2661 | 302.9238 | 1.1299 |
| 141 | 371.3089 | 412.5695 | 0.9 | 332.4675 | 444.4651 | 0.7480 |
| 142 | 379.8773 | 415.9003 | 0.9134 | 415.9003 | 379.8773 | 1.0948 |
| 143 | 378.5803 | 417.6269 | 0.9065 | 417.6269 | 378.5803 | 1.1031 |
| 144 | 374.1755 | 407.4259 | 0.9184 | 407.4259 | 374.1755 | 1.0889 |
| 145 | 377.5255 | 403.7149 | 0.9351 | 403.7149 | 377.5255 | 1.0694 |
| 146 | 322.9589 | 463.6449 | 0.6966 | 382.1987 | 416.1649 | 0.9184 |
| 147 | 328.9528 | 459.787 | 0.7154 | 459.787 | 328.9528 | 1.3977 |
| 148 | 337.3287 | 459.4949 | 0.7341 | 459.4949 | 337.3287 | 1.3622 |
| 149 | 328.9954 | 454.964 | 0.7231 | 454.964 | 328.9954 | 1.3829 |
| 150 | 337.7602 | 463.6962 | 0.7284 | 463.6962 | 337.7602 | 1.3729 |
| 151 | 88.7104 | 93.4059 | 0.9497 | 99.9529 | 81.2626 | 1.2300 |
| 152 | 63.2416 | 114.0435 | 0.5545 | 114.0435 | 63.2416 | 1.8033 |
| 153 | 64.4127 | 116.2906 | 0.5539 | 116.2906 | 64.4127 | 1.8054 |
| 154 | 65.1112 | 117.1496 | 0.5558 | 117.1496 | 65.1112 | 1.7992 |
| 155 | 66.058 | 117.3281 | 0.563 | 117.3281 | 66.0580 | 1.7761 |
| 156 | 152.7422 | 163.485 | 0.9343 | 171.7785 | 143.3516 | 1.1983 |
| 157 | 104.2617 | 190.4033 | 0.5476 | 190.4033 | 104.2617 | 1.8262 |
| 158 | 112.199 | 195.5409 | 0.5738 | 195.5409 | 112.1990 | 1.7428 |
| 159 | 114.3065 | 199.6868 | 0.5724 | 199.6868 | 114.3065 | 1.7469 |
| 160 | 119.2931 | 200.8401 | 0.594 | 200.8401 | 119.2931 | 1.6836 |
| 161 | 195.7189 | 210.8054 | 0.9284 | 218.5745 | 187.0027 | 1.1688 |
| 162 | 143.1355 | 265.2779 | 0.5396 | 265.2779 | 143.1355 | 1.8533 |
| 163 | 142.515 | 265.0369 | 0.5377 | 265.0369 | 142.5150 | 1.8597 |
| 164 | 144.0262 | 265.7019 | 0.5421 | 265.7019 | 144.0262 | 1.8448 |
| 165 | 145.1991 | 268.8831 | 0.54 | 268.8831 | 145.1991 | 1.8518 |
| 166 | 245.2068 | 269.6919 | 0.9092 | 273.7338 | 240.6864 | 1.1373 |
| 167 | 163.5994 | 323.5697 | 0.5056 | 323.5697 | 163.5994 | 1.9778 |
| 168 | 165.446 | 323.5697 | 0.5113 | 323.5697 | 165.4460 | 1.9557 |
| 169 | 172.0612 | 329.7176 | 0.5218 | 329.7176 | 172.0612 | 1.9163 |
| 170 | 167.4072 | 326.1765 | 0.5132 | 326.1765 | 167.4072 | 1.9484 |
| 171 | 247.9751 | 309.7016 | 0.8007 | 311.0038 | 246.3400 | 1.2625 |
| 172 | 167.9498 | 372.6552 | 0.4507 | 372.6552 | 167.9498 | 2.2188 |
| 173 | 169.5887 | 372.6489 | 0.4551 | 372.6489 | 169.5887 | 2.1974 |


| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 174 | 167.1795 | 376.4682 | 0.4441 | 376.4682 | 167.1795 | 2.2519 |
| 175 | 170.1 | 375.4764 | 0.453 | 375.4764 | 170.1000 | 2.2074 |
| 176 | 70.6428 | 62.4051 | 1.132 | 78.6263 | 51.9876 | 1.5124 |
| 177 | 33.7425 | 91.2695 | 0.3697 | 91.2695 | 33.7425 | 2.7049 |
| 178 | 32.2379 | 95.873 | 0.3363 | 95.873 | 32.2379 | 2.9739 |
| 179 | 35.996 | 95.9412 | 0.3752 | 95.9412 | 35.9960 | 2.6653 |
| 180 | 38.689 | 94.1467 | 0.4109 | 94.1467 | 38.6890 | 2.4334 |
| 181 | 113.3678 | 107.4873 | 1.0547 | 132.6994 | 82.4417 | 1.6096 |
| 182 | 47.7565 | 152.4468 | 0.3133 | 152.4468 | 47.7565 | 3.1922 |
| 183 | 50.2597 | 155.6077 | 0.323 | 155.6077 | 50.2597 | 3.0961 |
| 184 | 50.2975 | 155.8898 | 0.3226 | 155.8898 | 50.2975 | 3.0994 |
| 185 | 51.8714 | 156.5935 | 0.3312 | 156.5935 | 51.8714 | 3.0189 |
| 186 | 162.8985 | 154.9715 | 1.0512 | 186.3179 | 125.8480 | 1.4805 |
| 187 | 61.2472 | 210.745 | 0.2906 | 210.745 | 61.2472 | 3.4409 |
| 188 | 64.6666 | 211.8868 | 0.3052 | 211.8868 | 64.6666 | 3.2766 |
| 189 | 69.2517 | 216.0162 | 0.3206 | 216.0162 | 69.2517 | 3.1193 |
| 190 | 70.628 | 217.1014 | 0.3253 | 217.1014 | 70.6280 | 3.0739 |
| 191 | 223.1166 | 201.1148 | 1.1094 | 246.6438 | 171.4498 | 1.4386 |
| 192 | 88.1638 | 279.4771 | 0.3155 | 279.4771 | 88.1638 | 3.1700 |
| 193 | 86.1354 | 277.423 | 0.3105 | 277.423 | 86.1354 | 3.2208 |
| 194 | 86.2464 | 281.964 | 0.3059 | 281.964 | 86.2464 | 3.2693 |
| 195 | 91.2761 | 287.9853 | 0.3169 | 287.9853 | 91.2761 | 3.1551 |
| 196 | 259.2312 | 230.2289 | 1.126 | 286.2171 | 195.6679 | 1.4628 |
| 197 | 107.6019 | 325.5716 | 0.3305 | 325.5716 | 107.6019 | 3.0257 |
| 198 | 108.0435 | 331.8501 | 0.3256 | 331.8501 | 108.0435 | 3.0714 |
| 199 | 112.4562 | 336.0007 | 0.3347 | 336.0007 | 112.4562 | 2.9878 |
| 200 | 102.807 | 322.619 | 0.3187 | 322.619 | 102.8070 | 3.1381 |
| 201 | 169.5545 | 228.4957 | 0.742 | 173.6316 | 225.4131 | 0.7703 |
| 202 | 207.1426 | 192.6893 | 1.075 | 192.6893 | 207.1426 | 0.9302 |
| 203 | 202.68 | 194.1392 | 1.044 | 194.1392 | 202.6800 | 0.9579 |
| 204 | 217.7624 | 200.6148 | 1.0855 | 200.6148 | 217.7624 | 0.9213 |
| 205 | 214.5732 | 198.1373 | 1.083 | 198.1373 | 214.5732 | 0.9234 |
| 206 | 234.4741 | 326.8637 | 0.7173 | 237.7651 | 324.4777 | 0.7328 |
| 207 | 287.13 | 282.1961 | 1.0175 | 282.1961 | 287.1300 | 0.9828 |
| 208 | 292.2072 | 285.1416 | 1.0248 | 285.1416 | 292.2072 | 0.9758 |
| 209 | 284.7899 | 279.5205 | 1.0189 | 279.5205 | 284.7899 | 0.9815 |
| 210 | 289.2702 | 279.558 | 1.0347 | 279.558 | 289.2702 | 0.9664 |
| 211 | 309.3758 | 456.3637 | 0.6779 | 331.7829 | 440.3423 | 0.7535 |
| 212 | 373.3497 | 398.0761 | 0.9379 | 398.0761 | 373.3497 | 1.0662 |
| 213 | 382.5961 | 385.8474 | 0.9916 | 385.8474 | 382.5961 | 1.0085 |
| 214 | 382.5391 | 391.1423 | 0.978 | 391.1423 | 382.5391 | 1.0225 |
| 215 | 379.7901 | 396.6776 | 0.9574 | 396.6776 | 379.7901 | 1.0445 |
| 216 | 287.0673 | 496.7286 | 0.5779 | 364.9637 | 442.6607 | 0.8245 |
| 217 | 373.8964 | 424.6515 | 0.8805 | 424.6515 | 373.8964 | 1.1357 |
| 218 | 381.3443 | 437.8459 | 0.871 | 437.8459 | 381.3443 | 1.1482 |
| 219 | 390.1037 | 439.4337 | 0.8877 | 439.4337 | 390.1037 | 1.1265 |
| 220 | 377.0451 | 433.2095 | 0.8704 | 433.2095 | 377.0451 | 1.1490 |


| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 221 | 303.5935 | 556.7616 | 0.5453 | 401.4681 | 490.8930 | 0.8178 |
| 222 | 373.1608 | 478.6916 | 0.7795 | 478.6916 | 373.1608 | 1.2828 |
| 223 | 378.8455 | 472.3057 | 0.8021 | 472.3057 | 378.8455 | 1.2467 |
| 224 | 382.9149 | 474.1717 | 0.8075 | 474.1717 | 382.9149 | 1.2383 |
| 225 | 392.4226 | 487.8136 | 0.8045 | 487.8136 | 392.4226 | 1.2431 |
| 226 | 164.5504 | 184.5599 | 0.8916 | 163.1351 | 185.8121 | 0.8780 |
| 227 | 163.1026 | 182.9984 | 0.8913 | 182.9984 | 163.1026 | 1.1220 |
| 228 | 159.9201 | 178.6047 | 0.8954 | 178.6047 | 159.9201 | 1.1168 |
| 229 | 161.9422 | 182.6511 | 0.8866 | 182.6511 | 161.9422 | 1.1279 |
| 230 | 163.0827 | 181.1829 | 0.9001 | 181.1829 | 163.0827 | 1.1110 |
| 231 | 233.1829 | 271.1694 | 0.8599 | 233.0307 | 271.3002 | 0.8589 |
| 232 | 234.9983 | 266.0591 | 0.8833 | 266.0591 | 234.9983 | 1.1322 |
| 233 | 242.5081 | 275.9159 | 0.8789 | 275.9159 | 242.5081 | 1.1378 |
| 234 | 236.4188 | 270.1852 | 0.875 | 270.1852 | 236.4188 | 1.1428 |
| 235 | 237.9905 | 274.003 | 0.8686 | 274.003 | 237.9905 | 1.1513 |
| 236 | 279.5769 | 346.4283 | 0.807 | 291.6152 | 336.3575 | 0.8670 |
| 237 | 279.0627 | 343.8411 | 0.8116 | 343.8411 | 279.0627 | 1.2321 |
| 238 | 281.6154 | 342.3731 | 0.8225 | 342.3731 | 281.6154 | 1.2157 |
| 239 | 275.8128 | 342.3738 | 0.8056 | 342.3738 | 275.8128 | 1.2413 |
| 240 | 279.2154 | 342.2708 | 0.8158 | 342.2708 | 279.2154 | 1.2258 |
| 241 | 334.6459 | 425.5195 | 0.7864 | 350.2322 | 412.7858 | 0.8485 |
| 242 | 331.8301 | 416.7075 | 0.7963 | 416.7075 | 331.8301 | 1.2558 |
| 243 | 335.0354 | 424.1981 | 0.7898 | 424.1981 | 335.0354 | 1.2661 |
| 244 | 328.8234 | 420.35 | 0.7823 | 420.35 | 328.8234 | 1.2783 |
| 245 | 326.9944 | 424.9836 | 0.7694 | 424.9836 | 326.9944 | 1.2997 |
| 246 | 430.5991 | 484.6631 | 0.8885 | 386.2096 | 520.7264 | 0.7417 |
| 247 | 427.0402 | 488.0082 | 0.8751 | 488.0082 | 427.0402 | 1.1428 |
| 248 | 417.6366 | 483.0138 | 0.8646 | 483.0138 | 417.6366 | 1.1565 |
| 249 | 424.0487 | 490.4496 | 0.8646 | 490.4496 | 424.0487 | 1.1566 |
| 250 | 417.0269 | 487.2506 | 0.8559 | 487.2506 | 417.0269 | 1.1684 |
| 251 | 110.2801 | 107.5452 | 1.0254 | 118.2208 | 98.7498 | 1.1972 |
| 252 | 77.7225 | 130.8423 | 0.594 | 130.8423 | 77.7225 | 1.6835 |
| 253 | 78.8442 | 129.2723 | 0.6099 | 129.2723 | 78.8442 | 1.6396 |
| 254 | 76.9546 | 133.4419 | 0.5767 | 133.4419 | 76.9546 | 1.7340 |
| 255 | 77.8638 | 129.4782 | 0.6014 | 129.4782 | 77.8638 | 1.6629 |
| 256 | 202.375 | 175.2947 | 1.1545 | 192.0853 | 186.5131 | 1.0299 |
| 257 | 152.0043 | 220.2428 | 0.6902 | 220.2428 | 152.0043 | 1.4489 |
| 258 | 156.324 | 228.9791 | 0.6827 | 228.9791 | 156.3240 | 1.4648 |
| 259 | 149.3831 | 219.0391 | 0.682 | 219.0391 | 149.3831 | 1.4663 |
| 260 | 149.2316 | 219.1011 | 0.6811 | 219.1011 | 149.2316 | 1.4682 |
| 261 | 237.6644 | 238.273 | 0.9974 | 252.2228 | 222.8049 | 1.1320 |
| 262 | 163.8237 | 284.3597 | 0.5761 | 284.3597 | 163.8237 | 1.7358 |
| 263 | 166.1155 | 286.7002 | 0.5794 | 286.7002 | 166.1155 | 1.7259 |
| 264 | 169.8913 | 290.2186 | 0.5854 | 290.2186 | 169.8913 | 1.7083 |
| 265 | 170.3016 | 295.5275 | 0.5763 | 295.5275 | 170.3016 | 1.7353 |
| 266 | 331.9794 | 305.1023 | 1.0881 | 328.8548 | 308.4677 | 1.0661 |
| 267 | 243.4664 | 381.1891 | 0.6387 | 381.1891 | 243.4664 | 1.5657 |


| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 268 | 236.7358 | 376.3736 | 0.629 | 376.3736 | 236.7358 | 1.5898 |
| 269 | 240.0703 | 388.8308 | 0.6174 | 388.8308 | 240.0703 | 1.6197 |
| 270 | 247.0985 | 389.9095 | 0.6337 | 389.9095 | 247.0985 | 1.5780 |
| 271 | 327.375 | 357.4639 | 0.9158 | 367.9325 | 315.5638 | 1.1660 |
| 272 | 222.2084 | 427.8287 | 0.5194 | 427.8287 | 222.2084 | 1.9253 |
| 273 | 229.9665 | 428.6029 | 0.5365 | 428.6029 | 229.9665 | 1.8638 |
| 274 | 230.929 | 429.1843 | 0.5381 | 429.1843 | 230.9290 | 1.8585 |
| 275 | 233.4081 | 433.5332 | 0.5384 | 433.5332 | 233.4081 | 1.8574 |
| 276 | 75.5231 | 62.2963 | 1.2123 | 80.6946 | 55.4341 | 1.4557 |
| 277 | 34.379 | 93.6644 | 0.367 | 93.6644 | 34.3790 | 2.7245 |
| 278 | 36.4733 | 95.4205 | 0.3822 | 95.4205 | 36.4733 | 2.6162 |
| 279 | 37.0401 | 96.0515 | 0.3856 | 96.0515 | 37.0401 | 2.5932 |
| 280 | 31.39 | 92.8399 | 0.3381 | 92.8399 | 31.3900 | 2.9576 |
| 281 | 129.375 | 108.7244 | 1.1899 | 138.8432 | 96.3403 | 1.4412 |
| 282 | 58.8684 | 169.1589 | 0.348 | 169.1589 | 58.8684 | 2.8735 |
| 283 | 64.8787 | 166.0229 | 0.3908 | 166.0229 | 64.8787 | 2.5590 |
| 284 | 64.8416 | 167.4373 | 0.3873 | 167.4373 | 64.8416 | 2.5823 |
| 285 | 54.8339 | 171.6381 | 0.3195 | 171.6381 | 54.8339 | 3.1301 |
| 286 | 167.5055 | 149.9337 | 1.1172 | 191.4866 | 117.7756 | 1.6259 |
| 287 | 74.4158 | 219.5313 | 0.339 | 219.5313 | 74.4158 | 2.9501 |
| 288 | 76.2422 | 218.8497 | 0.3484 | 218.8497 | 76.2422 | 2.8705 |
| 289 | 74.3471 | 217.4577 | 0.3419 | 217.4577 | 74.3471 | 2.9249 |
| 290 | 83.6924 | 224.6447 | 0.3726 | 224.6447 | 83.6924 | 2.6842 |
| 291 | 197.1468 | 188.2939 | 1.047 | 236.0396 | 136.4065 | 1.7304 |
| 292 | 76.7912 | 262.8484 | 0.2922 | 262.8484 | 76.7912 | 3.4229 |
| 293 | 82.3925 | 270.9511 | 0.3041 | 270.9511 | 82.3925 | 3.2885 |
| 294 | 85.1815 | 271.8372 | 0.3134 | 271.8372 | 85.1815 | 3.1913 |
| 295 | 83.8936 | 269.3505 | 0.3115 | 269.3505 | 83.8936 | 3.2106 |
| 296 | 357.9019 | 228.4282 | 1.5668 | 302.7941 | 297.6389 | 1.0173 |
| 297 | 191.2584 | 369.0897 | 0.5182 | 369.0897 | 191.2584 | 1.9298 |
| 298 | 198.9184 | 369.0897 | 0.5389 | 369.0897 | 198.9184 | 1.8555 |
| 299 | 197.3296 | 364.3208 | 0.5416 | 364.3208 | 197.3296 | 1.8463 |
| 300 | 186.2928 | 369.2408 | 0.5045 | 369.2408 | 186.2928 | 1.9820 |
| 301 | 158.5647 | 227.7806 | 0.6961 | 175.8309 | 214.7329 | 0.8188 |
| 302 | 196.3354 | 192.175 | 1.0216 | 192.175 | 196.3354 | 0.9788 |
| 303 | 204.0934 | 201.2071 | 1.0143 | 201.2071 | 204.0934 | 0.9859 |
| 304 | 201.2784 | 193.76 | 1.0388 | 193.76 | 201.2784 | 0.9626 |
| 305 | 208.4875 | 202.2933 | 1.0306 | 202.2933 | 208.4875 | 0.9703 |
| 306 | 242.4013 | 337.6371 | 0.7179 | 249.2924 | 332.5815 | 0.7496 |
| 307 | 300.1617 | 291.3465 | 1.0303 | 291.3465 | 300.1617 | 0.9706 |
| 308 | 289.5194 | 286.3318 | 1.0111 | 286.3318 | 289.5194 | 0.9890 |
| 309 | 289.8274 | 286.5597 | 1.0114 | 286.5597 | 289.8274 | 0.9887 |
| 310 | 287.2581 | 293.0959 | 0.9801 | 293.0959 | 287.2581 | 1.0203 |
| 311 | 289.1253 | 431.7996 | 0.6696 | 308.9547 | 417.8412 | 0.7394 |
| 312 | 359.7902 | 373.8692 | 0.9623 | 373.8692 | 359.7902 | 1.0391 |


| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 313 | 349.0415 | 367.1384 | 0.9507 | 367.1384 | 349.0415 | 1.0518 |
| 314 | 356.6663 | 364.5413 | 0.9784 | 364.5413 | 356.6663 | 1.0221 |
| 315 | 349.8105 | 362.813 | 0.9642 | 362.813 | 349.8105 | 1.0372 |
| 316 | 295.0665 | 487.5075 | 0.6053 | 359.6964 | 441.9800 | 0.8138 |
| 317 | 386.0774 | 429.459 | 0.899 | 429.459 | 386.0774 | 1.1124 |
| 318 | 373.0587 | 428.976 | 0.8696 | 428.976 | 373.0587 | 1.1499 |
| 319 | 374.3297 | 435.5474 | 0.8594 | 435.5474 | 374.3297 | 1.1635 |
| 320 | 376.0092 | 429.0622 | 0.8764 | 429.0622 | 376.0092 | 1.1411 |
| 321 | 383.5387 | 610.5565 | 0.6282 | 436.8354 | 573.6341 | 0.7615 |
| 322 | 490.7619 | 544.2519 | 0.9017 | 544.2519 | 490.7619 | 1.1090 |
| 323 | 491.3546 | 544.1311 | 0.903 | 544.1311 | 491.3546 | 1.1074 |
| 324 | 491.4266 | 546.3741 | 0.8994 | 546.3741 | 491.4266 | 1.1118 |
| 325 | 491.3052 | 547.4965 | 0.8974 | 547.4965 | 491.3052 | 1.1144 |
| 326 | 152.4772 | 175.133 | 0.8706 | 153.6019 | 174.1474 | 0.8820 |
| 327 | 152.2068 | 180.9133 | 0.8413 | 180.9133 | 152.2068 | 1.1886 |
| 328 | 156.0352 | 179.9308 | 0.8672 | 179.9308 | 156.0352 | 1.1531 |
| 329 | 158.5667 | 179.1254 | 0.8852 | 179.1254 | 158.5667 | 1.1297 |
| 330 | 156.9991 | 176.181 | 0.8911 | 176.181 | 156.9991 | 1.1222 |
| 331 | 247.4289 | 279.3266 | 0.8858 | 240.1728 | 285.5896 | 0.8410 |
| 332 | 243.5632 | 275.3585 | 0.8845 | 275.3585 | 243.5632 | 1.1305 |
| 333 | 246.5875 | 278.1679 | 0.8865 | 278.1679 | 246.5875 | 1.1281 |
| 334 | 252.9061 | 282.2953 | 0.8959 | 282.2953 | 252.9061 | 1.1162 |
| 335 | 252.7687 | 284.098 | 0.8897 | 284.098 | 252.7687 | 1.1239 |
| 336 | 307.5088 | 364.4924 | 0.8437 | 307.9256 | 364.1404 | 0.8456 |
| 337 | 304.3039 | 358.126 | 0.8497 | 358.126 | 304.3039 | 1.1769 |
| 338 | 299.7853 | 355.6117 | 0.843 | 355.6117 | 299.7853 | 1.1862 |
| 339 | 298.1503 | 356.1509 | 0.8371 | 356.1509 | 298.1503 | 1.1945 |
| 340 | 306.4602 | 362.9809 | 0.8443 | 362.9809 | 306.4602 | 1.1844 |
| 341 | 335.8497 | 421.2274 | 0.7973 | 352.4936 | 407.4012 | 0.8652 |
| 342 | 335.8612 | 418.2116 | 0.8031 | 418.2116 | 335.8612 | 1.2452 |
| 343 | 334.4233 | 418.9726 | 0.7982 | 418.9726 | 334.4233 | 1.2528 |
| 344 | 338.8065 | 422.3275 | 0.8022 | 422.3275 | 338.8065 | 1.2465 |
| 345 | 338.8065 | 422.8405 | 0.8013 | 422.8405 | 338.8065 | 1.2480 |
| 346 | 462.9319 | 556.5036 | 0.8319 | 453.3699 | 564.3208 | 0.8034 |
| 347 | 463.8574 | 554.134 | 0.8371 | 554.134 | 463.8574 | 1.1946 |
| 348 | 461.594 | 546.7876 | 0.8442 | 546.7876 | 461.5940 | 1.1846 |
| 349 | 456.2306 | 559.0695 | 0.8161 | 559.0695 | 456.2306 | 1.2254 |
| 350 | 454.8527 | 541.429 | 0.8401 | 541.429 | 454.8527 | 1.1903 |
| 351 | 89.8206 | 97.8126 | 0.9183 | 104.3512 | 82.1333 | 1.2705 |
| 352 | 61.1567 | 117.5025 | 0.5205 | 117.5025 | 61.1567 | 1.9213 |
| 353 | 62.3705 | 120.783 | 0.5164 | 120.783 | 62.3705 | 1.9365 |
| 354 | 63.5301 | 120.5455 | 0.527 | 120.5455 | 63.5301 | 1.8975 |
| 355 | 64.199 | 121.12 | 0.53 | 121.12 | 64.1990 | 1.8866 |
| 356 | 130.8158 | 159.4002 | 0.8207 | 165.649 | 122.8072 | 1.3489 |
| 357 | 86.1069 | 189.8 | 0.4537 | 189.8 | 86.1069 | 2.2042 |
| 358 | 86.883 | 189.432 | 0.4587 | 189.432 | 86.8830 | 2.1803 |


