# MICROCONTROLLER-BASED CURRENT-MODE CONTROL 

## FOR POWER CONVERTERS

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## FOR POWER CONVERTERS

Dake He

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# MICROCONTROLLER-BASED CURRENT-MODE CONTROL FOR POWER CONVERTERS 


#### Abstract

Dake He

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Dake He , son of Bin He and Keli Li, was born on May 18, 1969 in Chengdu, China. He received a Bachelor of Science in Electrical Engineering in July, 1991 from North China Electric Power University, Baoding, China. He worked in electric power companies in China since July 1991. In September 1998, he entered Auburn University, Alabama to continue his graduate study. He received Master of Science Degree in Electrical Engineering in December 2000, and continued his Ph.D. program in Electrical Engineering at Auburn University under the guidance of Dr. R. Mark Nelms. Meanwhile, he entered Master of Business Administration (MBA) program at Auburn University Business School in August 2002, and received an MBA Degree in May 2004, with MBA Advisory Board Award. Mr. He is a member of Eta Kappa Nu, International Electrical and Computer Engineering Honor Society, and Tau Beta Pi, the Engineering Honor Society. He is the father of two daughters, Eris (Tingzhi) and Grace (Tingyu).

DISSERTATION ABSTRACT

# MICROCONTROLLER-BASED CURRENT-MODE CONTROL FOR POWER CONVERTERS 

Dake He<br>Doctor of Philosophy, in December 16, 2005<br>(M.B.A., Auburn University, 2004)<br>(M.S., Auburn University, 2000)<br>(B.S., North China Electric Power University, 1991)

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Presented in this dissertation is the implementation of microcontroller-based digital current-mode control (CMC) switch-mode power converters. A hybrid control method is proposed. By using on-board analog peripherals on the microcontroller, the current loop can be designed using analog components. A pure digital controller can be implemented in the voltage loop. Using this method, several microcontroller-based CMC systems have been constructed experimentally at relatively low cost.

Implementation issues for microcontroller-based digital controllers for CMC converters were discussed. These issues include system modeling, required
functionalities of a microcontroller, main design procedures, and $A / D$ conversion and time delay, as well as some considerations in hardware and software implementation.

This dissertation also presents fuzzy logic realizations for CMC power converters. By using lookup tables and other techniques, the fuzzy logic controllers were implemented on the microcontroller successfully.

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## Electronics Engineers

Computer software used Microsoft Word 2003, Microsoft Excel 2003, PSPICE 9.2, Microsoft Visio 2003, MATLAB 6.0 and Adobe Acrobat 7.0

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## CHAPTER 1

## Introduction

Current-mode control (CMC) has been a popular and effective control technique for power converter systems for many years. Traditional CMC systems employ pure analog components. With the development of computer technology, digital implementation of CMC systems is becoming a practical approach.

## 1-1. Basic Concept of Current-Mode Control

In many power converter systems, the output voltage of the power stage is sensed and sent to controller, as shown in Fig 1.1. By adjusting the duty cycle of the switch control signal, the output voltage is regulated. Ideally, the output voltage is identical to a reference voltage. This technique is known as "voltage-mode control" (VMC), since the duty cycle is solely determined by the error between the actual output voltage and the voltage reference.


Fig. 1.1 Concept of voltage-mode control

Another technique to regulate the power converter systems is called currentmode control (CMC) where the inductor current is directly controlled and the output voltage is controlled only indirectly. CMC, also called current-programmed control and current-injected control, has existed at least since 1978 [1-2]. A CMC power converter is typically a two-loop system (voltage loop and current loop), as shown in Fig. 1.2. The current loop, in which the inductor current is sensed as the main controlled variable, monitors and maintains the switch current (or inductor current) equal to a reference current. This reference current is obtained from the voltage loop, which compares a voltage reference to the output voltage of the power converter.

CMC has been widely used in many high-performance power supply applications in recent years, because CMC is considered to be superior to VMC due to the fast inner current loop. In a VMC power converter, any variation in input voltage or output load must alter the output voltage first, and then the controller can sense the change and react to that change by adjusting the control effort. In a CMC power converter, on the other hand, any variation in input voltage or output load can be reflected in the inductor current instantaneously. For this reason, CMC typically responds faster than a VMC power converter.


Fig. 1.2 Concept of current-mode control

A CMC power converter looks like a current source. Therefore, voltage variation at the input does not go through to the output, so a CMC power converter is more immune to an input disturbance than a VMC converter. This current source characteristic also makes it easier to parallel current sharing among several power stages. The power stages can be forced to share the load current equally by simply connecting the power stages to a common control voltage. This is very valuable in high power applications. Another advantage is that CMC converters have simpler dynamics. Their control-tooutput transfer function usually can be simplified to a first order system, and the system can be stabilized with a simpler compensation network around the error amplifier. In addition, CMC provides inherent over-current protection, since the inductor current is limited on a cycle-by-cycle basis.

Comparing Fig. 1.1 and Fig. 1.2, it can be seen that a CMC system has two control loops (voltage loop and current loop), while VMC has only one control loop (voltage loop). Therefore, CMC is more complicated in analysis and design. CMC system needs to sense or estimate the inductor current accurately. This may increase the cost and/or power loss.

Despite these advantages, CMC technology has developed very fast. In the mid 90's, Unitrode (part of Texas Instrument, Inc. today) developed a series of CMC IC chips, which drastically advanced the application of CMC power converters. Today, CMC has become a standard technology that has been applied widely.

## 1-2. Digital Control for Current-Mode Power Converters

Recently, digital control has been successfully applied to various switch-mode power converter systems [91-93]. Digital control offers several important advantages over analog control. It is easier to implement computational functions in digital control. Some of the advanced control methods are solely suitable for digital control, such as fuzzy logic control, adaptive control, optimal control, etc. Digital control is more flexible in design, is easier to revise by modifying the code, and is less sensitive to noise and environment variation. Digital control also has some important value-added features, such as system monitoring, self-diagnostics, historical data retrieving, remote communications or display. These features are very useful and suitable for power management, which is attracting more and more attention with the widespread application of portable and handheld electronic devices.

Digital control also has some disadvantages, such as sampling time delay, computation time delay, limited computation power, control loop bandwidth, and limited resolution due to finite word length of the processor and $A / D$ converter. These disadvantages may result in degradation in performance. Nevertheless, with the increasing functionality and decreasing price, digital controllers are progressively becoming a feasible and competitive option, especially in high-end switch-mode power converter systems.

CMC power converters have been successfully implemented for many years using analog circuit technology and linear system design techniques. The first current-mode control ICs emerged about two decades ago. Currently, many semiconductor companies


Fig. 1.3 Waveform of inductor current
manufacture different kinds of analog CMC IC chips. These ICs integrate together many analog components required for CMC , and makes CMC design easy and inexpensive.

Digital control, in contrast, faces a challenge in CMC systems. Fig. 1.3 is an inductor current waveform for a continuous conduction mode (CCM) power converter. This waveform has a fundamental frequency equal to the switching frequency - which can easily be in the range of hundreds of kHz . In addition, any change in input voltage or output load reflects at the inductor current instantaneously, so the dynamics of the current loop are fast. Therefore, pure digital implementation of the current loop requires a very high speed analog-to-digital (A/D) converter, or a digital processor with sufficient computational capability to estimate the inductor current.

In this dissertation, digital implementation of CMC power converter systems is investigated, and a hybrid control method is proposed. Using this method, several microcontroller-based CMC systems have been constructed at relatively low cost. This dissertation also explores the implementation of fuzzy logic control on CMC power converter systems.

### 1.3 Organization of the Dissertation

This dissertation is organized as follow:

- Chapter 2 reviews peak current-mode control and average current-mode control, and introduces the concept of the hybrid current-mode control method.
- Chapter 3 describes the design of a microcontroller-based peak current-mode control power converter system.
- Chapter 4 demonstrates the design of a microcontroller-based average currentmode control power converter system.
- Chapter 5 illustrates the design of microcontroller-based fuzzy logic currentmode control power converter systems.
- Chapter 6 presents conclusions and suggestions for future work.


## CHAPTER 2

## Hybrid Control Method for Current-Mode Power Converters

Among the different ways to implement CMC, peak current-mode control (PCMC) is probably the earliest and simplest approach, although it has some disadvantages. Average current-mode control (ACMC) overcomes those disadvantages at the expense of a more complicated design and analysis. In order to implement both of PCMC and ACMC at low cost, a hybrid control method is proposed such that microcontrollers can be used to control CMC power converters.

## 2-1. Peak Current-Mode Control (PCMC)

There are many ways to implement CMC, and peak current-mode control (PCMC) is probably the earliest and simplest approach. Fig. 2.1 is the block diagram of a PCMC power converter, and shows that a PCMC power converter is controlled with a two-loop


Fig. 2.1 Block diagram of peak current-mode control power converter system
system. The inner loop, or current loop, monitors and maintains the peak inductor current equal to a reference current $I_{\text {ref }}$. This reference current is obtained by the outer loop, or voltage loop, in which the output voltage is compared to a voltage reference.

In the current feedback loop of a PCMC converter, disturbances at the operating point gradually die out when the duty cycle is less than $50 \%$, as shown in Fig. 2.2, where $D$ is the duty cycle of the gate signal, $m_{1}$ is the current upslope, and $m_{2}$ is the down slope, $I_{0}(k)$ is the valley, and $I_{p}(k)$ is the peak of the inductor current in $k^{t h}$ switching cycle. When the duty cycle is more than $50 \%$, the current feedback loop becomes unstable, because the disturbance grows larger with each cycle. Fig. 2.3 shows the beginning of this process. This leads to large deviations from the nominal operating point and a phenomenon known as subharmonic oscillation [3].


Fig. 2.2 For duty cycles less than 0.5 , disturbances die out.


Fig. 2.3 For duty cycles greater than 0.5 , disturbances grow.

Subharmonic oscillation results in an unstable system. Unfortunately, subharmonic oscillation cannot be eliminated by simply adjusting the controller design. This can be proved mathematically. Referring to Fig. 2.2~2.3, if the switching period is $T_{s}$, then the duty cycle $D$ in $k^{\text {th }}$ switching cycle can be expressed as:

$$
\begin{equation*}
D=\frac{I_{p}(k)-I_{0}(k)}{m_{1}} / T_{s}=\frac{I_{p}(k)-I_{0}(k)}{m_{1} T_{s}} . \tag{2-1}
\end{equation*}
$$

$I_{0}(k+1)$ can be computed as:

$$
\begin{align*}
I_{0}(k+1) & =I_{p}(k)-m_{2}(1-D) T_{s} \\
& =I_{p}(k)-m_{2}\left(T_{s}-\frac{I_{p}(k)-I_{0}(k)}{m_{1}}\right)  \tag{2-2}\\
& =\left(1+\frac{m_{2}}{m_{1}}\right) I_{p}(k)-\frac{m_{2}}{m_{1}} I_{0}(k)-m_{2} T_{s}
\end{align*}
$$

Performing $z$-transform to (2-2), it changes to:

$$
\begin{equation*}
I_{0}(z)=\left(1+\frac{m_{2}}{m_{1}}\right) I_{p}(z) z^{-1}-\frac{m_{2}}{m_{1}} I_{0}(z) z^{-1} . \tag{2-3}
\end{equation*}
$$

Thus,

$$
\begin{equation*}
\frac{I_{o}(z)}{I_{p}(z)}=\frac{1+\frac{m_{2}}{m_{1}}}{z+\frac{m_{2}}{m_{1}}} \tag{2-4}
\end{equation*}
$$

Equation (2-4) has a pole at $-\frac{m_{2}}{m_{1}}$. Since both of $m_{1}$ and $m_{2}$ are positive real numbers, this pole must be at the negative real axis in $z$-plane, as shown in Fig. 2.4. In order to maintain stability, this pole must be inside unit circle, i.e., $m_{2}<m_{1}$. This condition is satisfied only when $D<0.5$.


Fig. 2.4 Location of the pole in $z$-plane

In order to stabilize the system when $D>0.5$, a ramp signal must be added to the current reference or the sensed current signal, known as slope compensation [3]. As shown in Fig. 2.5, the slope of the ramp signal, $m_{c}$, will in theory cause a disturbance to die out for any duty cycle when it is equal to or greater than half of $m_{2}$. When $m_{c}=m_{2}$, perfect rejection of disturbances on the first cycle can be achieved. However, with the increase of $m_{c}$, CMC tends to be voltage-mode control (VMC), and the advantages of CMC will be lost. For this reason, $m_{c}$ should be as small as possible, as long as it can ensure stability, and the extreme choice is:


Fig. 2.5 Slope compensation eliminates subharmonic oscillation (Ramp signal is added to current reference)

$$
\begin{equation*}
m_{c}=\frac{1}{2} m_{2} . \tag{2-5}
\end{equation*}
$$

In theory, a ramp signal with slope larger than the critical slope in (2-5) can eliminate subharmonic oscillation for duty cycle up to $100 \%$. In practice, this choice may still suffer subharmonic oscillation. For example, $m_{2}$ in a boost converter can be expressed as:

$$
\begin{equation*}
m_{2}=\frac{V_{\text {in }}-V_{\text {out }}}{L}, \tag{2-6}
\end{equation*}
$$

where $V_{\text {in }}$ is the input voltage, $V_{\text {out }}$ is the output voltage, and $L$ is the inductor value. Therefore, variation in $V_{\text {in }}$ and $V_{\text {out }}$ has a direct affect on $m_{2}$, which may result in instability when the duty cycle is high.

Indeed, slope compensation can also effectively enhance the noise immunity of a PCMC power converter system. For example, the current ripple may be very small compared to the average inductor current. At this time, a small amount of noise in the sensed current signal can result in a large variation in duty cycle, which may lead to significant jitter in the output voltage. By adding a ramp signal to the sensed current signal, the variation in duty cycle will be reduced. Therefore, slope compensation is a trade-off between stability, steady state performance and transient performance. Usually, $m_{c}$ is chosen in the range between $m_{c}=\frac{1}{2} m_{2}$ and $m_{2}$, but the optimum slope compensation is often found empirically.

The inductor current of a power converter can be either continuous or discontinuous at the nominal operating point. When the inductance is small, the inductor current goes down to zero before the end of each switching cycle, known as
discontinuous conduction mode (DCM). Since the current ramps up from zero in each switching cycle, disturbances in previous switching cycle have no any influence on the next switching cycle. Therefore, subharmonic oscillation only occurs when the power converter operates in the continuous conduction mode (CCM), so a DCM PCMC does not need slope compensation to stabilize the system. For this reason, it is more difficult and complicated to design a CCM PCMC than a DCM PCMC system. When the load or input voltage changes, the converter may transit between DCM and CCM. For generality, CCM is selected in this dissertation.

In a PCMC power converter, the switch current, as shown in Fig. 2.6, has the exactly the same peak value as the inductor current, although the switch current is zero when the switch is off. In order to reduce power loss, the switch current, instead of the inductor current, is sensed as the feedback signal.