| Run No. | F | N | F/N Ratio | Fs | Fn | Fs/Fn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 359 | 82.936 | 185.5118 | 0.4471 | 185.5118 | 82.9360 | 2.2368 |
| 360 | 82.9105 | 185.8108 | 0.4462 | 185.8108 | 82.9105 | 2.2411 |
| 361 | 220.3518 | 228.1979 | 0.9656 | 235.667 | 212.3447 | 1.1098 |
| 362 | 151.4303 | 274.1256 | 0.5524 | 274.1256 | 151.4303 | 1.8102 |
| 363 | 156.5936 | 276.4732 | 0.5664 | 276.4732 | 156.5936 | 1.7655 |
| 364 | 157.1355 | 277.2494 | 0.5668 | 277.2494 | 157.1355 | 1.7644 |
| 365 | 159.999 | 279.3632 | 0.5727 | 279.3632 | 159.9990 | 1.7460 |
| 366 | 269.2133 | 280.911 | 0.9584 | 290.9219 | 258.3626 | 1.1260 |
| 367 | 181.2863 | 342.5107 | 0.5293 | 342.5107 | 181.2863 | 1.8893 |
| 368 | 188.967 | 347.3744 | 0.544 | 347.3744 | 188.9670 | 1.8383 |
| 369 | 181.3638 | 342.7891 | 0.5291 | 342.7891 | 181.3638 | 1.8901 |
| 370 | 186.9441 | 347.3383 | 0.5382 | 347.3383 | 186.9441 | 1.8580 |
| 371 | 304.4865 | 353.0099 | 0.8625 | 367.1155 | 287.3226 | 1.2777 |
| 372 | 209.5801 | 414.2354 | 0.5059 | 414.2354 | 209.5801 | 1.9765 |
| 373 | 209.4235 | 415.6389 | 0.5039 | 415.6389 | 209.4235 | 1.9847 |
| 374 | 211.2018 | 416.244 | 0.5074 | 416.244 | 211.2018 | 1.9708 |
| 375 | 212.4995 | 423.9621 | 0.5012 | 423.9621 | 212.4995 | 1.9951 |
| 376 | 100.7103 | 70.789 | 1.4227 | 95.1356 | 78.1208 | 1.2178 |
| 377 | 50.7544 | 109.552 | 0.4633 | 109.552 | 50.7544 | 2.1585 |
| 378 | 51.1189 | 112.6215 | 0.4539 | 112.6215 | 51.1189 | 2.2031 |
| 379 | 49.955 | 108.7509 | 0.4594 | 108.7509 | 49.9550 | 2.1770 |
| 380 | 50.6559 | 110.5263 | 0.4583 | 110.5263 | 50.6559 | 2.1819 |
| 381 | 131.0256 | 116.1779 | 1.1278 | 144.2305 | 99.3104 | 1.4523 |
| 382 | 57.7285 | 169.0374 | 0.3415 | 169.0374 | 57.7285 | 2.9281 |
| 383 | 45.0762 | 158.2031 | 0.2849 | 158.2031 | 45.0762 | 3.5097 |
| 384 | 47.4462 | 161.4845 | 0.2938 | 161.4845 | 47.4462 | 3.4035 |
| 385 | 46.0538 | 157.6917 | 0.292 | 157.6917 | 46.0538 | 3.4241 |
| 386 | 161.2817 | 158.7095 | 1.0162 | 192.4396 | 119.0273 | 1.6168 |
| 387 | 63.5088 | 220.3345 | 0.2882 | 220.3345 | 63.5088 | 3.4694 |
| 388 | 66.2184 | 223.8298 | 0.2958 | 223.8298 | 66.2184 | 3.3802 |
| 389 | 67.4257 | 224.4799 | 0.3004 | 224.4799 | 67.4257 | 3.3293 |
| 390 | 69.5599 | 224.3973 | 0.31 | 224.3973 | 69.5599 | 3.2260 |
| 391 | 327.7175 | 188.8304 | 1.7355 | 260.4949 | 274.2228 | 0.9499 |
| 392 | 183.8052 | 324.5705 | 0.5663 | 324.5705 | 183.8052 | 1.7658 |
| 393 | 187.4379 | 329.6599 | 0.5686 | 329.6599 | 187.4379 | 1.7588 |
| 394 | 193.1028 | 328.3061 | 0.5882 | 328.3061 | 193.1028 | 1.7002 |
| 395 | 187.2169 | 329.0382 | 0.569 | 329.0382 | 187.2169 | 1.7575 |
| 396 | 261.9524 | 247.4856 | 1.0585 | 298.6957 | 201.6161 | 1.4815 |
| 397 | 101.9503 | 346.1842 | 0.2945 | 346.1842 | 101.9503 | 3.3956 |
| 398 | 94.5451 | 333.1663 | 0.2838 | 333.1663 | 94.5451 | 3.5239 |
| 399 | 95.4506 | 334.7357 | 0.2852 | 334.7357 | 95.4506 | 3.5069 |
| 400 | 97.1873 | 341.0194 | 0.285 | 341.0194 | 97.1873 | 3.5089 |

## APPENDIX F

The effective tool surface roughness calculated using data obtained from the profilometer, the Chip thickness ratio, Shear Plane Angle, Shear Front angle, Friction angle, Shear Area and Shear Stress calculated from the classical Metal Cutting equations using the raw data obtained from the experiments are tablulated below.

| Run No. | Roughness ( $\mu \mathrm{m}$ ) | t/te | $\Phi$ (degrees) | $\beta$ (degrees) | $\mathrm{A}_{\text {s }}\left(\right.$ inch $\left.^{2}\right)$ | $\tau_{\text {s }}(\mathbf{M P a})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 154.942318 | 0.121892 | 6.704454207 | 35.2848498 | 0.0010707 | 254.35318 |
| 2 |  |  |  | 46.09109792 |  |  |
| 3 |  |  |  | 44.5168538 |  |  |
| 4 |  |  |  | 46.22510005 |  |  |
| 5 |  |  |  | 46.40603269 |  |  |
| 6 | 161.1517652 | 0.162259 | 8.83393002 | 33.70095615 | 0.0016279 | 248.96012 |
| 7 |  |  |  | 43.80856404 |  |  |
| 8 |  |  |  | 44.03211179 |  |  |
| 9 |  |  |  | 43.9692226 |  |  |
| 10 |  |  |  | 43.64414797 |  |  |
| 11 | 169.620113 | 0.171292 | 9.303365676 | 32.79725047 | 0.0023197 | 219.85956 |
| 12 |  |  |  | 43.74369905 |  |  |
| 13 |  |  |  | 41.81090436 |  |  |
| 14 |  |  |  | 42.13079373 |  |  |
| 15 |  |  |  | 41.9711911 |  |  |
| 16 | 164.004236 | 0.191847 | 10.36155416 | 30.83008201 | 0.00278 | 222.69739 |
| 17 |  |  |  | 41.02620866 |  |  |
| 18 |  |  |  | 41.45726363 |  |  |
| 19 |  |  |  | 41.69795712 |  |  |
| 20 |  |  |  | 41.50534539 |  |  |
| 21 | 172.25711 | 0.207245 | 11.14494369 | 30.6222396 | 0.0032335 | 219.97836 |
| 22 |  |  |  | 40.82268516 |  |  |
| 23 |  |  |  | 40.84603361 |  |  |
| 24 |  |  |  | 40.91143225 |  |  |
| 25 |  |  |  | 40.69343989 |  |  |
| 26 | 57.234495 | 0.156299 | 8.883390955 | 46.01699116 | 0.0008095 | 318.0925 |
| 27 |  |  |  | 45.73987577 |  |  |
| 28 |  |  |  | 45.26687443 |  |  |
| 29 |  |  |  | 45.54367647 |  |  |
| 30 |  |  |  | 44.77756185 |  |  |


| Run No. | Roughness ( $\mu \mathrm{m}$ ) | t/te | $\Phi$ (degrees) | $\boldsymbol{\beta}$ (degrees) | $\mathbf{A}_{\text {S }}\left(\right.$ inch $\left.^{2}\right)$ | $\tau_{\text {s }}(\mathrm{MPa})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 31 | 53.159259 | 0.176025 | 9.98323796 | 41.19162882 | 0.0014421 | 266.08323 |
| 32 |  |  |  | 41.05666261 |  |  |
| 33 |  |  |  | 40.8061092 |  |  |
| 34 |  |  |  | 40.49030077 |  |  |
| 35 |  |  |  | 40.76831763 |  |  |
| 36 | 58.699539 | 0.215548 | 12.16389917 | 42.18632849 | 0.0017797 | 272.10987 |
| 37 |  |  |  | 42.73275743 |  |  |
| 38 |  |  |  | 42.07060344 |  |  |
| 39 |  |  |  | 42.01889115 |  |  |
| 40 |  |  |  | 42.10881411 |  |  |
| 41 | 65.485074 | 0.227505 | 12.816942 | 40.99378438 | 0.0022539 | 266.56076 |
| 42 |  |  |  | 42.34078987 |  |  |
| 43 |  |  |  | 43.38448966 |  |  |
| 44 |  |  |  | 41.34174946 |  |  |
| 45 |  |  |  | 42.75892418 |  |  |
| 46 | 84.619697 | 0.21384 | 12.07032234 | 34.76638147 | 0.0029888 | 228.18156 |
| 47 |  |  |  | 36.01788354 |  |  |
| 48 |  |  |  | 35.44656672 |  |  |
| 49 |  |  |  | 36.34093095 |  |  |
| 50 |  |  |  | 35.24691529 |  |  |
| 51 | 35.1411615 | 0.18423 | 10.58436298 | 39.71967382 | 0.0006805 | 270.02966 |
| 52 |  |  |  | 28.4394782 |  |  |
| 53 |  |  |  | 31.17087907 |  |  |
| 54 |  |  |  | 28.45687613 |  |  |
| 55 |  |  |  | 28.93456114 |  |  |
| 56 | 37.817199 | 0.190042 | 10.92721737 | 43.01217718 | 0.0013188 | 231.19109 |
| 57 |  |  |  | 29.41419657 |  |  |
| 58 |  |  |  | 29.85279808 |  |  |
| 59 |  |  |  | 30.01594471 |  |  |
| 60 |  |  |  | 30.36256106 |  |  |
| 61 | 43.691054 | 0.205959 | 11.86763239 | 41.71428606 | 0.0018235 | 218.80615 |
| 62 |  |  |  | 28.50889896 |  |  |
| 63 |  |  |  | 29.70489255 |  |  |
| 64 |  |  |  | 29.5641814 |  |  |
| 65 |  |  |  | 29.74939623 |  |  |
| 66 | 53.175756 | 0.204855 | 11.80234505 | 44.30271024 | 0.0024446 | 215.28004 |
| 67 |  |  |  | 29.64743485 |  |  |
| 68 |  |  |  | 30.79616222 |  |  |
| 69 |  |  |  | 30.65862121 |  |  |
| 70 |  |  |  | 31.36598967 |  |  |
| 71 | 54.113999 | 0.222896 | 12.8701278 | 42.58470373 | 0.0028059 | 219.69272 |
| 72 |  |  |  | 28.65818527 |  |  |
| 73 |  |  |  | 29.29491121 |  |  |
| 74 |  |  |  | 28.78917684 |  |  |
| 75 |  |  |  | 29.50865716 |  |  |


| Run No. | Roughness( $\mu \mathrm{m}$ ) | t/te | $\Phi$ (degrees) | $\beta$ (degrees) | $\mathrm{A}_{\text {s }}\left(\right.$ inch $\left.^{2}\right)$ | $\tau_{\text {s }}(\mathrm{MPa})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 76 | 116.491447 | 0.179986 | 9.719680126 | 58.5932362 | 0.0007404 | 239.32775 |
| 77 |  |  |  | 28.65223424 |  |  |
| 78 |  |  |  | 28.49222898 |  |  |
| 79 |  |  |  | 28.70710918 |  |  |
| 80 |  |  |  | 28.59372273 |  |  |
| 81 | 137.235826 | 0.211461 | 11.57316922 | 53.3706542 | 0.0012461 | 220.69079 |
| 82 |  |  |  | 24.66481459 |  |  |
| 83 |  |  |  | 26.24246689 |  |  |
| 84 |  |  |  | 26.4909587 |  |  |
| 85 |  |  |  | 26.72512571 |  |  |
| 86 | 142.468258 | 0.263112 | 14.70181433 | 51.43387331 | 0.0014776 | 244.27549 |
| 87 |  |  |  | 22.55817056 |  |  |
| 88 |  |  |  | 22.39552793 |  |  |
| 89 |  |  |  | 22.04434714 |  |  |
| 90 |  |  |  | 22.6955593 |  |  |
| 91 | 135.535181 | 0.285144 | 16.06656599 | 53.34280063 | 0.0018067 | 264.90069 |
| 92 |  |  |  | 23.42818756 |  |  |
| 93 |  |  |  | 24.50160964 |  |  |
| 94 |  |  |  | 23.62469373 |  |  |
| 95 |  |  |  | 24.17644769 |  |  |
| 96 | 149.38949 | 0.284608 | 16.03318923 | 45.14351729 | 0.0022629 | 225.83987 |
| 97 |  |  |  | 15.71874978 |  |  |
| 98 |  |  |  | 15.13175104 |  |  |
| 99 |  |  |  | 16.77470165 |  |  |
| 100 |  |  |  | 16.11029953 |  |  |
| 101 | 118.496228 | 0.105574 | 5.829622051 | 37.35830095 | 0.0012307 | 227.92588 |
| 102 |  |  |  | 47.28875955 |  |  |
| 103 |  |  |  | 47.31746222 |  |  |
| 104 |  |  |  | 46.95394022 |  |  |
| 105 |  |  |  | 47.01222052 |  |  |
| 106 | 133.933197 | 0.148765 | 8.127782915 | 34.33494855 | 0.0017683 | 226.82207 |
| 107 |  |  |  | 44.90859972 |  |  |
| 108 |  |  |  | 44.66072384 |  |  |
| 109 |  |  |  | 44.70841079 |  |  |
| 110 |  |  |  | 44.56111497 |  |  |
| 111 | 110.688898 | 0.182039 | 9.858404852 | 32.09103038 | 0.0021902 | 225.93223 |
| 112 |  |  |  | 42.46048613 |  |  |
| 113 |  |  |  | 42.56808022 |  |  |
| 114 |  |  |  | 42.05751601 |  |  |
| 115 |  |  |  | 42.30134468 |  |  |
| 116 | 126.345719 | 0.203562 | 10.95831878 | 30.68608481 | 0.0026303 | 229.01087 |
| 117 |  |  |  | 41.14952263 |  |  |
| 118 |  |  |  | 41.18108185 |  |  |
| 119 |  |  |  | 41.49995673 |  |  |
| 120 |  |  |  | 41.19212386 |  |  |