PCMC has the advantage of fast response, especially when there is no or a little slope compensation. However, PCMC has the requirement of slope compensation when duty cycle is larger than $50 \%$. In addition to this disadvantage, PCMC has poor noise immunity. In order to solve these problems, a new method in CMC family, known as average current-mode control (ACMC), has been developed.

## 2-2. Average Current-Mode Control (ACMC)

ACMC was developed in early 90 's [4]. ACMC, just as PCMC, is also a two loop control system. The main difference is that, as illustrated in Fig. 2.7, ACMC


Fig. 2.7 Block diagram of average current-mode control power converter system
includes a compensator in the inner loop (the current loop) to average and compensate the inductor current. The desired current level, or current reference, is set by the voltage error amplifier in the outer loop (the voltage loop). The current error, or the difference between averaged current and the current reference, is amplified and compared to a sawtooth (oscillator ramp) at the comparator inputs, where the PWM control signal is generated.

In most cases, the average inductor current is proportional to the peak inductor current. Therefore, ACMC can be used to replace PCMC. The current loop compensator in an ACMC power converter acts as low-pass filter, so it can filter out switching noise while obtaining the average inductor current.

ACMC has several important advantages over PCMC. ACMC can track the average inductor current with a high degree of accuracy. As s result, ACMC is particularly suitable for power factor correction (PFC), and other applications where a constant current source is needed, since the average current is used as a controlled
quantity. ACMC eliminates the need for slope compensation, although a ramp signal is needed. This ramp signal is independent of any signal in the power stage and the controller, that is, this ramp signal starts from zero at each switching cycle with a preset (fixed) slope. At the end of each switching cycle, it is driven to zero immediately. Therefore, any current errors in previous switching cycles are washed away, and thus excellent noise immunity is achieved.

However, the advantages of ACMC are obtained at the expense of an increased complexity in design and analysis. Comparing with PCMC, ACMC has an extra compensator in the current loop. The inductor current has a triangular waveform, so the output of the current loop compensator always has some ripple. In addition, since a lowpass filter is inserted into the current loop, its dynamics are slowed down. Therefore, ACMC may have a slower transient response than PCMC, if slope compensation for the PCMC power converter does not slow down the transient response.

In order to obtain a mathematical model for design purposes, a small ripple assumption is typically employed; that is, the ripple is sufficiently small that it can be neglected. However, this assumption may not be valid when the ripple is large - for example, when the power converter is in DCM. As a result, the model may no be able to predict the system behavior correctly, and thus the controller design may be inaccurate.

## 2-3. Efforts on Digital Implementation of Current-Mode Control

Pure digital implementation of CMC must obtain the inductor current value by sampling through $\mathrm{A} / \mathrm{D}$ conversion or estimation through other parameters. As described previously, the frequency of the inductor current is the same as the switching frequency. In a pure digital controller, the inductor current can be sampled in two ways: multiple
current samples or single current sample per switching period. With multiple current samples per switching period, the peak, valley, slope, and average values of the inductor current can be computed, given the duty cycle. However, this requires very high A/D conversion speed, or multiple A/D converters, as well as high computation power. Notice that $A / D$ conversion frequency is different from and usually higher than the controller sampling frequency. That is, even if high-speed $A / D$ converter is available, the digital processor must have enough computation power to process the sampled data in one switching period.

Digital signal processors (DSPs) combined with high speed A/D converters can be a solution. Ideally, $\mathrm{A} / \mathrm{D}$ conversion and the reference current should be updated on a cycle by cycle basis. This is usually impractical for a pure digital controller. However, since the dynamics of the power stage are much slower than the switching period, the variation of the inductor current between adjacent switching cycles should be small. Therefore, the inductor current may be sampled or estimated at a frequency slower than the switching frequency.

Researchers have paid a large amount of attention to the implementation of digital CMC power converter systems. For example, in 1994, Holme and Manning developed a digital CMC scheme [5]. This digital control system consists of three sub-systems: analog data acquisition sub-system based on a high speed 12-bit A/D converter, 16-bit DSP sub-system, and PWM sub-system consisting of counter circuits, latches and flipflops. Obviously, this early attempt had severe drawbacks because of complicated hardware, high cost and low reliability.

With the development of microelectronics technology and computer technology, the functionality of a DSP has improved significantly with drastically decreased cost. Today, many DSPs integrate analog/digital interfaces, PWM generators, and signal processing unit onto a single chip. In addition, because of the powerful computational ability of a DSP, the inductor current value of a switching-mode power converter can be estimated instead of direct measurement, and the required calculations can be completed in one switching cycle. As a result, digital implementation of CMC is becoming a practical approach.

For example, using sensorless CMC [6-8] and predictive CMC [9] techniques, Kelly and Rinne proposed a solution for digital CMC using a 16-bit DSP [10]. The inductor current is estimated from the measured load voltage of dc-dc converters and the current estimation of previous switching cycles. Indeed, this method is an observer-based control system where a state variable (inductor current) is observed. When using this approach, the time delay for current estimation and calculation should not last more than three or four switching cycles. Longer time delay results in not only more complicated parameter estimation, but also large estimation error. Therefore, a DSP should have sufficient computational capability to estimate the inductor current fast enough.

However, the high cost of a DSP and the associated hardware seriously restricts its applications. Though cheaper, microcontrollers usually are not fast enough to perform A/D conversion and computation to estimate the required parameters. Therefore, it would be very difficult to construct a pure digital CMC system using a microcontroller. However, a microcontroller can be integrated with some analog peripherals that can
compensate for the limitation in computing power while expanding the functionalities at low cost.

## 2-4. Hybrid Current-Mode Control Method

As depicted previously, the fast dynamics of the current loop put forward a difficult challenge for digital implementation of the current loop. Accordingly, analog implementation of the current loop is much easier and more cost-effective than a digital implementation.

In contrast, the dynamics of the voltage loop are much slower than that of the current loop mainly because of the energy storage components (inductors and capacitors) in the power stage. For example, the resonant frequency $\omega_{0}$ of the power stage (buck or boost) can be expressed as:

$$
\begin{equation*}
\omega_{0}=\frac{1}{\sqrt{L C}} \tag{2-7}
\end{equation*}
$$

where $L$ is the inductor value and $C$ is the capacitor value. Equation (2-7) suggests that the power stage bandwidth can be just few kilohertz. As a result, a standard digital compensator can be used in the voltage loop straightforwardly.

Some microcontrollers have on-board analog features such as operational amplifiers and comparators. By using these analog features, the current loop contains only analog signals. Hence, this "analog" current loop combines with a "digital" voltage loop to construct a hybrid controller. Fig. 2.8 is an example of a microcontroller to control a hybrid CMC power converter.

Fig. 2.8 indicates that the microcontroller should contain some required peripherals before it is suitable as a hybrid CMC controller. An on-board A/D converter


Fig. 2.8 Block diagram of hybrid current-mode control power converter system
is required to convert the output voltage signal into a digital value. Since the output voltage has relatively slow dynamics, the voltage change in adjacent switching cycles is small. Therefore, A/D conversion for the output voltage does not have to be performed on a cycle-by-cycle basis. Instead, the output voltage can be sampled every several switching cycles, as long as the sampling frequency is much higher than the crossover frequency of the power stage. Therefore, the on-board A/D converter does not have to be very fast, since it will not be used to sample the inductor current.

In the current loop, an analog comparator is indispensable. In peak current-mode control (PCMC), this comparator is used to generate a gate signal by comparing the peak value of the inductor current signal to the reference current obtained by the voltage loop. Since the output of the voltage loop is the reference current of the analog comparator in the current loop, the comparator should have a digitally programmable reference, or a D/A converter is required to convert the digital signal in the voltage loop to an analog
signal. For ACMC , this comparator is used to generate the gate signal by comparing a ramp signal to the computed control effort. Therefore, an on-board comparator is required for both PCMC and ACMC to implement a hybrid control method.

For ACMC , an analog operational amplifier is required in the current loop to average the current signal. Since the input of the operational amplifier is the output of the voltage loop, a $\mathrm{D} / \mathrm{A}$ converter is required to convert the digital signal in the voltage loop to an analog signal.

It is desired to have a PWM module inside the microcontroller when the converter operates at a constant switching frequency. An on-board PWM module can make the procedure to generate the gate signal simpler and more reliable. Without a PWM module, a timer must be used as an interrupt source to set the switching frequency. Many microcontrollers do not have priority levels in their interrupt sources. In order to ensure constant switching frequency, no other interrupt can be allowed, which may increase the difficulty in the software design.

As described previously, a PCMC converter has subharmonic oscillation problem, and slope compensation is required to stabilize the system. In hybrid control, the current loop is made of analog components, so the signal in the current loop is noisy, just like a pure analog control. Therefore, slope compensation is necessary in hybrid control. The microcontroller should have the mechanism to generate a synchronous ramp signal to implement slope compensation to stabilize the system when the duty cycle exceeds $50 \%$. In ACMC, a synchronous ramp signal is also required as the reference to generate the gate signal. Therefore, a mechanism to generate a synchronous ramp signal is required for both PCMC and ACMC to implement hybrid control method.

The output voltage $V_{o}$ of a boost converter can be expressed as:

$$
\begin{equation*}
V_{o}=\frac{1}{1-D} V_{i n}=\frac{1}{D^{\prime}} V_{i n} \text {, } \tag{2-8}
\end{equation*}
$$

Equation (2-8) shows that $V_{o}$ is proportional to $D^{\prime}$. However, when $D$ is above $80 \sim 85 \%$, (2-8) is no longer valid, because $V_{o}$ will decrease with an increased $V_{i n}$ when the duty-cycle $D$ is above approximately $85 \%$. Fig. 2.9 shows the relationship between output voltage and duty cycle [11], which indicates that a boost converter has two operating point for a given $V_{o}$. Obviously, one of the operating points is not stable, so $D$ must be limited to less than $85 \%$ to ensure proper operating conditions. Therefore, for a boost converter, a mechanism is needed to limit the maximum duty cycle.

The above analysis shows that the microcontroller used in hybrid CMC should have comprehensive analog peripherals. Key peripherals include: an A/D converter, a D/A converter, an analog comparator, a PWM module, a mechanism to generate ramp signal, and a mechanism to limit the maximum duty cycle. For ACMC, an analog


Fig. 2.9 Output voltage change with duty cycle for a boost converter [11]
operational amplifier is also desired. Although it is easy to find microcontrollers that contain some of the desired peripherals, it is not trivial to select an appropriate microcontroller that contains all the required functionalities. For example, in [12], a PCMC boost converter is controlled by a microcontroller, the PIC14000, which contains an on-board analog comparator. However, the PIC14000 does not have PWM module, so external components are required to a generate PWM signal and to limit the maximum duty cycle. Also, this system can only operate in the discontinuous conduction mode (DCM), since it has no slope compensation. Although slope compensation can be implemented in this system, more external components have to be added into the system. In [13], a single phase power factor correction system using an ACMC technique is controlled by a hybrid controller. This controller has a microcontroller (the PIC16F887A) to control the voltage loop. An external 512 kB EPROM is connected to the PIC16F887A to store a lookup table. In the current loop, an analog IC chip UC3854 is implemented to control the inductor current. In the above two examples, extra external components are added to compensate for the deficiency of computation power of the microcontrollers. The hybrid controllers using this approach have the disadvantages of more complicated circuit, less reliability and higher cost than pure analog controller due to the extra components used in the circuits. Therefore, it is important to select appropriate microcontrollers that contain required analog peripheral features.

As long as an appropriate microcontroller can be selected, the hybrid CMC method combines the advantages of analog control and digital control. It can handle a high frequency current signal, while maintaining simplicity and flexibility in design. Because the fast current loop contains only analog signals, performance will not be
sacrificed. Advanced digital control techniques can be implemented in the voltage loop compensator. The current loop design is very similar to analog controllers, so design methods and guidelines are fully established. Meanwhile, the analog current loop is not simply an addition to the digital voltage loop. Since the analog signal and components are inside the microcontroller, they are controlled by the microcontroller directly. For this reason, the resulting system still can maintain the valued added features of digital controllers, and have the full potential for power management. Compared to DSP-based systems, this microcontroller-based system has lower cost.

## 2-5. The PIC16C782 Microcontroller

The PIC16C782 from Microchip Inc. is an 8-bit microcontroller and is released in 2001 [14]. Fig 2.10 illustrates the pin diagram of the PIC16C781/782 devices. The only difference between the PIC16C781 and the PIC16C782 is that the PIC16C781 has $1 \mathrm{~K} \times$ 14 on-board program memory while the PIC16C782 has $2 \mathrm{~K} \times 14$. The PIC16C782 has a 13-bit program counter capable of addressing an $8 \mathrm{~K} \times 14$ program memory space. Accessing a location above the physically implemented address causes a wraparound.

The maximum clock frequency for this 20 pin microcontroller is 20 MHz . Its instruction cycle is 4 times a clock cycle, or 200 ns with a 20 MHz clock frequency. It has


Fig. 2.10 Pin diagram of the PIC16C781/782 [141
a RISC (Reduced Instruction Set Computer) CPU core with only 35 single word instructions. Each instruction word has 14 bits. These instructions can be completed in a single instruction cycle, except for program branches which need two instruction cycles.

The PIC16C782 has 128 general purpose registers and 39 special function registers. All the registers are 8 -bit. The data memory is partitioned into four banks, which contain the General Purpose Registers and the Special Function Registers. Each bank extents up to 128 bytes with some unimplemented bytes. The lower locations of each bank are reserved for the Special Function Registers. Some frequently used Special Function Registers from one bank are mirrored in other banks for code reduction and quicker access. The General Purpose Registers are at the higher locations of each bank, and are implemented as static RAM.

The PIC16C782 has totally 16 I/O pins, 8 of them can be either analog or digital input pins. It has up to 8 internal/external interrupt sources without priority. When an interrupt occurs, it blocks all other interrupt sources.

The PIC16C782 has many peripheral features, and many of these features are critical in a hybrid CMC implementation. Following is a list of important peripheral features included in the PIC16C782:

- Two Timers
- Timer 0: 8-bit timer/counter with 8-bit prescaler
- Enhanced Timer 1: 16-bit timer/counter with prescaler
- Analog-to-Digital Converter (ADC): 8-bit resolution; programmable 8channel input
- Digital-to-Analog Converter (DAC): 8-bit resolution; reference from AVDD, VREF1, or VR module; output configurable to VDAC pin, comparators, and ADC reference
- Analog Operational Amplifier Module (OPA): firmware initiated input offset voltage Auto Calibration module; programmable Gain Bandwidth Product (GBWP)
- Dual Analog Comparator Module (C1 and C2): programmable speed and output polarity; fully configurable inputs and outputs; reference from DAC, or VREF1/VREF2 pins
- Voltage Reference Module (VR): 3.072V +/- $0.7 \%$ @ $25^{\circ} \mathrm{C}$, AVDD $=5 \mathrm{~V}$; configurable output to ADC reference, DAC reference, and VR pin; 5 mA sink/source
- Programmable Switch Mode Controller Module (PSMC): PWM and PSM modes; programmable switching frequency; slope compensation output available; programmable minimum and maximum duty cycle.