| Run No. | Roughness( $\mu \mathrm{m}$ ) | t/te | (degrees) | (degrees) | As | Ts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 121 | 113.423296 | 0.213712 | 11.47147953 | 31.20408077 | 0.0031426 | 223.10984 |
| 122 |  |  |  | 40.30880414 |  |  |
| 123 |  |  |  | 40.63829025 |  |  |
| 124 |  |  |  | 40.16899295 |  |  |
| 125 |  |  |  | 40.18564309 |  |  |
| 126 | 19.352671 | 0.13369 | 7.614711942 | 44.59891579 | 0.0009433 | 265.52076 |
| 127 |  |  |  | 44.46675534 |  |  |
| 128 |  |  |  | 44.54844023 |  |  |
| 129 |  |  |  | 44.88802365 |  |  |
| 130 |  |  |  | 44.6762923 |  |  |
| 131 | 24.915753 | 0.152742 | 8.684335384 | 40.06682403 | 0.0016557 | 234.01789 |
| 132 |  |  |  | 39.99034048 |  |  |
| 133 |  |  |  | 40.22227919 |  |  |
| 134 |  |  |  | 40.28705667 |  |  |
| 135 |  |  |  | 39.72285881 |  |  |
| 136 | 33.139799 | 0.195084 | 11.03883918 | 42.7594888 | 0.0019585 | 257.40035 |
| 137 |  |  |  | 42.3610167 |  |  |
| 138 |  |  |  | 41.49304171 |  |  |
| 139 |  |  |  | 41.83091193 |  |  |
| 140 |  |  |  | 41.51054659 |  |  |
| 141 | 38.858533 | 0.198295 | 11.21595131 | 41.98693244 | 0.0025706 | 238.43237 |
| 142 |  |  |  | 42.40812283 |  |  |
| 143 |  |  |  | 42.19242117 |  |  |
| 144 |  |  |  | 42.56402744 |  |  |
| 145 |  |  |  | 43.08000153 |  |  |
| 146 | 49.853782 | 0.223095 | 12.57643961 | 34.85972652 | 0.0028704 | 239.77567 |
| 147 |  |  |  | 35.5816763 |  |  |
| 148 |  |  |  | 36.28348575 |  |  |
| 149 |  |  |  | 35.87159574 |  |  |
| 150 |  |  |  | 36.06990863 |  |  |
| 151 | 32.636596 | 0.184298 | 10.58836712 | 43.5230622 | 0.0006803 | 257.36627 |
| 152 |  |  |  | 29.01007802 |  |  |
| 153 |  |  |  | 28.98179965 |  |  |
| 154 |  |  |  | 29.06511571 |  |  |
| 155 |  |  |  | 29.3803564 |  |  |
| 156 | 30.554164 | 0.204666 | 11.79118859 | 43.05430474 | 0.0012234 | 242.80984 |
| 157 |  |  |  | 28.70438441 |  |  |
| 158 |  |  |  | 29.8466818 |  |  |
| 159 |  |  |  | 29.7880701 |  |  |
| 160 |  |  |  | 30.70906352 |  |  |
| 161 | 37.8082255 | 0.219587 | 12.67416333 | 42.87467325 | 0.0017092 | 232.79172 |
| 162 |  |  |  | 28.34988487 |  |  |
| 163 |  |  |  | 28.26770075 |  |  |
| 164 |  |  |  | 28.46032117 |  |  |
| 165 |  |  |  | 28.36941354 |  |  |


| Run No. | Roughness( $\mu \mathrm{m}$ ) | t/te | (degrees) | (degrees) | As | Ts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 166 | 42.3096365 | 0.242748 | 14.04679692 | 42.27745102 | 0.00206 | 237.27695 |
| 167 |  |  |  | 26.82152185 |  |  |
| 168 |  |  |  | 27.08133603 |  |  |
| 169 |  |  |  | 27.55754097 |  |  |
| 170 |  |  |  | 27.16876053 |  |  |
| 171 | 46.1084783 | 0.25373 | 14.69812596 | 38.68392024 | 0.0024633 | 227.56587 |
| 172 |  |  |  | 24.26033583 |  |  |
| 173 |  |  |  | 24.46979594 |  |  |
| 174 |  |  |  | 23.94473221 |  |  |
| 175 |  |  |  | 24.37169004 |  |  |
| 176 | 121.240644 | 0.266809 | 14.92963965 | 48.54295922 | 0.0004852 | 291.26065 |
| 177 |  |  |  | 20.28945305 |  |  |
| 178 |  |  |  | 18.58555156 |  |  |
| 179 |  |  |  | 20.56549311 |  |  |
| 180 |  |  |  | 22.33990008 |  |  |
| 181 | 125.14415 | 0.273224 | 15.32609707 | 46.52520894 | 0.0009459 | 246.87197 |
| 182 |  |  |  | 17.39404798 |  |  |
| 183 |  |  |  | 17.89991409 |  |  |
| 184 |  |  |  | 17.88218123 |  |  |
| 185 |  |  |  | 18.32739056 |  |  |
| 186 | 118.718115 | 0.309725 | 17.60841967 | 46.42855131 | 0.0012396 | 260.5954 |
| 187 |  |  |  | 16.2050536 |  |  |
| 188 |  |  |  | 16.97187965 |  |  |
| 189 |  |  |  | 17.77510871 |  |  |
| 190 |  |  |  | 18.0208893 |  |  |
| 191 | 117.246707 | 0.297442 | 16.83552537 | 47.96885199 | 0.0017264 | 246.6355 |
| 192 |  |  |  | 17.50838508 |  |  |
| 193 |  |  |  | 17.24873959 |  |  |
| 194 |  |  |  | 17.00767905 |  |  |
| 195 |  |  |  | 17.58585984 |  |  |
| 196 | 113.104302 | 0.283543 | 15.96683921 | 48.39102061 | 0.0022721 | 218.61285 |
| 197 |  |  |  | 18.28880409 |  |  |
| 198 |  |  |  | 18.03417339 |  |  |
| 199 |  |  |  | 18.50489775 |  |  |
| 200 |  |  |  | 17.67519805 |  |  |
| 201 | 52.118844 | 0.10533 | 5.81644704 | 36.5771382 | 0.0012334 | 241.07724 |
| 202 |  |  |  | 47.0702517 |  |  |
| 203 |  |  |  | 46.23299541 |  |  |
| 204 |  |  |  | 47.34701011 |  |  |
| 205 |  |  |  | 47.28055825 |  |  |
| 206 | 57.687602 | 0.1485 | 8.113851469 | 35.65358416 | 0.0017713 | 238.75172 |
| 207 |  |  |  | 45.49652487 |  |  |
| 208 |  |  |  | 45.70115128 |  |  |
| 209 |  |  |  | 45.53499919 |  |  |
| 210 |  |  |  | 45.97817584 |  |  |


| Run No. | Roughness( $\mu \mathrm{m}$ ) | t/te | (degrees) | (degrees) | As | Ts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 211 | 93.959022 | 0.162937 | 8.869287411 | 34.13393102 | 0.0024322 | 242.61655 |
| 212 |  |  |  | 43.16413518 |  |  |
| 213 |  |  |  | 44.75758184 |  |  |
| 214 |  |  |  | 44.36290735 |  |  |
| 215 |  |  |  | 43.75406285 |  |  |
| 216 | 110.938971 | 0.193986 | 10.47090273 | 30.02429158 | 0.0027512 | 236.63271 |
| 217 |  |  |  | 41.36321563 |  |  |
| 218 |  |  |  | 41.05441531 |  |  |
| 219 |  |  |  | 41.59680663 |  |  |
| 220 |  |  |  | 41.03477238 |  |  |
| 221 | 131.161133 | 0.226634 | 12.11963791 | 28.60295374 | 0.0029768 | 241.0205 |
| 222 |  |  |  | 37.93795612 |  |  |
| 223 |  |  |  | 38.73377128 |  |  |
| 224 |  |  |  | 38.92242908 |  |  |
| 225 |  |  |  | 38.81500604 |  |  |
| 226 | 19.937807 | 0.12276 | 6.99859315 | 41.71964144 | 0.0010259 | 268.50532 |
| 227 |  |  |  | 41.70994256 |  |  |
| 228 |  |  |  | 41.84081167 |  |  |
| 229 |  |  |  | 41.56085238 |  |  |
| 230 |  |  |  | 41.99037291 |  |  |
| 231 | 17.636055 | 0.152068 | 8.646617757 | 40.69276358 | 0.0016629 | 245.92637 |
| 232 |  |  |  | 41.45274501 |  |  |
| 233 |  |  |  | 41.31289647 |  |  |
| 234 |  |  |  | 41.18673587 |  |  |
| 235 |  |  |  | 40.97656697 |  |  |
| 236 | 27.020858 | 0.179404 | 10.17091464 | 38.90445738 | 0.0021236 | 242.68349 |
| 237 |  |  |  | 39.06291105 |  |  |
| 238 |  |  |  | 39.43864681 |  |  |
| 239 |  |  |  | 38.85456006 |  |  |
| 240 |  |  |  | 39.20664911 |  |  |
| 241 | 14.950266 | 0.203521 | 11.50377489 | 38.18295517 | 0.0025071 | 251.80642 |
| 242 |  |  |  | 38.53080781 |  |  |
| 243 |  |  |  | 38.30199033 |  |  |
| 244 |  |  |  | 38.03468489 |  |  |
| 245 |  |  |  | 37.57570096 |  |  |
| 246 | 23.386262 | 0.209223 | 11.81710815 | 41.61950008 | 0.0030519 | 237.1712 |
| 247 |  |  |  | 41.18812113 |  |  |
| 248 |  |  |  | 40.84824563 |  |  |
| 249 |  |  |  | 40.84709285 |  |  |
| 250 |  |  |  | 40.55947967 |  |  |
| 251 | 20.5794515 | 0.159898 | 9.152670309 | 45.71933637 | 0.0007858 | 252.96485 |
| 252 |  |  |  | 30.71101543 |  |  |
| 253 |  |  |  | 31.37932982 |  |  |
| 254 |  |  |  | 29.9715998 |  |  |
| 255 |  |  |  | 31.02125831 |  |  |


| Run No. | Roughness( $\mu \mathrm{m}$ ) | t/tc | (degrees) | (degrees) | As | Ts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 256 | 23.3734121 | 0.175254 | 10.05549407 | 49.10129007 | 0.0014318 | 233.70773 |
| 257 |  |  |  | 34.61215505 |  |  |
| 258 |  |  |  | 34.32134804 |  |  |
| 259 |  |  |  | 34.29370822 |  |  |
| 260 |  |  |  | 34.25910613 |  |  |
| 261 | 20.6853593 | 0.20024 | 11.52953691 | 44.92673638 | 0.0018762 | 232.81205 |
| 262 |  |  |  | 29.9468613 |  |  |
| 263 |  |  |  | 30.0882126 |  |  |
| 264 |  |  |  | 30.34431365 |  |  |
| 265 |  |  |  | 29.95326133 |  |  |
| 266 | 20.7577006 | 0.187073 | 10.75205775 | 47.41575244 | 0.0026801 | 215.73722 |
| 267 |  |  |  | 32.5664694 |  |  |
| 268 |  |  |  | 32.16954441 |  |  |
| 269 |  |  |  | 31.69183965 |  |  |
| 270 |  |  |  | 32.36378236 |  |  |
| 271 | 20.8684733 | 0.227355 | 13.13433213 | 42.48428541 | 0.0027505 | 235.23231 |
| 272 |  |  |  | 27.44675008 |  |  |
| 273 |  |  |  | 28.21574245 |  |  |
| 274 |  |  |  | 28.28313444 |  |  |
| 275 |  |  |  | 28.29738964 |  |  |
| 276 | 71.088548 | 0.251762 | 14.00557088 | 50.48199183 | 0.0005165 | 275.29501 |
| 277 |  |  |  | 20.15539787 |  |  |
| 278 |  |  |  | 20.91871662 |  |  |
| 279 |  |  |  | 21.08799022 |  |  |
| 280 |  |  |  | 18.68083078 |  |  |
| 281 | 79.01599 | 0.26469 | 14.79902697 | 49.95691006 | 0.0009787 | 257.53574 |
| 282 |  |  |  | 19.18822072 |  |  |
| 283 |  |  |  | 21.3446422 |  |  |
| 284 |  |  |  | 21.16935148 |  |  |
| 285 |  |  |  | 17.71731102 |  |  |
| 286 | 97.07791 | 0.242248 | 13.42561044 | 48.16836424 | 0.0016151 | 205.75187 |
| 287 |  |  |  | 18.72541568 |  |  |
| 288 |  |  |  | 19.20715874 |  |  |
| 289 |  |  |  | 18.87515773 |  |  |
| 290 |  |  |  | 20.4331013 |  |  |
| 291 | 106.87934 | 0.246883 | 13.70771943 | 46.31575535 | 0.00211 | 192.6175 |
| 292 |  |  |  | 16.28572723 |  |  |
| 293 |  |  |  | 16.9137869 |  |  |
| 294 |  |  |  | 17.39863067 |  |  |
| 295 |  |  |  | 17.30005457 |  |  |
| 296 | 107.649215 | 0.300951 | 17.05583469 | 57.45224505 | 0.0021309 | 258.15728 |
| 297 |  |  |  | 27.39271565 |  |  |
| 298 |  |  |  | 28.32214753 |  |  |
| 299 |  |  |  | 28.44161136 |  |  |
| 300 |  |  |  | 26.77228235 |  |  |


| Run No. | Roughness( $\mu \mathrm{m}$ ) | t/te | (degrees) | (degrees) | As | Ts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 301 | 121.806137 | 0.105865 | 5.845269409 | 34.84289847 | 0.0012274 | 243.7968 |
| 302 |  |  |  | 45.61353377 |  |  |
| 303 |  |  |  | 45.40801828 |  |  |
| 304 |  |  |  | 46.09032587 |  |  |
| 305 |  |  |  | 45.86390265 |  |  |
| 306 | 115.622348 | 0.136295 | 7.470094597 | 35.67586264 | 0.0019229 | 226.76377 |
| 307 |  |  |  | 45.85381127 |  |  |
| 308 |  |  |  | 45.31715513 |  |  |
| 309 |  |  |  | 45.32482235 |  |  |
| 310 |  |  |  | 44.4236793 |  |  |
| 311 | 129.862754 | 0.179254 | 9.714966585 | 33.80555492 | 0.0022223 | 247.93154 |
| 312 |  |  |  | 43.90062299 |  |  |
| 313 |  |  |  | 43.55252096 |  |  |
| 314 |  |  |  | 44.37440158 |  |  |
| 315 |  |  |  | 43.95469948 |  |  |
| 316 | 108.54511 | 0.178492 | 9.675640327 | 31.18464826 | 0.0029749 | 217.02949 |
| 317 |  |  |  | 41.95508114 |  |  |
| 318 |  |  |  | 41.01183172 |  |  |
| 319 |  |  |  | 40.67729674 |  |  |
| 320 |  |  |  | 41.22974519 |  |  |
| 321 | 103.904811 | 0.196002 | 10.57373429 | 32.13616906 | 0.003406 | 238.38043 |
| 322 |  |  |  | 42.04155916 |  |  |
| 323 |  |  |  | 42.08228092 |  |  |
| 324 |  |  |  | 41.96924183 |  |  |
| 325 |  |  |  | 41.90375002 |  |  |
| 326 | 15.744253 | 0.132415 | 7.542953922 | 41.04402325 | 0.0009522 | 283.14689 |
| 327 |  |  |  | 40.07472539 |  |  |
| 328 |  |  |  | 40.93168557 |  |  |
| 329 |  |  |  | 41.51613203 |  |  |
| 330 |  |  |  | 41.70499515 |  |  |
| 331 | 21.373276 | 0.14771 | 8.402429902 | 41.53468336 | 0.0017109 | 246.44243 |
| 332 |  |  |  | 41.49376414 |  |  |
| 333 |  |  |  | 41.55602605 |  |  |
| 334 |  |  |  | 41.85690719 |  |  |
| 335 |  |  |  | 41.66024506 |  |  |
| 336 | 37.702539 | 0.169645 | 9.628268605 | 40.15309215 | 0.0022421 | 240.69029 |
| 337 |  |  |  | 40.35494988 |  |  |
| 338 |  |  |  | 40.13132544 |  |  |
| 339 |  |  |  | 39.9342506 |  |  |
| 340 |  |  |  | 40.17398099 |  |  |
| 341 | 27.113344 | 0.18655 | 10.56705068 | 38.56577913 | 0.0027265 | 231.36113 |
| 342 |  |  |  | 38.76756981 |  |  |
| 343 |  |  |  | 38.59681483 |  |  |
| 344 |  |  |  | 38.7378555 |  |  |
| 345 |  |  |  | 38.70391014 |  |  |