These peripheral features of the PIC16C782 indicate that this microcontroller can be used for a hybrid CMC system. Fig. 2.11 illustrates the connections of the analog peripherals inside the PIC16C782 [14]. These analog components are integrated inside the chip, and can be configured and controlled by the microcontroller through multiplexers and control bits.

However, the PIC16C782 has limited computational ability that imposes challenges in hardware and software design. When the PIC16C782 was selected to implement hybrid current-mode control, there were some common issues in hardware and


Fig. 2.11 Analog multiplexing diagram of the PIC16C781/782 [14]
software design that had to be taken into account. For example, the PIC16C782 does not have multiplication/division instructions. Instead, it has only 8-bit unsigned addition/ subtraction instructions. Therefore, the software to perform direct multiplication/division calculations can be very complicated and very time-consuming to execute. Therefore, direct multiplication/division is not practical for on-line control of power converters, and must be avoided. One solution is to employ power-of-two arithmetic, where multiplication/division can be done by simply shifting register bits left/right. However, this arithmetic may limit the available gains, and hence may degrade the performance.

The PIC16C782 does not have a sign bit. No negative numbers can exist in the system, and the software must keep track of the sign during calculation procedure, which increases the size and complexity of the code considerably.

Although the PIC16C782 has the ability to address 8 kB program memory, it has a limited internal memory space of 2 kB . External memory can increase the cost and complexity of the circuit considerably. Therefore, the software must be concise and should be limited to 2 kB of size.

The ADC module for the PIC16C782 captures a snapshot of the scaled output voltage and holds it for an $\mathrm{A} / \mathrm{D}$ conversion. Because of the limited sampling rate and computation power of the PIC16C782, switching noise in the output voltage must be avoided or filtered out in "hardware" instead of by a digital filter to ensure on-time control. Therefore, the output voltage should be sampled during the period that has minimum switching noise, and the sampling moment must be controlled precisely. This can be achieved by sending back the PWM signal to an I/O pin to trigger an interrupt that starts an $A / D$ conversion. As a result, the sampling moment can be controlled, and the
output voltage can always be captured at a fixed point in the switching cycle after the switching noise has subsided. However, the PIC16C782 does not have priority levels for interrupts, so any other interrupt can interfere with the correct timing. In order to ensure the proper sampling moment, an interrupt from any other source should not be allowed. When the oscillator frequency is 20 MHz , an $\mathrm{A} / \mathrm{D}$ conversion cycle requires $15.2 \mu \mathrm{~s}$, which equals 2.375 switching cycles. Typically, this is much faster than the total calculation time. Therefore, the controller sampling frequency is directly determined by the speed of the calculations instead of $A / D$ conversion speed.

Although the PIC16C782 has limited computational ability, its adequate analog peripheral features can largely overcome its weakness. Therefore, it has been selected to implement various hybrid current-mode control schemes [15-20].

## 2-6. Digital Controller Design

When using a hybrid CMC method, the voltage loop compensator is indeed a typical digital controller. Therefore, digital control techniques are needed to design the voltage loop. The voltage loop compensator is a standard digital controller, and can be designed in either the $s$-domain or the $z$-domain. When designing the digital controller in the $s$-domain (emulation method), the controller $G_{c}(s)$ is first designed directly in $s$ domain just as an analog control system. Then $G_{c}(s)$ is mapped to $G_{c}(z)$ in the $z$-domain. In contrast, when designing the digital controller in the $z$-domain, the analog plant $G_{p}(s)$ is mapped to $G_{p}(z)$ first, then direct digital design techniques are utilized to design a digital controller $G_{c}(z)$ directly. In both cases, analog systems (plants or controllers) need to be mapped into digital systems.

There are many existing mapping methods to perform mapping from the $s$-domain to the $z$-domain [21-22]. These methods can be clarified into three categories: matched pole-zero methods, input hold methods (zero-order-hold and first-order-hold) and numerical approximations. Followings are some of the commonly used methods to perform this transformation, given $T$ as the sampling period:

1. Standard $z$-transform (matched pole-zero method).

The standard $z$-transform method is suitable only for band-limited signals with maximum frequency less than half of the sampling frequency. It can be expressed as:

$$
\begin{equation*}
z=e^{s T} \text { or } s=\frac{1}{T} \ln z \tag{2-9}
\end{equation*}
$$

The standard $z$-transform method requires a partial-fraction expression to complete the mapping of

$$
\begin{equation*}
\frac{1}{s+a} \rightarrow \frac{1}{1-e^{-a T} z^{-1}} \tag{2-10}
\end{equation*}
$$

In order to simplify the calculation, a simplified matched pole-zero method can be used to perform the mapping:

$$
\begin{equation*}
s+a \rightarrow 1-e^{-a T} z^{-1} \tag{2-11}
\end{equation*}
$$

The simplified matched pole-zero method achieves a one to one mapping of poles and zeros. This method produces the same poles as the standard $z$-transform, but the zeros are different. As a result, the simplified matched pole-zero method can be used on non-band-limited inputs. This method is especially useful to transform an analog controller/filter to an equivalent digital controller/filter.
2. Zero-order-hold $(\mathrm{ZOH})$.

The transfer function of a ZOH can be expressed as:

$$
\begin{equation*}
G_{Z O H}(s)=\frac{1-e^{-s T}}{s} \tag{2-12}
\end{equation*}
$$

Thus, $G_{p}(z)$, the mapping of analog system $G_{p}(s)$ using ZOH method, can be expressed as:

$$
\begin{equation*}
\left.G_{p}(z)=\vartheta\left[G_{p}(s) \frac{1-e^{-s T}}{s}\right]=\frac{z-1}{z}\right\}\left[\frac{G_{p}(s)}{s}\right], \tag{2-13}
\end{equation*}
$$

where $\mathcal{Z}$ represents the standard $z$-transform. $G_{p}(z)$ is known as a pulse transfer function. The ZOH method is commonly used to transform an analog plant to its digital representation to design its digital controller in the $z$-domain.
3. Numerical approximations.

By using difference equations to approximate integral and differential equations, numerical approximation methods can be used to transform designed analog controllers or filters to digital ones. The forward rule, backward rule and trapezoidal rule are several of the most commonly used numerical approximation methods:

- Forward rule. The forward rule can be expressed as:

$$
\begin{equation*}
s=\frac{z-1}{T} . \tag{2-14}
\end{equation*}
$$

The forward rule maps the left half-plane in the $s$ - plane to the region of left side of $z=1$ in the $z$-plane, so some stable analog designs may be unstable when they are mapped to the $z$-plane.

- Backward rule. The backward rule can be expressed as:

$$
\begin{equation*}
s=\frac{(z-1)}{z T} . \tag{2-15}
\end{equation*}
$$

The back rule maps the left half-plane in the $s$-plane to a circle inside the unit circle in the $z$-plane. Therefore, stable analog designs always yield stable digital designs. Indeed, even some unstable analog designs result in stable digital designs.

- Trapezoidal (Tustin/Bilinear) rule. The trapezoidal rule can be expressed as:

$$
\begin{equation*}
s=\frac{2}{T} \frac{(z-1)}{(z+1)} . \tag{2-16}
\end{equation*}
$$

This rule maps the left half-plane in the $s$-plane to the region inside the unit circle in the $z$-plane, and the imaginary axis is mapped to the unit circle.

When the sampling frequency is high enough, all of the above methods can deliver similar mapping results.

Traditional analog control systems are designed in the $s$-domain, and there are many familiar and mature design methods. The emulation method is useful to transform existing analog designs into digital ones. Some designers prefer the emulation method because they are familiar with $s$-domain techniques. When A/D conversion speed and controller calculation are small compared to the sampling period, one may neglect the sampling effect and design the controller in the $s$-domain, and then transform the design into the digital domain using some of the mapping methods described above, i.e., matched pole-zero method and numerical approximation. The emulation method ignores $\mathrm{A} / \mathrm{D}$ conversion delay and controller time delay. Therefore, the emulation method is an approximate approach to design digital controllers,

Notice that the $A / D$ conversion delay and controller time delay are different from the actual sampling period. The $A / D$ conversion delay is the time required for an $A / D$ converter to perform an $\mathrm{A} / \mathrm{D}$ conversion. Controller time delay is derived from the time required to compute the control effort. In many low-speed systems, the actual sampling period may be much longer than $A / D$ converter sampling and controller time delay, so the time delay due to the $\mathrm{A} / \mathrm{D}$ conversion and computation can be ignored. Sampling and computation delay introduce additional phase shift. When the sampling period is close to the $\mathrm{A} / \mathrm{D}$ conversion delay or controller time delay, this phase shift may not be negligible any more. At this time, the phase margin is reduced, and the system may show more overshoot, or even be unstable. Therefore, more phase margin is desired when designing a digital controller using the emulation method.

Indeed, it is more desirable to design digital controllers directly in the $z$-domain. When using this method, the analog system transfer function $G_{p}(s)$ is transformed to the $z$-domain first. A ZOH is commonly used method to perform the mapping, and the mapping can be expressed as (2-13). Note that (2-13) ignores the time delay due to $\mathrm{A} / \mathrm{D}$ conversion and computation.

However, in power converter applications, in order to achieve fast response, it is desired to update the control effort as soon as possible, ideally on a cycle-by-cycle basis. Since the switching frequency can easily be in the hundreds of kilohertz, so the sampling frequency is at least several kilohertz. In this case, the $\mathrm{A} / \mathrm{D}$ conversion time delay or controller time delay usually directly determines the possible maximum sampling frequency, and the overall time delay should be the maximum of $\mathrm{A} / \mathrm{D}$ conversion delay and controller time delay. Typically, the controller time delay is mush longer than the
$\mathrm{A} / \mathrm{D}$ conversion time. This time delay should be considered when mapping $G_{p}(s)$ to the $z$-domain, and can be expressed as $e^{-s T_{d}}$ in the $s$-plane, where $T_{d}$ is the controller time delay. In this case, the sampling period equals the overall time delay, plus a short slice of waiting time to start the next sampling for a fixed sampling frequency. When using ZOH method, $G_{p}(z)$, the mapping of $G_{p}(s)$, can be expressed as:

$$
\begin{equation*}
G_{p}(z)=\vartheta\left[G_{p}(s) \frac{1-e^{-s T}}{s} e^{-s T_{d}}\right] . \tag{2-17}
\end{equation*}
$$

When the time slice is short enough to be ignored, the time delay $T_{d}$ approximately equals the sampling period $T$. Thus, (2-17) is converted to:

$$
\begin{equation*}
G_{p}(z)=\mathcal{G}\left[G_{p}(s) \frac{1-e^{-s T}}{s} e^{-s T}\right]=\frac{z-1}{z^{2}} \mathcal{Z}\left[\frac{G_{p}(s)}{s}\right] . \tag{2-18}
\end{equation*}
$$

Once $G_{p}(z)$ is obtained, it can be used to design the digital controller $G_{c}(z)$ using design techniques like $z$-domain root locus. Some existing $s$-domain techniques, such as Bode plot and Routh-Hurwitz criterion, cannot be used in the $z$-domain directly. In order to using those techniques, $G_{p}(z)$ needs to be transformed to $G_{p}(w)$ :

$$
\begin{equation*}
G_{p}(w)=\mathscr{\omega}\left\{G_{p}(z)\right\}=\left.G_{p}(z)\right|_{z=\frac{1+(T / 2) w}{1-(T / 2) w}} . \tag{2-19}
\end{equation*}
$$

Equation (2-19) indicates a bilinear transformation, which maps the region inside the unit circle in the $z$-plane to the left half-plane in the $w$-plane. In the $w$-plane, those familiar techniques can be used to design the digital controller $G_{c}(w)$. After $G_{c}(w)$ is designed, it needs to be transformed back to the $z$-plane:

$$
\begin{equation*}
G_{c}(z)=\xi\left\{G_{c}(w)\right\}=\left.G_{c}(w)\right|_{w=\frac{z z-1}{T} \frac{z+1}{z+1}} . \tag{2-20}
\end{equation*}
$$

MATLAB is a powerful tool to perform various transformations. In addition, MATLAB can be used to design digital controllers directly and conveniently. For example, the SISO Design Tool, which is opened by command sisotool( ), can be used for this purpose [23]. Its graphical user interface allows a user to design single-input/single-output (SISO) compensators by putting zeros and poles visually and freely in the root locus or Bode and Nichols plots of the open-loop system, and getting the controller directly.

In Chapter 3 and Chapter 4, a method which combines the direct digital design method and the emulation method is proposed to design the digital controllers. In this method, the analog plant $G_{p}(s)$ is transformed to $G_{p}(z)$ just as in the direct digital design method. In this procedure, the effects of time delay and ZOH are included. Instead of designing the controller in the $z$-plane or the $w$-plane, the controller is designed in the $s$ domain. In MATLAB, command bode( ) plots the Bode diagram of a model. When the model is a discrete-time transfer function, bode( ) maps the model into the $s$-plane using $z=e^{j \omega T}$. This procedure is equivalent to map $G_{p}(z)$ back to the $s$-plane, with the effects of time delay and ZOH. Based on the Bode diagram, the controller $G_{c}(s)$ can be designed. Then, using a numerical approximation, $G_{c}(s)$ is converted to $G_{c}(z)$. This method has the advantage of emulation method that some existing design techniques like a Bode diagram can be used directly without mapping to the $w$-plane. Meanwhile, the proposed method considers the effects of time delay and ZOH , and thus can result in a more accurate design.

When $G_{c}(z)$ is obtained, it needs to be transformed to difference equations to realize the control law. There are unlimited ways to realize the control law. $G_{c}(z)$ is essentially a digital filter, and can be represented by simulation diagram. Many digital filter structures can be used to construct the simulation diagram [21]. The third direct structure (3D) is one of the commonly used methods. When using this method, $G_{c}(z)$ can be written as:

$$
\begin{equation*}
G_{c}(z)=\frac{V_{c}(z)}{E(z)}=\frac{\sum_{i=0}^{n} a_{i} z^{-i}}{\sum_{i=0}^{n} b_{i} z^{-i}} . \tag{2-21}
\end{equation*}
$$

where $V_{c}(z)$ is the controller output, and $E(z)$ is the controller input. Therefore,

$$
\begin{equation*}
V_{c}(z)=\sum_{i=0}^{n} a_{i} z^{-i} E(z)-\sum_{i=1}^{n} b_{i} z^{-i} V_{c}(z) . \tag{2-22}
\end{equation*}
$$

In time domain, (2-22) can be expressed as:

$$
\begin{equation*}
v_{c}(k)=\sum_{i=0}^{n} a_{i} e(k-i)-\sum_{i=1}^{n} b_{i} v_{c}(k-i) . \tag{2-23}
\end{equation*}
$$

Another commonly used method is to transform analog systems into discrete state-space representations, and then use pole placement or other techniques to design the digital controller. There are two approaches to perform the transformation to the discrete state space model. In the first approach, the discrete state-space model is obtained from $z$-domain transfer function $G_{p}(z)$. At first, a simulation diagram for $G_{p}(z)$ is obtained based on the selected digital filter structure. Then, the state-space model can be derived from the simulation diagram. Some typical state space representations can be directly
written out based on $G_{p}(z)$ without the assistance of a simulation diagram. For example, if $G_{p}(z)$ can be expressed as:

$$
\begin{equation*}
G_{p}(z)=\frac{b_{n-1} z^{n-1}+\ldots+b_{1} z+b_{0}}{z^{n}+a_{n-1} z^{n-1}+\ldots+a_{1} z+a_{0}} \tag{2-24}
\end{equation*}
$$

then its controllable canonical form can be expressed as:

$$
\begin{align*}
& {\left[\begin{array}{c}
x_{1}(k+1) \\
x_{2}(k+1) \\
\vdots \\
x_{n-1}(k+1) \\
x_{n}(k+1)
\end{array}\right]=\left[\begin{array}{ccccc}
0 & 1 & \cdots & 0 & 0 \\
0 & 0 & \cdots & 0 & 0 \\
& \vdots & & \ddots & \\
0 & 0 & \cdots & 0 & 1 \\
-a_{0} & -a_{1} & \cdots & -a_{n-2} & -a_{n-1}
\end{array}\right]\left[\begin{array}{c}
x_{1}(k) \\
x_{2}(k) \\
\vdots \\
x_{n-1}(k) \\
x_{n}(k)
\end{array}\right]+\left[\begin{array}{c}
0 \\
0 \\
\vdots \\
0 \\
1
\end{array}\right] u(k)}  \tag{2-25}\\
& y(k)=\left[\begin{array}{lllll}
-b_{0} & -b_{1} & \cdots & -b_{n-2} & -b_{n-1}
\end{array}\right]\left[\begin{array}{c}
x_{1}(k) \\
x_{2}(k) \\
\vdots \\
x_{n-1}(k) \\
x_{n}(k)
\end{array}\right]
\end{align*}
$$

Another approach to obtain a discrete state-space model is to compute it from the continuous state-space model. If the continuous state space model is expressed as:

$$
\begin{align*}
& X(t)=A X(t)+B U(t) \\
& Y(t)=C X(t) \tag{2-26}
\end{align*}
$$

then the discrete model can be expressed as:

$$
\begin{aligned}
& X(k+1)=A_{d} X(k)+B_{d} U(k) \\
& Y(k)=C_{d} X(k)
\end{aligned}
$$

where :

$$
\begin{align*}
& A_{d}=\Phi(T)=\mathfrak{L}^{-1}\left[(s I-A)^{-1}\right]_{t=T}  \tag{2-27}\\
& B_{d}=\left[\int_{0}^{T} \Phi(T-\tau) d \tau\right] B \\
& C_{d}=C
\end{align*}
$$

The transformation also can be easily realized using MATLAB. As long as a discrete state-space model is obtained, the digital controller can be designed directly based on the model. Pole placement is one of the commonly used methods to design the controllers. Desired poles are mapped from the $s$-plane to the $z$-plane using $z=e^{s T}$, and then the feedback gain matrix $K$ is selected to ensure that the eigenvalues of $\left[A_{d}-B_{d} K\right]$ equal the desired poles. Observers are usually needed to estimate the states.

The state-space control method, also know as the modern control method, has become a very powerful approach to analyze and design control systems. However, state-space control method usually requires a more accurate system model. In addition, this method usually involves many floating point calculations and its feedback gains need to be accurate. Therefore, the state-space control method may be difficult to apply to illdefined systems. For nonlinear power converter systems, their transfer functions are approximations. Even worse, their transfer functions may change with operating conditions. Microcontrollers usually have limited resolution and computation capacity. Therefore, when using microcontrollers to control power converter systems, state space control method may not be able to compute an accurate control effort fast enough to ensure proper operation of the power stage. Therefore, the state-space control method is not used in this dissertation. Though, it is still useful to analyze the systems off-line.

## 2-7. Boost Converter

Boost converter is one of the basic dc-dc converter topologies. It can produce an output voltage higher than the input voltage. However, the boost converter has a righthalf plane zero in its control-to-output transfer function. Thus, it has a more complicated dynamics than other simple topologies. In addition, as discussed previously, the
maximum duty cycle of a boost converter must be limited to ensure stability. For generalization, boost converter is selected in this research.

Fig. 2.12 illustrates a boost converter. Obviously, a boost converter is a timevarying nonlinear system because of the switching behavior in the circuit. In order to obtain the transfer function of the boost converter for design purposes, the system must be linearized first. Usually, the averaged switch model [3] is used to derive the transfer function. In order to simplify the derive process, ESRs of the inductor and the output capacitor are ignored.

A boost converter can be viewed as Fig. 2.13, in which Fig. 2.12 is split into two states: the switch is closed and the switch is opened. In each state, the system is linear. Fig. 2.13 (a) can be expressed as:

$$
\begin{equation*}
C \frac{d v_{o}}{d t}=-\frac{v_{o}}{R}, \text { and } L \frac{d i_{L}}{d t}=v_{i n} . \tag{2-28}
\end{equation*}
$$



Fig. 2.12 A boost converter


Fig. 2.13 Boost converter: (a) switch is closed, (b) switch is opened

That is:

$$
\frac{d}{d t}\left[\begin{array}{c}
v_{o}  \tag{2-29}\\
i_{L}
\end{array}\right]=\left[\begin{array}{cc}
-\frac{1}{R C} & 0 \\
0 & 0
\end{array}\right]\left[\begin{array}{c}
v_{o} \\
i_{L}
\end{array}\right]+\left[\begin{array}{c}
0 \\
\frac{1}{L}
\end{array}\right] v_{i n} .
$$

Fig. 2.13 (b) can be written as:

$$
\begin{equation*}
C \frac{d v_{o}}{d t}=i_{L}-\frac{v_{o}}{R}, \text { and } L \frac{d i_{L}}{d t}=v_{i n}-v_{o} . \tag{2-30}
\end{equation*}
$$

That is:

$$
\frac{d}{d t}\left[\begin{array}{c}
v_{o}  \tag{2-31}\\
i_{L}
\end{array}\right]=\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{1}{C} \\
-\frac{1}{L} & 0
\end{array}\right]\left[\begin{array}{c}
v_{o} \\
i_{L}
\end{array}\right]+\left[\begin{array}{c}
0 \\
\frac{1}{L}
\end{array}\right] v_{i n}
$$

Using the averaged switch model, when the duty cycle is $D$, the average of (2-29) and (2-31) can be expressed by:

$$
\begin{gather*}
\frac{d}{d t}\left[\begin{array}{c}
v_{o} \\
i_{L}
\end{array}\right]=d\left(\left[\begin{array}{cc}
-\frac{1}{R C} & 0 \\
0 & 0
\end{array}\right]\left[\begin{array}{l}
v_{o} \\
i_{L}
\end{array}\right]+\left[\begin{array}{l}
0 \\
\frac{1}{L}
\end{array}\right] v_{i n}\right)+d^{\prime}\left(\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{1}{C} \\
-\frac{1}{L} & 0
\end{array}\right]\left[\begin{array}{l}
v_{o} \\
i_{L}
\end{array}\right]+\left[\begin{array}{l}
0 \\
\frac{1}{L}
\end{array}\right] v_{i n}\right) \\
\Rightarrow \frac{d}{d t}\left[\begin{array}{l}
v_{o} \\
i_{L}
\end{array}\right]=\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{d^{\prime}}{C} \\
-\frac{d^{\prime}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
v_{o} \\
i_{L}
\end{array}\right]+\left[\begin{array}{c}
0 \\
\frac{1}{L}
\end{array}\right] v_{\text {in }} . \tag{2-32}
\end{gather*}
$$

For large signals, $v_{i n}=V_{i n}, v_{o}=V_{o}, i_{L}=I_{L}, d=D$ and $d^{\prime}=D^{\prime}$ all are constant, so:

$$
\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{D^{\prime}}{C}  \tag{2-33}\\
-\frac{D^{\prime}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
V_{o} \\
I_{L}
\end{array}\right]+\left[\begin{array}{c}
0 \\
\frac{1}{L}
\end{array}\right] V_{i n}=0
$$

That is:

$$
\left\{\begin{array}{l}
\frac{V_{o}}{V_{i n}}=\frac{1}{D^{\prime}}  \tag{2-34}\\
I_{L}=\frac{V_{o}}{R D^{\prime}}
\end{array} .\right.
$$

Equation (2-34) is the familiar large-signal dc model for the boost converter. Average small-signal ac model for a boost converter can also be obtained through (2-32). In order to obtain the control effort to output transfer function, $G_{v d}(s)=\frac{\hat{v}_{o}(s)}{\hat{d}(s)}$, it is assumed $v_{i n}=V_{i n}=$ constant. When there is a positive duty cycle perturbation $D+\hat{d}$ (which is equivalent to $D^{\prime}-\hat{d}$ ), both $v_{o}$ and $i_{L}$ will increase a little bit. Thus, (2-32) can be written as:

$$
\frac{d}{d t}\left[\begin{array}{c}
\hat{v}_{o}  \tag{2-35}\\
\hat{i}_{L}
\end{array}\right]=\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{D^{\prime}-\hat{d}}{C} \\
-\frac{D^{\prime}-\hat{d}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
V_{0}+\hat{v}_{o} \\
I_{L}+\hat{i}_{L}
\end{array}\right]+\left[\begin{array}{c}
0 \\
\frac{1}{L}
\end{array}\right] V_{i n} .
$$

Rearrange (2-35), following equation can be obtained:

$$
\begin{align*}
\frac{d}{d t}\left[\begin{array}{c}
\hat{v}_{o} \\
\hat{i}_{L}
\end{array}\right]= & {\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{D^{\prime}}{C} \\
-\frac{D^{\prime}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
\hat{v}_{o} \\
\hat{i}_{L}
\end{array}\right]+\left[\begin{array}{cc}
0 & \frac{-\hat{d}}{C} \\
\frac{\hat{d}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
V_{o} \\
I_{L}
\end{array}\right] }  \tag{2-36}\\
& +\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{D^{\prime}}{C} \\
-\frac{D^{\prime}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
V_{o} \\
I_{L}
\end{array}\right]+\left[\begin{array}{c}
0 \\
\frac{V_{i n}}{L}
\end{array}\right]+\left[\begin{array}{cc}
0 & \frac{-\hat{d}}{C} \\
\frac{\hat{d}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
\hat{v}_{o} \\
\hat{i}_{L}
\end{array}\right] .
\end{align*}
$$

Substitute (2-34) into (2-36), $\left[\begin{array}{cc}-\frac{1}{R C} & \frac{D^{\prime}}{C} \\ -\frac{D^{\prime}}{L} & 0\end{array}\right]\left[\begin{array}{c}V_{o} \\ I_{L}\end{array}\right]+\left[\begin{array}{c}0 \\ \frac{V_{i n}}{L}\end{array}\right]$ is canceled out. Also,
considering that $\hat{d}^{\prime}, \hat{i}_{L}$ and $\hat{v}_{o}$ are small signal perturbations, their product should be very
small. Therefore, the term $\left[\begin{array}{cc}0 & \frac{-\hat{d}}{C} \\ \frac{\hat{d}}{L} & 0\end{array}\right]\left[\begin{array}{l}\hat{v}_{o} \\ \hat{i}_{L}\end{array}\right]=\left[\begin{array}{c}\frac{-\hat{d} \hat{i}_{L}}{C} \\ \frac{\hat{d} \hat{v}_{o}}{L}\end{array}\right]$ is approximately zero. Thus, (2-36)
can be rewritten as:

$$
\frac{d}{d t}\left[\begin{array}{l}
\hat{v}_{o}  \tag{2-37}\\
\hat{i}_{L}
\end{array}\right]=\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{D^{\prime}}{C} \\
-\frac{D^{\prime}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
\hat{v}_{o} \\
\hat{i}_{L}
\end{array}\right]+\left[\begin{array}{cc}
0 & \frac{-\hat{d}}{C} \\
\frac{\hat{d}}{L} & 0
\end{array}\right]\left[\begin{array}{c}
V_{o} \\
I_{L}
\end{array}\right] .
$$

Rearrange (2-37) and replace $I_{L}$ by (2-34), then (2-37) becomes:

$$
\frac{d}{d t}\left[\begin{array}{l}
\hat{v}_{o}  \tag{2-38}\\
\hat{i}_{L}
\end{array}\right]=\left[\begin{array}{cc}
-\frac{1}{R C} & \frac{D^{\prime}}{C} \\
-\frac{D^{\prime}}{L} & 0
\end{array}\right]\left[\begin{array}{l}
\hat{v}_{o} \\
\hat{i}_{L}
\end{array}\right]+\left[\begin{array}{c}
-\frac{V_{o}}{R C D^{\prime}} \\
\frac{V_{o}}{L}
\end{array}\right] \hat{d} .
$$

The control-to-output transfer function $G_{v d}(s)$ can be derived as:

$$
\begin{gather*}
G_{v d}(s)=\frac{\hat{v}_{o}(s)}{\hat{d}(s)}=\left[\begin{array}{ll}
1 & 0
\end{array}\right]\left[\begin{array}{cc}
s+\frac{1}{R C} & -\frac{D^{\prime}}{C} \\
\frac{D^{\prime}}{L} & s
\end{array}\right]^{-1}\left[\begin{array}{c}
-\frac{V_{o}}{R C D^{\prime}} \\
\frac{V_{o}}{L}
\end{array}\right] \\
G_{v d}(s)=\frac{V_{o}}{D^{\prime}} \frac{1-\frac{L}{R D^{\prime 2}} s}{1+\frac{L}{R D^{\prime 2}} s+\frac{L C}{D^{\prime 2}} s^{2}} \tag{2-39}
\end{gather*}
$$

Similarly, the control-to-inductor-current transfer function $G_{i d}(s)$ can be derived as:

$$
\begin{gather*}
G_{i d}(s)=\frac{\hat{i}_{L}(s)}{\hat{d}(s)}=\left[\begin{array}{ll}
0 & 1
\end{array}\right]\left[\begin{array}{cc}
s+\frac{1}{R C} & -\frac{D^{\prime}}{C} \\
\frac{D^{\prime}}{L} & s
\end{array}\right]^{-1}\left[\begin{array}{c}
-\frac{V_{o}}{R C D^{\prime}} \\
\frac{V_{o}}{L}
\end{array}\right] \\
G_{i d}(s)=\frac{\frac{2 V_{o}}{D^{\prime 2} R}\left(1+\frac{R C}{2} s\right)}{1+\frac{L}{D^{\prime 2} R} s+\frac{L C}{D^{\prime 2}} s^{2}} \tag{2-40}
\end{gather*}
$$

Equation (2-38) is the linearized state space representation of the open-loop boost converter, and (2-39) and (2-40) are its corresponding transfer functions. Notice that (2$33) \sim(2-40)$ are based on the assumption that variations of the inductor current $i_{L}$ are very small. This assumption is valid only when the boost converter operates at CCM. Therefore, (2-38) ~ (2-40) only represent the CCM boost converter model. For DCM, the model described here is no longer valid. Since CCM is selected in this dissertation, the DCM boost converter model is not derived here.