| Run No. | Roughness( $\mu \mathrm{m}$ ) | t/te | (degrees) | (degrees) | As | Ts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 346 | 21.472416 | 0.20284 | 11.46629484 | 39.75564374 | 0.003144 | 261.76429 |
| 347 |  |  |  | 39.93220429 |  |  |
| 348 |  |  |  | 40.17080691 |  |  |
| 349 |  |  |  | 39.21628381 |  |  |
| 350 |  |  |  | 40.03350653 |  |  |
| 351 | 23.5926107 | 0.185254 | 10.64474123 | 42.56104242 | 0.0006767 | 267.67096 |
| 352 |  |  |  | 27.49569151 |  |  |
| 353 |  |  |  | 27.31114832 |  |  |
| 354 |  |  |  | 27.79020572 |  |  |
| 355 |  |  |  | 27.92556918 |  |  |
| 356 | 30.7779982 | 0.211193 | 12.17726827 | 39.37486468 | 0.0011852 | 239.64441 |
| 357 |  |  |  | 24.40244384 |  |  |
| 358 |  |  |  | 24.63857018 |  |  |
| 359 |  |  |  | 24.0877774 |  |  |
| 360 |  |  |  | 24.04687895 |  |  |
| 361 | 29.6081105 | 0.225462 | 13.02215933 | 43.99786953 | 0.0016642 | 250.13986 |
| 362 |  |  |  | 28.91679199 |  |  |
| 363 |  |  |  | 29.52708703 |  |  |
| 364 |  |  |  | 29.54308487 |  |  |
| 365 |  |  |  | 29.80095548 |  |  |
| 366 | 30.247557 | 0.222148 | 12.82583963 | 43.78186721 | 0.0022524 | 229.97571 |
| 367 |  |  |  | 27.89166617 |  |  |
| 368 |  |  |  | 28.5455959 |  |  |
| 369 |  |  |  | 27.88254479 |  |  |
| 370 |  |  |  | 28.28998527 |  |  |
| 371 | 37.3319742 | 0.212748 | 12.26926654 | 40.77920915 | 0.0029411 | 214.72721 |
| 372 |  |  |  | 26.83687613 |  |  |
| 373 |  |  |  | 26.74167247 |  |  |
| 374 |  |  |  | 26.90319282 |  |  |
| 375 |  |  |  | 26.62107593 |  |  |
| 376 | 80.090936 | 0.25974 | 14.49449315 | 54.89672427 | 0.0004994 | 333.06602 |
| 377 |  |  |  | 24.85781941 |  |  |
| 378 |  |  |  | 24.4132774 |  |  |
| 379 |  |  |  | 24.67182121 |  |  |
| 380 |  |  |  | 24.6226962 |  |  |
| 381 | 81.766506 | 0.285878 | 16.1122984 | 48.43719405 | 0.0009008 | 272.08272 |
| 382 |  |  |  | 18.85569715 |  |  |
| 383 |  |  |  | 15.90364506 |  |  |
| 384 |  |  |  | 16.37345565 |  |  |
| 385 |  |  |  | 16.2804337 |  |  |
| 386 | 97.385863 | 0.288517 | 16.27697499 | 45.46054437 | 0.0013379 | 251.50532 |
| 387 |  |  |  | 16.07899756 |  |  |
| 388 |  |  |  | 16.48045914 |  |  |
| 389 |  |  |  | 16.71838305 |  |  |
| 390 |  |  |  | 17.22267609 |  |  |


| Run No. | Roughness ( $\mu \mathrm{m}$ ) | t/tc | (degrees) | (degrees) | As | Ts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 391 | 127.930611 | 0.290824 | 16.42113251 | 60.04950995 | 0.0017687 | 275.53886 |
| 392 |  |  |  | 29.52299472 |  |  |
| 393 |  |  |  | 29.62167771 |  |  |
| 394 |  |  |  | 30.46315721 |  |  |
| 395 |  |  |  | 29.63910855 |  |  |
| 396 | 97.068583 | 0.306297 | 17.39225545 | 46.62663458 | 0.0020909 | 245.1935 |
| 397 |  |  |  | 16.40955704 |  |  |
| 398 |  |  |  | 15.84274896 |  |  |
| 399 |  |  |  | 15.91561355 |  |  |
| 400 |  |  |  | 15.90704706 |  |  |

## APPENDIX F

The Flow stress and Specific Horse power calculations are as shown below.

Velocity of Cut, V = 500 SFM
Width of cut, $\mathrm{w}=0.125$ inch
Uncut chip thickness, $t=0.001$ inch

Rake Angle, $\alpha=0^{\circ}$
Shear Angle, $\varphi=8.8834^{\circ}$
Cutting Force, $\mathrm{Fc}=172.4828 \mathrm{~N}=38.7756 \mathrm{lbs}$
Thrust Force, $\mathrm{Ft}=178.7172 \mathrm{~N}=40.1772 \mathrm{lbs}$

Flow Stress, $\tau=\frac{\left(F_{t} \cdot \cos (\phi) \cdot \sin (\phi)-F_{c} \sin ^{2}(\phi)\right.}{t \cdot w}=41641.8558 \mathrm{psi}$

Spindle Horse Power, $\mathrm{HP}=\frac{F_{c} \cdot V}{33,000}=0.58750909$

Material Removal Rate, $\mathrm{MRR}=\frac{\pi \cdot\left(D^{2}-D_{1}^{2}\right)}{4} . t . N=0.7226 \mathrm{inch}^{3} / \mathrm{min}$.

Specific Horse Power $=\mathrm{HP}_{\mathrm{s}}=\frac{\text { SpindleHP }}{M R R}=0.8130488 \mathrm{hp} / \mathrm{inch}^{3} / \mathrm{min}$.

Rake Angle, $\alpha=15^{\circ}$

Shear Angle, $\varphi=10.5844^{\circ}$

Cutting Force, $\mathrm{Fc}=122.6205 \mathrm{~N}=27.5661 \mathrm{lbs}$

Thrust Force, $\mathrm{Ft}=66.4581 \mathrm{~N}=14.9403 \mathrm{lbs}$

Flow Stress, $\tau=\frac{\left(F_{t} \cdot \cos (\phi) \cdot \sin (\phi)-F_{c} \sin ^{2}(\phi)\right.}{t \cdot w}=14140.1440 \mathrm{psi}$

Spindle Horse Power, $\mathrm{HP}=\frac{F_{c} \cdot V}{33,000}=0.41766818$

Material Removal Rate, $\operatorname{MRR}=\frac{\pi \cdot\left(D^{2}-D_{1}^{2}\right)}{4} . t . N=0.72266 \mathrm{inch}^{3} / \mathrm{min}$.

Specific Horse Power $=\mathrm{HP}_{\mathrm{s}}=\frac{\text { SpindleHP }}{M R R}=0.577959 \mathrm{hp} / \mathrm{inch}^{3} / \mathrm{min}$.

## APPENDIX G

## Sample Calculations:

These sample calculations are provided using the data in Run 1 (or page 88) to illustrate the exact method for data reproduction.

Friction Force, $F=F_{c} \times \sin \alpha+F_{t} \times \cos \alpha$

$$
F=175.993 \times \sin (-10)+177.7517 \times \cos (-10)=144.4904 \mathrm{~N}
$$

Normal Force, $N=F_{c} \times \cos \alpha-F_{t} \times \sin \alpha$

$$
N=175.993 \times \cos (-10)-177.7517 \times \sin (-10)=204.1855 \mathrm{~N}
$$

Shear Force along the onset of Shear Plane, $F_{s}=F_{c} \times \cos \phi-F_{t} \times \sin \phi$

$$
F_{s}=175.993 \times \cos (6.7)-177.7517 \times \sin (6.7)=154.0374 \mathrm{~N}
$$

Normal Force along the onset of Shear Plane, $F_{n}=F_{c} \times \sin \phi+F_{t} \times \cos \phi$

$$
F_{n}=175.993 \times \sin (6.7)+177.7517 \times \cos (6.7)=197.0830 \mathrm{~N}
$$

Onset of Shear Plane Angle, $\phi=\tan ^{-1}\left[\frac{r_{c} \times \cos \alpha}{1-r_{c} \times \sin \alpha}\right]$

$$
\phi=\tan ^{-1}\left[\frac{0.12189 \times \cos (-10)}{1-0.12189 \times \sin (-10)}\right]=6.704454^{\circ}
$$

Friction Angle, $\beta=\tan ^{-1}\left[\frac{F}{N}\right]$

$$
\beta=\tan ^{-1}\left[\frac{144.4904}{204.1855}\right]=35.284849^{\circ}
$$

Shear Area, $A_{s}=\frac{t \times w}{\sin \phi} ; A_{s}=\frac{0.001 \times 0.125}{\sin (6.704454)}=0.0010707 \mathrm{inch}^{2}$

Shear Stress, $\tau_{s}=\frac{F_{s}}{A_{s}}=\frac{F_{s} \times \sin \phi}{t \times w}$;

$$
\tau_{s}=\frac{154.0374}{0.0010107}=152406.6489 \mathrm{~N} / \mathrm{inch}^{2}=254.35318 \mathrm{MPa}
$$