The CCM boost converter model is derived with another assumption that $V_{\text {in }}$ and $R$ are constant. When $V_{i n}$ or $R$ changes, the system model also changes. Therefore, the compensator designed at nominal conditions may not operate correctly when $V_{i n}$ or $R$ changes to other values. Indeed, it is commonly desired that the system can operate correctly under other possible conditions. Therefore, possible operating conditions should be determined first before designing the controller, which should have enough stability margins to compensate for the uncertainty.

Equation (2-39) shows that the boost converter has a right half-plane zero. This zero in $G_{v d}(s)$ has negligible magnitude at low frequency. However, at high frequency, it causes a phase reversal. Therefore, it is difficult to obtain a traditional single-loop controller with wide bandwidth.

## CHAPTER 3

## Microcontroller-Based Peak Current-Mode Control

In order to demonstrate the feasibility of a microcontroller-based hybrid CMC power converter, a peak current-mode controlled (PCMC) boost converter operating in the continuous conduction mode (CCM) has been designed and implemented using a PIC16C782 microcontroller. This microcontroller-based hybrid PCMC controller has been compared to a pure analog controller based on a UC3842, an analog chip manufactured by Texas Instruments, Inc.

## 3-1. Modeling Peak Current-Mode Control

When designing a PCMC power converter, an ac equivalent circuit model of the PCMC converter is needed, especially control-to-output transfer function.

A large number of continuous-time models for PCMC converters have been presented since PCMC was first proposed in 1978 [1-2]. There are two generally accepted models for PCMC converters: one was proposed by Ridley in 1991 [23-25], and another by Tan in 1994 [26-28]. Both models include a high-frequency extension so that thay are accurate up to half the switching frequency. In addition, both models can be applied to different types of power converter topologies.

The block diagram of Ridley's model is shown in Fig. 3.1. The terms in the diagram are defined as following:

- $\hat{v}_{i n}$, the perturbation of the input voltage of the power stage.


Fig. 3.1 Small-signal block diagram for PCMC power converter [23-25]

- $\hat{v}_{o}$, the perturbation of the output voltage.
- $\hat{i}_{L}$, the perturbation of the inductor current.
- $\hat{d}$, the perturbation of the duty cycle that controls the switch in the power stage.
- $G_{v d}(s)$, the control-to-output transfer function of the power converter, which can be expressed as

$$
\begin{equation*}
G_{v d}(s)=\frac{\hat{v}_{o}}{\hat{d}} \tag{3-1}
\end{equation*}
$$

- $G_{i d}(s)$, inductor current transfer function of the power converter, which can be expressed as:

$$
\begin{equation*}
G_{i d}(s)=\frac{\hat{i}_{L}}{\hat{d}} \tag{3-2}
\end{equation*}
$$

- $H_{e}(s)$ is the sampling gain, which is used to model the sampling action in the current loop.
- $R_{i}$, the effective linear gain (volts/amp) from the sensed current to the comparator input.
- $F_{m}$, the modulator gain which is the ac gain from the error current signal to the duty cycle.
- $\quad K_{f}$ and $K_{r}$ are the feedforward and feedback gains.

The following terms are used in the model:

- $S_{e}$, the slope of the external compensation ramp (volts/sec) at the comparator input.
- $S_{n}$, the slope of the sensed current ramp (volts/sec) at the comparator input.
- $T_{s}$, the switching period.

The sampling gain $H_{e}(s)$ and modulator gain $F_{m}$ can be computed by:

$$
\begin{gather*}
H_{e}(s) \cong 1+\frac{s}{\omega_{n} Q_{z}}+\frac{s^{2}}{\omega_{n}^{2}}  \tag{3-3}\\
\omega_{n}=\frac{\pi}{T_{s}}  \tag{3-4}\\
Q_{z}=-\frac{2}{\pi}  \tag{3-5}\\
F_{m}=\frac{1}{\left(S_{e}+S_{n}\right) T_{s}} \tag{3-6}
\end{gather*}
$$

$F_{m}$ is usually a constant and can only be affected by the external ramp signal, $S_{e}$.

Feedforward and feedback gain terms $K_{f}$ and $K_{r}$ are different for different types of converters. Table 3.1 lists $K_{f}$ and $K_{r}$ for three basic types of converters.

Table 3.1 $K_{f}$ and $K_{r}$ for different converter topologies in Ridley's model [24-25]

|  | Buck | Boost | Buck-Boost |
| :---: | :---: | :---: | :---: |
| $K_{f}$ | $-\frac{D R_{i} T_{s}}{L}\left(1-\frac{D}{2}\right)$ | $-\frac{R_{i} T_{s}}{2 L}$ | $-\frac{D R_{i} T_{s}}{L}\left(1-\frac{D}{2}\right)$ |
| $K_{r}$ | $-\frac{R_{i} T_{s}}{2 L}$ | $\frac{D^{\prime 2} R_{i} T_{s}}{2 L}$ | $\frac{D^{\prime 2} R_{i} T_{s}}{2 L}$ |

Tan's model [26-28] uses different notation, which is equivalent to Ridley's model by the following conversions:

$$
\begin{equation*}
\hat{i}_{c}=\hat{v}_{c} / R_{i}, M_{1}=S_{n} / R_{i}, M_{2}=S_{f} / R_{i}, \text { and } M_{e}=S_{e} / R_{i} \tag{3-7}
\end{equation*}
$$

The system block of Tan's model is similar to Ridley's model, but the contents inside the block are different. In Tan's model,

$$
\begin{equation*}
K_{f}=\alpha k, K_{r}=\beta k \tag{3-8}
\end{equation*}
$$

where $\alpha=1,0,1$, and $\beta=0,1,1$, respectively for the buck, boost, and buck-boost converter, and:

$$
\begin{equation*}
k=\frac{D D^{\prime}}{2 L} \tag{3-9}
\end{equation*}
$$

Tan's unified modulator gain can be expressed as:

$$
\begin{equation*}
F_{m}=\frac{1}{\left(S_{e}+S_{n}-\frac{V_{o f f} R_{i}}{2 L}\right) T_{s}} \tag{3-10}
\end{equation*}
$$

where $V_{\text {off }}$ is the dc voltage applied between the active and passive terminals of the switch element. Indeed, $V_{\text {off }}$ appears across either switch (main switch or diode) when it is off. This equation suggests that the only difference between Tan's and Ridley's modulator
gain equations is the term $-\frac{V_{o f f} R_{i}}{2 L}$. If there is no slope compensation ramp $\left(S_{e}\right)$, the term $-\frac{V_{o f f} R_{i}}{2 L}$ allows Tan's modulator gain $F_{m}$ to go infinity when $S_{n}=\frac{V_{o f f} R_{i}}{2 L}$, then changes sign as the duty cycle goes above $50 \%$. This is sure to cause instability, which intuitively agrees with the subharmonic oscillation at $50 \%$ duty cycle and above without slope compensation.

Tan's model does not include the sampling gain $H_{e}(s)$, i.e., $H_{e}(s)=1$. Instead, Tan's model includes the sampling effect by adding an extra pole, $\omega_{p}$, to the modulator gain, $F_{m}$. Therefore, modified $F_{m}$ can be expressed as:

$$
\begin{gather*}
F_{m}=\frac{1}{\left(S_{e}+S_{n}-\frac{V_{o f f} R_{i}}{2 L}\right) T_{s}\left(1+\frac{s}{\omega_{p}}\right)}  \tag{3-11}\\
\omega_{p}=\frac{\omega_{n}}{Q}=\frac{\omega_{n}}{\pi\left(m_{c} D^{\prime}-0.5\right)}  \tag{3-12}\\
m_{c}=1+\frac{M_{e}}{M_{1}}=1+\frac{S_{e}}{S_{n}} \tag{3-13}
\end{gather*}
$$

Many later papers extend these two models or derive new models [29-35] such that a more accurate model can be achieved. However, these two models are accurate enough for design purpose in most cases. Considering the tradeoff between the accuracy and model complexity, Ridley's model often has been chosen for design.

## 3-2. System Design

## 3-2-1. System overview

The system block diagram for the microcontroller-based PCMC boost converter controlled by a PIC16C782 is shown in Fig. 3.2. The peak switch current is sensed by a low-value resistor. A ramp signal, generated from the PSMC module, is added to the sensed current signal for slope compensation. By using a comparator, the current loop monitors and maintains the peak switch current (compensated by the ramp signal) equal to a reference current, which is calculated by a digital proportional-integral (PI) controller in the voltage loop. The reference current is converted into an analog signal and is compared to the feedback current signal at the on-chip comparator. A pulse is generated when they are equal. This pulse is sent to the PSMC module to generate a PWM signal that controls the switch.


Fig. 3.2 Block diagram of a PCMC boost converter controlled by a PIC16C782 microcontroller

Fig. 3.2 reflects the hybrid control method in the design. By using the on-board comparator and PSMC module, the analog current loop and digital voltage loop are integrated onto a single microcontroller.

For the laboratory prototype, the nominal input and output voltages of the boost converter are 12 V and 28 V , respectively, and the nominal load is $50 \Omega(0.56 \mathrm{~A})$. The switching frequency is 156.25 kHz , and the system operates in CCM.

## 3-2-2. Current-loop design

When designing the control system, the current loop should be designed first. Since there is no compensator in the current loop of a PCMC converter system, current loop design is relatively simple. Two issues are involved in designing the current-loop: the method and gain of the current sensing and the slope of the ramp signal for slope compensation.

The inductor current can be sensed directly using a low-value resistor or a transformer. A sense resistor is a simple and inexpensive approach. In order to ensure that the value of the sensed signal is in a usable range and the sensed signal is within the normal operational range of the comparator circuit, the sense resistor should provide sufficient gain, which may result in significant power loss, especially at high current situations. Sometimes, it may be necessary toutilize an amplifier as a low-pass filter to amplify the current signal while filtering out high frequency switching noise.

A transformer can be used to sense the current. Typically, this transformer has a 1-turn primary and a $n$-turn secondary winding. A transformer can reduce power loss in the circuit and provide excellent isolation between the power stage and the control circuit. The main disadvantage of the transformer approach is the higher cost and increased
design complexity.
In this implementation, the switch current, whose peak value is the same as the inductor current, is sensed by a low-value resistor. Since the sensed current signal can be very noisy, a simple RC low-pass filter is added to filter out noise.

The external ramp signal for slope compensation is generated by the PSMC module and an RC network. Slope compensation design will be discussed in detail later in Section 3-2-5, which depicts the design considerations regarding the PSMC module.

When the current loop is closed, the control-to-output transfer function, $G_{v c}(s)$, is useful in designing the voltage loop. Using Ridley's model, $G_{v c}(s)$ can be derived from Fig. 3.1 as:

$$
\begin{equation*}
G_{v c}(s)=\frac{\hat{v}_{o}}{\hat{v}_{c}}=\frac{F_{m} G_{v d}(s)}{1+F_{m} R_{i} H_{e}(s) G_{i d}(s)-F_{m} K_{r} G_{v d}(s)}, \tag{3-14}
\end{equation*}
$$

where $K_{r}=\frac{D^{\prime 2} T_{s} R_{i}}{2 L}, S_{n}=\frac{V_{i}}{L}, D^{\prime}=1-D . G_{v d}(s)$ and $G_{i d}(s)$ for a boost converter have been derived in Chapter 2, referring to (2-39) and (2-40). The actual transfer function $G_{v c}(s)$ has an infinite number of poles. In a practical design, since high frequency zeros or poles can be neglected, $G_{v c}(s)$ can be simplified to a second order system or generated from experimental measurements after the slope the ramp signal $S_{e}$ is selected. Since $G_{v c}(s)$ is an approximation of actual transfer function, error always exists. A more accurate and simple method is to measure the transfer function directly. In this implementation, a network analyzer (Model 102B form AP Instrument Inc.) is used to measure the frequency response of the PCMC system with the current loop closed. The transfer function can be obtained by using MATLAB to fit it to the measured frequency
response data. Fig. 3.3 shows the measured open-loop control-to-output frequency response of a PCMC boost converter and its theoretical frequency response using Ridley's model. It can be seen from Fig. 3.3 that the theoretical calculation is close to the experimental measurement up to half of the switching frequency. Obviously, it is more desirable to use measured model for design purpose when it is available.

## 3-2-3. Analog to digital conversion (ADC) and time delay

In the proposed hybrid control scheme, the voltage loop is implemented digitally. Therefore, the output voltage $v_{o}$ of the power stage must be sampled as the feedback to the voltage loop compensator. The ADC module inside the PIC16C782 captures a snapshot of the sampled signal and holds it for an $A / D$ conversion. It is required that the $\mathrm{A} / \mathrm{D}$ conversion should have adequate resolution to ensure proper measurement of


Fig. 3.3 Comparison of experimental and theoretical (Ridley's model) open-loop control-to-output frequency responses of a PCMC boost converter
the output voltage. This resolution is determined by the range of measurement and the word length of the digital value. In this implementation, the nominal output voltage of the boost converter is 28 V , so the output voltage can easily be higher than 30 V . Since the ADC module has an 8 -bit resolution, the $\mathrm{A} / \mathrm{D}$ conversion error can be easily more than 0.12 V when the possible full range of output voltage $(0-30 \mathrm{~V}$ or more) is measured.

In order to get higher $\mathrm{A} / \mathrm{D}$ resolution, a level-shift circuit has been designed such that the $\mathrm{A} / \mathrm{D}$ result represents a "windowed" range of the output voltage around the nominal value. The level shifter is built from an external operational amplifier with several resistors. An external voltage buffer (voltage follower) is needed to ensure accurate measurement of the output voltage. In this implementation, shown in Fig. 3.4, the dc bias voltage is set to 2.5 V , and the gain of the opamp is set to 12 . This design can measure the "windowed" range of 25.67 V and 30.33 V for a 28 V nominal output voltage. The level shifter can be built from the internal OPA module with several external resistors. An external voltage buffer (voltage follower) is needed to ensure accurate measurement of the output voltage. Another channel is used to measure the fullrange output voltage with lower resolution. This channel is not used during normal


Fig. 3.4 Level-shift circuit
operation in this implementation, because the variation in the output voltage resulting from a possible disturbance is within this window range. However, this channel can be used to implement a soft-start when the startup ramp of the output voltage needs to be precisely controlled. When the ADC resolution is satisfactory for an application, the level-shift circuit can be eliminated, and hence the external voltage buffer can be eliminated also.

Since the current-loop is constructed using analog components, the signal in the current loop instantaneously varies with the inductor current without time delay. Therefore, it is desirable to update the current reference, which is the output of the voltage loop, at the beginning of each switching cycle.

However, this ideal situation is difficult to achieve when using a PIC16C782 to control a power converter. Because of the limited computation power of PIC16C782 and the fast dynamics of the power stage, the delays due to $A / D$ conversion and control computation cannot be neglected. For example, in this implementation, the switching frequency is 156.25 kHz for a switching period of $6.4 \mu \mathrm{~s}$. When the oscillator frequency is 20 MHz , an $\mathrm{A} / \mathrm{D}$ conversion cycle requires $15.2 \mu \mathrm{~s}$, which equals 2.375 switching cycles. For a 20 MHz oscillator frequency, the instruction cycle (the time to execute an instruction) is $0.2 \mu \mathrm{~s}$, so only 32 instructions can be executed in each switching cycle. This implies that even a very simple control law is difficult to be completed in a single switching cycle. In this implementation, nearly 4 switching cycles (or nearly $25.6 \mu \mathrm{~s}$ ) are needed to finish the calculation of the control law. A/D conversion and calculations can be performed simultaneously, but the $A / D$ conversion time is much faster than the calculation time (controller time delay), so the calculation time directly determines the
sampling period. In order to achieve constant sampling frequency, there is a short waiting period (less than a switching cycle, or $6.4 \mu \mathrm{~s}$, in this implementation) before starting the next sampling period. When this waiting period is neglected, the controller sampling period approximately equals the controller time delay, or $25.6 \mu \mathrm{~s}$. In order to update the current reference as soon as possible, the controller time delay should be as short as possible. Therefore, compact software design is critical in this implementation.

Switching noise in the output voltage is inevitable. In order to achieve concise software, switching noise in the output voltage should be avoided or filtered out in "hardware" instead of by a digital filter. Digital filter is indeed not practical in this implementation, because the switching noise contains harmonics with frequency much higher than possible sampling frequency. Therefore, the output voltage should be sampled during the period that has minimum switching noise. In this implementation, the PWM signal is sent back to another I/O pin to trigger an interrupt that starts an A/D conversion, so the sampling moment can be controlled accurately, and the output voltage can always be captured after the switching noise has subsided. Since the PIC16C782 does not have priority levels for interrupts, an interrupt from any other source should not be allowed to ensure constant sampling rate and the proper sampling moment. The starting point of each $\mathrm{A} / \mathrm{D}$ conversion cycle can be controlled precisely at a $0.2 \mu \mathrm{~s}$ (one instruction cycle) precision.

## 3-2-4. Voltage-loop controller design

Once the current loop is designed, the converter with the closed current loop can be treated as a "new" open-loop plant, and the voltage loop compensator $G_{c}(s)$ is designed to control the "new" plant $G_{v c}(s)$. The "new" system, shown in Fig. 3.5, is


Fig. 3.5 System block diagram of a PCMC power converter
essentially a typical digital control system, and the voltage loop compensator is a standard digital controller. Usually, the digital controller can be designed using either the emulation method or the direct digital design method described in Chapter 2. In this implementation, a new method combining the emulation method and the direct digital design method is proposed.

As stated before, $G_{v c}(s)$ can be computed using (3-14) or measured experimentally. It can be seen from (3-14) that $G_{v c}(s)$ is a function of $G_{v d}(s)$ and $G_{i d}(s)$. Referring to (2$39)$ and (2-20), both $G_{v d}(s)$ and $G_{i d}(s)$ are a function of the load. Therefore, $G_{v c}(s)$ is a function of load. Thus, the frequency response of the system varies with the load. In this implementation, $G_{v c}(s)$ is measured at different loads, as shown in Fig. 3.6, by a Analog Network Analyzer (Model 102B from AP Instrument Inc.). In order to ensure the stability of the system for different loads, the load used to design the controller should be selected carefully. In this implementation, the system with the lightest load (which is 0.187 A ) was chosen to design the voltage loop compensator; the reason for this section will be explained shortly. Using MATLAB to fit the measured frequency response data, a mathematical model for $G_{v c}(s)$ can be obtained. The order of $G_{v c}(s)$ can be high enough to fit the experimental data accurately.


Fig. 3.6 Bode plots of $G_{v c}(s)$ for different loads

Once $G_{v c}(s)$ is obtained, it can be converted to a discrete-time model $G_{v c}(z)$ using the zero-order hold $(\mathrm{ZOH})$ method. The ZOH , as expressed in (2-12), introduces a phase lag and magnitude reduction to the system. This can be seen clearly in its Bode plot shown in Fig. 3.7. In this implementation, the total time delay is approximately four times the switching period ( $6.4 \mu \mathrm{~s}$ ), so $25.6 \mu \mathrm{~s}$ is used as the controller sampling period. According to (2-13), $G_{v c}(z)$ can written as:

$$
\begin{equation*}
\left.G_{v c}(z)=\frac{z-1}{z}\right\}\left[\frac{G_{v c}(s)}{s}\right] . \tag{3-15}
\end{equation*}
$$

As stated previously, the calculation time is approximately equal to the sampling period. Considering the time delay, the mapping of $G_{v c}(s)$, referring to (2-18), can be


Fig. 3.7 Bode plot of zero-order-hold when sampling frequency is $25.6 \mu \mathrm{~s}$
expressed as:

$$
\begin{equation*}
\left.G_{v c}^{\prime}(z)=z^{-1} G_{v c}(z)=\frac{z-1}{z^{2}}\right\}\left[\frac{G_{v c}(s)}{s}\right] . \tag{3-16}
\end{equation*}
$$

In Fig. 3.8, the Bode plots of $G_{v c}(s), G_{v c}(z)$, and $G_{v c}^{\prime}(z)$ are compared when the load is 0.187 A , where the transformation $z=e^{j \omega T}$ is used to map the unit circle to the real frequency axis. Fig. 3.8 indicates that the ZOH and controller time delay introduce considerable phase delay at high frequency when mapping the system from thee $s$-plane to the $z$-plane. Therefore, $G_{v c}^{\prime}(z)$ should be used to design the voltage loop compensator.

A PI controller is usually used as the voltage loop compensator in a PCMC power converter system. A PI controller is essentially a phase-lag compensator. It can eliminate steady-state error, since it has high gain at low frequency (a pole at zero).


Fig. 3.8 Bode plots of PCMC boost converter when load is 0.187 A

However, a PI controller cannot be designed directly in z-plane. Usually, a digital PI controller is designed using the emulation method or in the $w$-plane. However, the direct emulation method is not suitable when the ZOH and time delay need to be considered. Designing in the $w$-plane requires that the model be transformed between the $z$-plane and the $w$-plane. In this work, instead of mapping the system from the $z$-plane to the $w$-plane, the system is mapped from the $z$-plane to $s$-plane.

Using MATLAB, the Bode plot of $G_{v c}^{\prime}(z)$ can be obtained as shown in Fig. 3.8. Notice that the Bode plot of $G_{v c}^{\prime}(z)$ is indeed obtained from mapping $G_{v c}^{\prime}(z)$ to $G_{v c}^{\prime}(s)$ in the $s$-domain using $z=e^{s T}$, or:

$$
\begin{equation*}
G_{v c}^{\prime}(s)=\left.G_{v c}^{\prime}(z)\right|_{z=e^{s T}} . \tag{3-17}
\end{equation*}
$$

The Bode plot cannot be generated in the $z$-domain, so the Bode plot of $G_{v c}^{\prime}(z)$ is actually the Bode plot of $G_{v c}^{\prime}(s)$. It could be difficult to develop a mathematical equation for $G_{v c}^{\prime}(s)$, but it is very easy to obtain its Bode plot using MATLAB. The difference between $G_{v c}^{\prime}(s)$ and $G_{v c}(s)$ is that the ZOH and time delay are included in $G_{v c}^{\prime}(s)$, so $G_{v c}^{\prime}(s)$ is more accurate for design purposes. Once the Bode plot of $G_{v c}^{\prime}(s)$ is obtained, it can be used to design the controller.

In this implementation, a PI controller is designed in the $s$-domain using the Bode plot of $G_{v c}^{\prime}(s)$. The PI controller can be expressed as:

$$
\begin{equation*}
G_{c}(s)=K_{P}+\frac{K_{I}}{s}=\frac{K_{I}\left(1+s / \omega_{0}\right)}{s}, \tag{3-18}
\end{equation*}
$$

Equation (3-18) shows that the zero $\omega_{0}$ is located at $K_{I} / K_{P}$, and its high frequency gain is $K_{P}$. Therefore, a PI controller will not change the phase of the system at high frequency. Suppose the phase margin is specified to be $\varphi_{m}$ at a certain frequency, and the phase margin of $H_{v} G_{v c}^{\prime}(s)$ is $\varphi_{m}$ at $\omega_{1}$. Assume that the dc gain of $H_{v} G_{v c}^{\prime}$ is adjusted by a factor of $K_{c}$ to meet the low frequency specification, then the following equation must be satisfied when designing the controller:

$$
\begin{equation*}
K_{P} K_{c} H_{v} G_{v c}^{\prime}\left(j \omega_{1}\right)=1 \angle-\left(180^{\circ}-\varphi_{m}\right) \tag{3-19}
\end{equation*}
$$

Equation (3-19) shows that $K_{P}$ should be adjusted such that the open loop gain of the compensated system has unity gain at $\omega_{1}$. In order to ensure that the compensator introduces very little phase lag at $\omega_{1}$, the zero $\omega_{0}$ should be placed far enough from $\omega_{1}$, and one tenth of $\omega_{1}$ is a suitable value. Equation (3-19) neglects any phase lag of the
compensator. Indeed, when choosing $\omega_{0}=0.1 \omega_{1}$, the phase lag at $\omega_{1}$ is about $5^{\circ}$. Thus, following equation is used to determine $K_{P}$ :

$$
\begin{equation*}
K_{P}=\frac{1}{\left|K_{c} H_{v} G_{v c}^{\prime}\left(j \omega_{1}\right)\right|}, \tag{3-20}
\end{equation*}
$$

where $\omega_{1}$ is the frequency that the phase of $G_{v c}^{\prime}\left(j \omega_{1}\right)$ is $-\left(180^{\circ}-\varphi_{m}-5^{\circ}\right)$. When $K_{P}$ is obtained, $K_{I}$ can be computed by:

$$
\begin{equation*}
K_{I}=\omega_{0} K_{P}=0.1 \omega_{1} K_{P} \tag{3-21}
\end{equation*}
$$

Referring to (3-19), since dc gain of $H_{v} G_{v c}^{\prime}$ has been adjusted by the factor $K_{c}$, the dc gain should be adjusted back by a factor of $K_{c}$, so the complete PI controller transfer function is:

$$
\begin{equation*}
G_{c}(s)=K_{c}\left(K_{P}+\frac{K_{I}}{s}\right) \tag{3-22}
\end{equation*}
$$

As stated before, $G_{v c}(s)$ is a function of load. Therefore, it is desired that at any possible load, the following condition should be satisfied:

$$
\begin{equation*}
\left|K_{P} K_{c} H_{v} G_{v c}^{\prime}\left(j \omega_{1}\right)\right| \leq 1 \tag{3-23}
\end{equation*}
$$

Equation (3-23) implies that, in order to ensure proper phase margin, the load $R$ selected for the purposes of design should be the value at which $H_{v} G_{v c}^{\prime}(s)$ has its largest magnitude. In this implementation, assume that there is no need to adjust the dc gain of $H_{v} G_{v c}^{\prime}$ to meet the low frequency specification, that is, $K_{c}=1$. With a maximum load is 0.75 A and a minimum load of 0.187 A , the Bode plot of $H_{v} G_{v c}^{\prime}(s)$ at these two


Fig. 3.9 Bode plots of $H_{v} G^{\prime}{ }_{v c}(s)$ at different load
operating conditions is shown in Fig. 3.9. Set the phase margin $\varphi_{m}$ to $55^{\circ}$, so the phase of $G_{v c}^{\prime}\left(j \omega_{1}\right)$ is $-\left(180^{\circ}-55^{\circ}-5^{\circ}\right)=120^{\circ}$. For 0.187 A of load, $\omega_{1}$ is $1.12 \times 10^{6} \mathrm{rad} / \mathrm{s}$, corresponding to a magnitude of 2.43 dB . For 0.75 A of load, $\omega_{1}$ is $9.28 \times 10^{5} \mathrm{rad} / \mathrm{s}$, corresponding to a magnitude of 1.24 dB . Since $H_{v} G_{v c}^{\prime}\left(j \omega_{1}\right)$ has the largest magnitude at 0.187 A of load (lightest load) in this case, the system with the lightest load should be chosen for the design of the voltage loop compensator.

Substitute $\left|H_{v} G_{v c}^{\prime}\left(j \omega_{1}\right)\right|=2.43 \mathrm{~dB}$ into (3-20):

$$
\begin{equation*}
K_{P}=\frac{1}{\left|H_{v} G_{v c}^{\prime}\left(j \omega_{1}\right)\right|}=\frac{1}{10^{2.43 / 20}}=0.76 . \tag{3-24}
\end{equation*}
$$

Thus, $K_{I}$ can be computed according to (3-21),

$$
\begin{equation*}
K_{I}=0.1 \omega_{1} K_{P}=0.1 \times 1.12 \times 10^{4} \times 0.76=851.2 \tag{3-25}
\end{equation*}
$$

Hence, the zero $\omega_{0}$ of the PI controller is:

$$
\begin{equation*}
\omega_{0}=\frac{K_{I}}{K_{p}}=\frac{851.2}{0.76}=1120 \mathrm{rad} / \mathrm{s} . \tag{3-26}
\end{equation*}
$$

The voltage loop compensator can be expressed in the s-domain by:

$$
\begin{equation*}
G_{c}(s)=K_{p}+\frac{K_{I}}{s}=0.76+\frac{851.2}{s} . \tag{3-27}
\end{equation*}
$$

Recall that the sampling period is 4 times of switching period, or $25.6 \mu \mathrm{~s}$. Using the backward rule, the $s$-domain PI controller is then converted to a $z$-domain transfer function as:

$$
\begin{equation*}
G_{c}(z)=K_{p}+\frac{K_{I} T z}{z-1}=K_{p}+\frac{K_{I}^{\prime} z}{z-1}=0.76+\frac{0.021 z}{z-1} . \tag{3-28}
\end{equation*}
$$

According to $G_{c}(z)$, the current reference $v_{c}(k)$ can be computed using the following difference equation:

$$
\begin{equation*}
v_{c}(k)=K_{p} e(j)+K_{I}^{\prime} \sum_{j=0}^{k} e(j)=0.76 e(k)+0.021 \sum_{j=0}^{k} e(j), \tag{3-29}
\end{equation*}
$$

where $e(k)$ is the error signal, and is computed digitally by:

$$
\begin{equation*}
e(k)=V_{r e f}(k)-V_{o}(k), \tag{3-30}
\end{equation*}
$$

where $V_{o}(k)$ is the ADC result of the output voltage, and $V_{r e f}(k)$ is the voltage reference. $V_{r e f}(k)$ is fixed at 7 Fh , which represents the fixed nominal output voltage.

The PIC16C782 does not have multiplication/division instructions, so power-oftwo arithmetic is employed. Multiplication/division can be done by simply shifting register bits left/right. However, this arithmetic limits the available gains, and hence may degrade the performance. For example, in this implementation, both of $K_{P}$ and $K_{I}{ }^{\prime}$ must be a power-of-two, which are different from desired values ( 0.76 and 0.021 ). In order to ensure proper phase margin, $K_{P}$ should not be larger than the desired value. Therefore, $K_{P}=0.5$ should be selected in this implementation.

The PIC16C782 microcontroller does have a sign bit, so the software must keep track of the sign. In this implementation, the sign of $e(k)$ is stored in the flag bit, so the proportional term and the integral term are computed without considering their signs, and every possible sign combination has a separate code path to compute the control effort. Though this method increases the size and structure complexity of the code considerably, the calculation time is reduced and calculations in each code path are simplified.

The DAC module inside the PIC16C782 is used to convert the output of the digital PI controller into an analog signal $v_{c}$, which is sent to the comparator $\mathrm{C}_{1}$. The effective linear gain $R_{i}$, which is the gain of the sensed current to the comparator input, must be chosen carefully such that $v_{c}$ is within the normal operational range of $\mathrm{C}_{1}$ and is compatible with the sensed current signal. The signal $v_{c}$ is also a function of the reference voltage of the DAC module, which can be provided by the on-board voltage reference module $\left(\mathrm{V}_{\mathrm{R}}\right)$.

## 3-2-5. Programmable Switch Mode Controller (PSMC) module

The PSMC module can be configured for the Pulse Width Modulation (PWM)
mode. The frequency of the PWM signal, which equals the switching frequency, is
programmed by two bits of a control register. Therefore, once the oscillation frequency is selected, only four switching frequencies $(1 / 128,1 / 64,1 / 32$ and $1 / 16$ of the oscillator frequency) are available. A switching frequency of 156.25 kHz , which is $1 / 128$ of 20 MHz , was selected in this implementation.

Another four bits in the control register are used to determine the maximum and minimum duty cycles. In a boost converter, it is required to limit the maximum duty as discussed previously. Since only two bits are used to define the maximum duty cycle, only four possible maximum duty cycles $(1 / 2,5 / 8,3 / 4$ and $15 / 16)$ are available. In this implementation, $D_{M A X}=0.75$ was selected.

As stated previously, PCMC converters suffer subharmonic oscillation problems, and slope compensation is required to ensure stability when the duty cycle of a CCM converter is above $50 \%$. The PSMC module can provide a PWM signal, and it can also be used to implement slope compensation [36]. At this time, the pin PSMC1A is configured as PWM output, and another output pin of the PSMC module (PSMC1B) is configured as a slope compensation ramp generator. Fig. 3.10 shows the slope compensation circuit. The complete current loop is also included, and the waveforms at critical points are illustrated in Fig. 3.10. The pin PSMC1B is grounded internally through a gate. It appears as a high resistance when the gate is turned off during the first $15 / 16$ of each switching cycle. The gate is turned on during the last $1 / 16$ of each switching cycle and the external capacitor is discharged thoroughly in a very short time. Connecting this pin to an RC network generates a positive going ramp $v_{m}$. The ramp signal $v_{m}$ at the pin PSMC1B can be expressed as:


Fig. 3.10 Current loop and slope compensation circuit

$$
\begin{equation*}
v_{m}(t)=5-5 e^{-\frac{t}{R_{T} C_{T}}} . \tag{3-31}
\end{equation*}
$$

According to (3-31), by choosing the resistor $R_{T}$ and the capacitor $C_{T}$ of the RC network, $v_{m}(t)$ is approximately a linear (constant slope) ramp signal in the range of interest. The ramp signal $v_{m}$ is added to the sensed inductor current through a resistor $R_{\text {slope }}$, while the inductor current value is sensed by sense resistor $R_{i}$ and passes through another resistor $R_{f}$. Once $R_{T}$ and $C_{T}$ are selected, the actual slope $m_{c}$ of the added ramp signal is determined by $R_{f}$ and $R_{\text {slope }}$. Neglecting the sense resistor $R_{i}$ (very small value compared with $R_{f}$ and $R_{\text {slope }}$ ), $m_{c}$ can be expressed as:

$$
\begin{equation*}
m_{c}=\frac{\Delta V_{m}}{\Delta t} \frac{R_{f}}{R_{\text {slope }}+R_{f}} \tag{3-32}
\end{equation*}
$$

where $\Delta V_{\mathrm{m}}$ is the voltage of the ramp signal at maximum duty cycle $(75 \%$ in this implementation), and $\Delta t$ is time period of the maximum duty cycle $(4.8 \mu \mathrm{~s}$ in this implementation). Equation (3-32) shows that the slope of the ramp at the current input


Fig. 3.10 Slope compensation waveforms
pin of the microcontroller can be any desired value by adjusting $R_{\text {slope }}$ and $R_{f}$. According to (3-32), $R_{\text {slope }}$ can be computed by:

$$
\begin{equation*}
R_{\text {slope }}=\frac{\Delta V_{m}}{\Delta t} \frac{R_{f}}{m_{c}}-R_{f} . \tag{3-33}
\end{equation*}
$$

Equation (3-33) provides the method to compute $R_{\text {slope }}$. As described previously, $m_{c}$ should be in the range of $m_{2}$ and half of $m_{2}$, where $m_{2}$ is the down slope of the inductor current. For example, in a boost converter case, $m_{2}$, scaled by the linear gain of the sense resistor $R_{i}$, can be computed by:

$$
\begin{equation*}
m_{2}=\frac{V_{i n}-V_{o}}{L} R_{i} . \tag{3-34}
\end{equation*}
$$

When choosing $\left|m_{c}\right|=\left|m_{2}\right|, R_{\text {slope }}$ can be computed by substituting (3-34) into (333):

$$
\begin{equation*}
R_{\text {slope }}=\frac{\Delta V_{m}}{\left|V_{i n}-V_{o}\right|} \frac{R_{f}}{R_{i}} \frac{L}{\Delta t}-R_{f} \tag{3-35}
\end{equation*}
$$

The selection of the $R_{f}$ can be in a wide range, as long as the combination of $R_{f}$ and $R_{\text {slope }}$ is significantly larger than $R_{T}$ such that the insertion of the slope compensation has negligible effect on $v_{m}(t)$. There is another reason that $R_{f}$ and $R_{\text {slope }}$ should be large enough. Notice that $R_{i}$ is neglected in the calculation, so the current provided by the slope compensation circuit generates a voltage error when passing through $R_{i}$. Fortunately, this error can be neglected since $R_{f}$ and $R_{\text {slope }}$ can easily be selected significantly larger than $R_{i}$.

## 3-2-6. Algorithm structure

The software can be roughly classified into a main routine and interrupt service routine. After the microcontroller is initialized, it enters the main routine. The tasks of the main routine include reading the sampled the output voltage and calculating and updating the control effort. In order to conveniently change the proportional and integral gains for different applications, each possible gain has a separate code path to compute the proportional and integral terms, at the expense of considerably increasing the length of the code. Fig. 3.11 is the flowchart of the main routine.

The interrupt service routine, as shown in Fig. 3.12, is independent from the main routine, and its only task is to start the $A / D$ conversion at the desired moment to avoid


Fig. 3.11 Flowchart of the main routine


Fig. 3.12 Flowchart of the interrupt service routine (ISR)
switching noise and maintain a fixed sampling frequency.

## 3-3. Analog PCMC Power Converter

In order to evaluate the performance of the hybrid PCMC power converter, a pure analog PCMC controller is designed to control the same boost converter for comparison. An IC chip, UC3842 from Texas Instruments, was used in this design [37~40].

The UC3842 provides the necessary features to implement off-line or dc to dc fixed frequency PCMC schemes with several external parts. Important internal circuits, shown in Fig. 3.14, include an error amplifier (used as the voltage loop compensator), precision reference (used as the 2.5 V voltage reference for the error amplifier and to provide 5 V voltage reference at an output pin), current sense comparator (used as the comparator in the current loop to sense the current peak), RS latch (to ensure latched operation), a totem pole output stage (to source or sink a maximum 200 mA current to


Fig. 3.14 Internal block diagram of the UC3842 [39]
drive the switch), and an oscillator (to provide fix frequency timing for the RS latch and slope compensation).

The block diagram of the boost converter controller by a UC3842 is shown in Fig. 3.15. When designing a UC3842-based PCMC controller, an external resistor $R_{T}$ and capacitor $C_{T}$ should be selected first to determine the switching frequency $f_{s}$ of the power converter and the maximum duty cycle $D_{\max } . \quad R_{T}$ is connected to $\operatorname{Pin} 8\left(\mathrm{~V}_{\text {REF }}\right)$ of the UC3842, which provides 5 V reference voltage. $C_{T}$ is discharged by the internal oscillator at the end of each cycle, and a ramp signal is produced on Pin 4. When $R_{T}>$ $5 \mathrm{k} \Omega$, the oscillator frequency $f_{\text {osc }}$, which is also the switching frequency $f_{s}$, can be expressed as [38]:

$$
\begin{equation*}
f_{s}=f_{\text {osc }}=\frac{1.72}{R_{T} C_{T}} . \tag{3-36}
\end{equation*}
$$



Fig. 3.15 Block diagram of a boost converter controller by a UC3842

Equation (3-36) shows that a fixed witching frequency $f_{s}$ can be defined (156.25 kHz in this implementation) by selecting $R_{T} C_{T} . R_{T}$ and $C_{T}$ also determine the maximum duty cycle $D_{\max }$. $D_{\max }$ can be expressed by following equation [37]:

$$
\begin{equation*}
D_{\max }=1-t_{d} f_{s} . \tag{3-37}
\end{equation*}
$$

where $t_{d}$ is the dead time, or discharge time of the capacitor. $t_{d}$ is a function of $R_{T}$ and $C_{T}$. When $R_{T}$ is large enough $\left(R_{T}>5 \mathrm{k} \Omega\right)$, $t_{d}$ is approximately directly determined by $C_{T}$. The relationship between $t_{d}$ and $C_{T}$ is illustrated in Fig. 3.16 [37]. Thus, as long as $f_{s}$ and $D_{\max }$ are specified, $C_{T}$ can be obtained from Fig. 3.16 directly. For example, $D_{\max }$ is set to $75 \%$,


Fig. 3.16 Dead time $t_{d}$ vs. $C_{T}$ when $R_{T}>5 \mathrm{k} \Omega$ [37]
the same as the hybrid controller. According to (3-37), $t_{d}$ should be $1.6 \mu \mathrm{~s}$ when $f_{s}$ is 156.25 kHz . By checking Fig. 3.16, $C_{T}$ is approximately 4.7 nF . According to (3-44), $R_{T}$ can be computed by:

$$
\begin{equation*}
R_{T}=\frac{1.72}{f_{S} C_{T}}=\cdot \frac{1.72}{156.25 \times 10^{3} \times 4.7 \times 10^{-9}}=2.34 \mathrm{k} \Omega \tag{3-38}
\end{equation*}
$$

Note that $C_{T}$ obtained from Fig. 3.16 is an approximation. In addition, the actual available values of $R_{T}$ and $C_{T}$ may be slightly different from calculated values. In many cases, $R_{\text {slope }}$ and $R_{f}$ are determined empirically and experimentally. For example, in this implementation, $D_{\max }$ is less than 0.75 when $C_{T}=4.7 \mathrm{nF}$. Instead, $D_{\max }$ is 0.75 when $C_{T}=$ 4.8 nF , according to experimental measurements.

Note that the signal on Pin 4 is a ramp signal. Its frequency is identical to the switching frequency. Therefore, this signal can also be used to implement slope
compensation. Referring to Fig. 3.15, the ramp signal is added to the sensed inductor current through a resistor $R_{\text {slope }}$, while the sensed current passes through another resistor $R_{f}$. The values of $R_{f}$ and $R_{\text {slope }}$ determines the slope of the ramp signal. The calculation method is similar to the hybrid controller, which is represented by (3-32) - (3-35). However, since the ramp signal is also used to generate the switching frequency and to set the maximum duty cycle, the current for slope compensation introduces an error into the switching frequency and the maximum duty cycle. Therefore, it is required that $R_{\text {slope }}$ and $R_{f}$ should be significantly larger than $R_{T}$. Also, since the current sensing comparator consumes up to $10 \mu \mathrm{~A}$ of bias current, large $R_{f}$ may result in considerable error in the measured the inductor current. Therefore, $R_{\text {slope }}$ and $R_{f}$ should be well below $100 \mathrm{k} \Omega$.

In order to minimize the impact of the slope compensation circuit, the ramp signal can amplified first by a transistor before it is added to the sensed current signal, as shown in Fig. 3.17. By using an extra transistor amplifier, the slope compensation circuit has very little effect on the switching frequency and maximum duty cycle. Also, smaller values of $R_{\text {slope }}$ and $R_{f}$ can be used in the circuit.


Fig. 3.17 A transistor is added in slope compensation circuit

Just as in the hybrid PCMC system, the voltage loop is also a PI controller, and the equivalent gains are designed as close as possible to the digital counterpart. The PI controller is constructed using the on-board error amplifier and three external components (one capacitor $C_{2}$ and two resistors $R_{3}$ and $R_{4}$ ). Referring to Fig. 3.15, the transfer function of the PI controller can be expressed as:

$$
\begin{equation*}
G_{P I}(s)=-\left(\frac{R_{4}}{R_{3}}+\frac{1}{R_{3} C_{2}} \frac{1}{s}\right) .=-\left(K_{P}+\frac{K_{I}}{s}\right) \tag{3-39}
\end{equation*}
$$

## 3-4. Experimental Results

The specification of the boost converter used in experimental test is listed below:

- Nominal input voltage: 12 V
- Nominal output voltage: 28 V
- Switching frequency: 156.25 kHz :
- Nominal load: $50 \Omega(0.56 \mathrm{~A}, 15.68 \mathrm{~W})$
- Operating condition: CCM
- Inductor: $257 \mu \mathrm{H}$
- Output capacitor: $35.42 \mu \mathrm{C}$

All the experimental waveforms in this chapter were recorded using a Tektronix TDS 744A oscilloscope. AC coupling is utilized on the oscilloscope to remove the dc level from all signals displayed on the oscilloscope. The block diagram of the boost converter and its control system is shown in Fig. 3.18. The key component of the control system is the PIC16C782 microcontroller. The voltage follower, which is constructed using an external operational amplifier, is used to condition the voltage feedback. Since the PWM output of the PIC16C782 is a 5 V level and cannot provide enough current to


Fig. 3.18 The PIC16C782 microcontroller controlling a PCMC boost converter
drive the MOSFET switch, an external gate drive is required. In this implementation, the UC3705N is selected as the gate drive chip, which is an 8-pin high speed power driver IC from Texas Instruments [41-43]. The gate drive circuit is shown in Fig. 3.19.

At nominal conditions, the duty cycle $D$ for this boost converter is:

$$
\begin{equation*}
D=\frac{V_{o}-V_{i n}}{V_{o}}=\frac{28-12}{28}=0.57 . \tag{3-40}
\end{equation*}
$$

Since the duty cycle $D$ is larger than 0.5 at nominal conditions, slope compensation must be added to eliminate subharmonic oscillation. In this implementation, the slope of the ramp signal is set to the down slope of the inductor current.


Fig. 3.19 Gate drive circuit

The primary issue in designing a power converter system is its ability to respond to load or voltage changes and to adjust the output voltage to the nominal value. According to the experimental results, the system can maintain an output voltage of 28 V for a wide range of input voltages from 9.5 V to 25.5 V .

Ideally, the values of $K_{P}$ and $K_{I}$ ' are 0.7 and 0.0225 , respectively. However, since power-of-two arithmetic is employed, the values of $K_{P}$ and $K_{I}{ }^{\prime}$ are $1 / 2$ and $1 / 32=$ 0.03125 , respectively are selected; the system is a little bit under damped. For a load change from 0.75 A to 0.187 A (Fig. 3.20), the system's response time is roughly 2 ms to reach steady state with small overshoot. The maximum transient error is about 1.2 V , which is less than $5 \%$ of 28 V . In about 1 ms , the error reduces to around 0.1 V , which is about $0.35 \%$ of 28 V . The steady state error of the system is approximately zero.

When the load changes from 0.187 A to 0.75 A (Fig. 3.21), the response is similar. The system spends roughly 2.5 ms to reach steady state with small overshoot. The maximum transient error is 1.2 V . Within 1.2 ms , the error reduces to 0.1 V . The steady


Fig. 3.20 Transient response using the PIC16C782 when the load change is from 0.75 A to 0.187 A , and $K_{P}=1 / 2$ and $K_{I}^{\prime}=1 / 32$. Output voltage: $500 \mathrm{mV} /$ DIV; Time: $500 \mu \mathrm{~s} /$ DIV


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Fig. 3.21 Transient response using the PIC16C782 when the load change is from 0.187 A to 0.75 A , and $K_{P}=1 / 2$ and $K_{I}{ }^{\prime}=1 / 32$. Output voltage: $500 \mathrm{mV} / \mathrm{DIV}$; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$
state error of the system is approximately zero.
The step response for the voltage reference $V_{\text {ref }}$ (changing from 00 h to 7 Fh ) is shown in Fig. 3.22. The system can reach steady state in less than 2 ms with a small overshoot of about 1.5 V , which is about $5 \%$ of 28 V .

The simulated results of the compensated system when $K_{P}=1 / 2$ and $K_{I}{ }^{\prime}=1 / 32$ are depicted in Fig. 3.23. Compared to the uncompensated system, the gain at low frequency and the gain margin are increased, but the phase margin is deceased to about $30^{\circ}$ when the load is 0.187 A . By using the analog network analyzer, the frequency response of the compensated system are recorded experimentally and then plotted in MATLAB, as shown in Fig. 3.24. The experimental responses in Fig. 3.24 match the simulated responses in Fig. 3.23 well with small errors.


Fig. 3.22 Step response using the PIC16C782 when the load is 0.56 A . Output voltage: $5 \mathrm{~V} / \mathrm{DIV}$; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$


Fig. 3.23 Simulation of compensated PCMC boost converter using PI controller for different load


Fig. 3.24 Experimental responses of compensated PCMC boost converter using digital PI controller for different load

If $K_{P}=1 / 2$ and $K_{I}{ }^{\prime}=1 / 64=0.015625$ are selected, the system is a little bit over damped, so the speed of response is a little slower than when $K_{I}{ }^{\prime}=1 / 32=0.03125$. For a load change from 0.75 A to 0.187 A (Fig. 3.25), the system's response time is roughly 2.8 ms to reach steady state without any overshoot. When the load changes from 0.187 A to 0.75 A (Fig. 3.26), the response is roughly 3 ms without any overshoot. In both cases, the maximum transient error is about 1.3 V , which is less than $5 \%$ of 28 V , and the steady state error of the system is approximately zero.

Fig. 3.20 - Fig. 3.26 indicate that the power-of-two algorithm can achieve satisfactory results. When higher resolution for the gains is required, two or more power-of-two numbers can be added together. For example, by adding $1 / 2$ and $1 / 4$ of the original number together, a gain of $3 / 4$ can be obtained.


Fig. 3.25 Transient response using the PIC16C782 when the load change is from 0.75 A to 0.187 A , and $K_{P}=1 / 2$ and $K_{I}^{\prime}=1 / 64$. Output voltage: $500 \mathrm{mV} /$ DIV; Time: $500 \mu \mathrm{~s} /$ DIV


Fig. 3.26 Transient response using the PIC16C782 when the load change is from 0.187 A to 0.75 A , and $K_{P}=1 / 2$ and $K_{I}{ }^{\prime}=1 / 64$. Output voltage: $500 \mathrm{mV} / \mathrm{DIV}$; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$

The analog controller using the UC3842 from Texas Instruments is tested on the same boost converter for comparison. This analog controller also contains a PI controller in its voltage loop with the equivalent gains as close as possible to the digital counterpart. Fig. 3.27 and Fig. 3.28 illustrate the transient responses of the analog controller. When load changes from 0.75 A to 0.187 A or vice versa, the system's response time is less than 1.5 ms to reach steady state with a maximum transient error less than 0.9 V . Therefore, the analog controller performs a little bit better than the digital controller. On the other hand, the digital controller demonstrates some advantages over analog controller. According to the experimental results, the analog controller remains stable for input voltages up to 19 V . The switching frequency alters a little bit when the load changes due to the slope compensation circuit.


Fig. 3.27 Transient response using analog controller when the load change is from 0.75 A to 0.187 A . Output voltage: $200 \mathrm{mV} /$ DIV; Time: $200 \mu \mathrm{~s} /$ DIV


Fig. 3.28 Transient response using analog controller when the load change is from 0.187 A to 0.75 A . Output voltage: $200 \mathrm{mV} / \mathrm{DIV}$; Time: $200 \mu \mathrm{~s} /$ DIV

## 3-5. Conclusion

Presented in this chapter is the practical design of a microcontroller-based PCMC boost converter. The PIC16C782 provides a one-chip solution for a PCMC DC-DC converter with the exception of a voltage follower. The on-board peripherals of the PIC16C782 are suitable and critical in designing the PCMC dc-dc converter. The PIC16C82 also provides the mechanism to implement slope compensation, which allows PCMC DC-DC converters to operate for duty cycles greater than $50 \%$. Practical issues in designing a microcontroller-based peak CMC boost converter are briefly discussed.

Experimental results are presented, and encouragingly demonstrate the performance that a microcontroller-based PCMC DC-DC converter can achieve. An analog controller based on a UC3842 is also designed for comparison.

Though this microcontroller-based PCMC system is designed for a boost converter, it can be directly applied to all major converters with very minor modifications.

## Chapter 4

## Microcontroller-Based Average Current-Mode Control

This chapter presents a practical implementation of average current-mode control for a boost converter using an 8 -bit microcontroller. The design principles of the hybrid control method used in PCMC power converter systems are extended to an ACMC boost converter, which proves that the hybrid method can be used in both PAMC and ACMC power converter systems. This microcontroller-based hybrid ACMC controller has been compared to a pure analog ACMC controller based on a UC3886 from Texas Instruments.

## 4-1. Modiling Average Current-Mode Control

The difference between ACMC and PCMC is that a current amplifier is inserted in the current loop for ACMC. The complete current loop is shown in Fig. 4.1, in which $\hat{i}_{L}$ is the inductor current, $R_{i}$ is linear gain of the current-sense network, $\hat{v}_{c}$ is the control reference from the voltage loop, $V_{m}$ is the peak-to-peak voltage of the ramp signal, $S_{n}$ is


Fig. 4.1 Typical current loop compensator
the sensed inductor current slope when the switch is turned on, and $S_{n}{ }^{\prime}$ is the signal slope at the output of the current amplifier (or the input of the comparator). The gain of this current amplifier can be expressed as:

$$
\begin{equation*}
G_{C A}(s)=\frac{K_{c}\left(1+s / \omega_{z}\right)}{s\left(1+s / \omega_{p}\right)}, \tag{4-1}
\end{equation*}
$$

where $K_{c}=\frac{1}{R_{l}\left(C_{f p}+C_{f z}\right)}, \omega_{z}=\frac{1}{R_{f} C_{f z}}, \omega_{p}=\frac{C_{f p}+C_{f z}}{R_{f} C_{f p} C_{f z}}$.
The control-to-output transfer function with the current loop closed is useful in designing the voltage loop compensator. However, because of the insertion of the current amplifier, the ACMC model is more complicated than the PCMC model. Various ACMC models developed in the past years can be used to obtain the control-to-output transfer function $G_{v c}(s)$ [4, 44-53]. Some ACMC models are based on a small ripple assumption [4, 44], where the ripple of the output of the current error amplifier is neglected. The model proposed by J. Sun and R.M Bass [44] may be the simplest one. In this model, not only are the feed forward gain of the input voltage and feedback gain of the output voltage neglected, the sampling effect in the current loop is also neglected. Thus, the model can be simplified as shown in Fig. 4.2. Therefore, when neglecting the ESR of the output capacitor, $G_{v c}(s)$ can be written as:

$$
\begin{equation*}
G_{v c}(s)=\frac{\hat{v}_{o}}{\hat{v}_{c}}=\frac{F_{m}\left[1+G_{C A}(s)\right] G_{v d}(s)}{1+T_{c}(s)} \tag{4-2}
\end{equation*}
$$

where $G_{v d}(s)$ is the transfer function of duty cycle to output voltage for the power stage, $F_{m}$ is the modulator gain, and $T_{c}(s)$ is the current loop gain. The modulator gain $F_{m}$ is the gain introduced by the comparator, and it can be computed by:


Fig. 4.2 Sun and Bass' small signal model for an ACMC converter [44]

$$
\begin{equation*}
F_{m}=\frac{1}{V_{m}} . \tag{4-3}
\end{equation*}
$$

The current loop gain $T_{c}(s)$ is:

$$
\begin{equation*}
T_{c}(s)=R_{i} F_{m} G_{C A}(s) G_{i d}(s) . \tag{4-4}
\end{equation*}
$$

where $G_{i d}(s)$ is the duty cycle to inductor current transfer function. Although this model is simple, it neglects the feedback and the feedforward terms, the sampling effect in the current loop ripple, as well as the ripple in the output of the current amplifier. When the inductor and capacitor are not large enough, the current ripple in the inductor and voltage ripple at the output may be too large to ignore. In addition, when the gain of the current amplifier is high, the model is inaccurate. All these may lead to an inaccurate design. Therefore, many models have attempted to include the effect of inductor ripple and sampling effect on the dynamics of an ACMC converter [45-53].
T. Suntio, etal. [46-47] expended the previous model by including the dynamic effects of inductor current ripple, and the resulting control-to-output transfer function is:

$$
\begin{equation*}
G_{v c}(s)=\frac{\hat{v}_{o}}{\hat{v}_{c}}=\frac{F_{m}\left[1+G_{C A}(s)\right] G_{v d}(s)}{1+T_{c}(s)+T_{v}(s)}, \tag{4-5}
\end{equation*}
$$

where $T_{v}(s)$ is voltage loop gain. $T_{v}(s)$ is computed by:

$$
\begin{equation*}
T_{v}(s)=F_{m} q_{0} G_{v d}(s), \tag{4-6}
\end{equation*}
$$

where $q_{0}$ is a coefficient depending on the topology. Compared to (4-2), an extra voltage loop gain $T_{v}(s)$ is added. The expression of the modulator gain $F_{m}$ is also different, since one more term is added in the denominator:

$$
\begin{equation*}
F_{m}=\frac{1}{V_{m}+\frac{K_{l} V_{o}\left(D^{\prime}-D\right)}{2 L f_{s}}} \tag{4-7}
\end{equation*}
$$

where $K_{l}$ is an coefficient derived from the current loop compensator, and can be expressed as (referring to Fig. 4.1):

$$
\begin{equation*}
K_{l}=\frac{R_{f} C_{f z}}{R_{l}\left(C_{f p}+C_{f z}\right)} . \tag{4-8}
\end{equation*}
$$

For a boost converter, $q_{0}$ can be expressed as:

$$
\begin{equation*}
q_{0}=\frac{K_{l} D D^{\prime}}{2 L f_{s}} \tag{4-9}
\end{equation*}
$$

Since this model includes the inductor ripple effect, it is more accurate at the expense of more complicated expressions.

In [52-53], another ACMC small-signal model is derived utilizing previous results based on Ridley's PCMC model [23-25]. This model is illustrated in Fig. 4.3, $K_{f}$ is the feed-forward gain, $K_{r}$ is the feedback gain, and $H_{e}(s)$ is the sampling gain. $G_{s}(s)$ and $G_{p}(s)$


Fig. 4.3 Tang's small-signal model for ACMC converter [52-53]
are derived from the current amplifier, and can be computed by (referring to Fig. 4.1):

$$
\begin{align*}
& G_{s}(s)=\frac{K_{c}\left(1+\frac{s}{\omega_{z}}\right)}{s},  \tag{4-10}\\
& G_{p}(s)=\frac{1}{\left(1+\frac{s}{\omega_{p}}\right)}, \tag{4-11}
\end{align*}
$$

where $K_{c}, \omega_{p}$ and $\omega_{z}$ are identical to the values in (4-1).
The sampling gain $H_{e}(s)$ and the modulator gain $F_{m}$ can be computed by:

$$
\begin{gather*}
H_{e}(s) \cong 1+\frac{s}{\omega_{n} Q_{z}}+\frac{s^{2}}{\omega_{n}^{2}},  \tag{4-12}\\
\omega_{n}=\frac{\pi}{T_{s}},  \tag{4-13}\\
Q_{z}=-\frac{2}{\pi}  \tag{4-14}\\
F_{m}=\frac{1}{\left(S_{e}+S_{n}^{\prime}\right) T_{s}} \tag{4-15}
\end{gather*}
$$

where $S_{e}$ is the slope of the external ramp, $S_{n}{ }^{\prime}$ is the modified slope of the inductor current waveform, as illustrated in Fig. 4.1. $S_{n}^{\prime}$ ' can be computed by [52-53]:

$$
\begin{equation*}
S_{n}^{\prime}=K_{c} S_{n}\left[D T_{s}+\left(\frac{1}{\omega_{z}}-\frac{1}{\omega_{p}}\right)\left(1-e^{-\omega_{p} D T_{s}}\right)\right] . \tag{4-16}
\end{equation*}
$$

Feedforward and feedback gain terms $K_{f}$ and $K_{r}$ are different for different types of converters. Table 4-1 lists $K_{f}$ and $K_{r}$ for three basic types of converters, where:

$$
\begin{gather*}
\xi=\alpha D T_{s}+\alpha \beta\left(1-e^{-D T_{s} / \gamma}\right)  \tag{4-17}\\
\zeta=\frac{\alpha\left(D T_{s}\right)^{2}}{2}+\alpha \beta D T_{s}-\alpha \beta \gamma\left(1-e^{-D T_{s} / \gamma}\right), \tag{4-18}
\end{gather*}
$$

Table 4.1 Feedforward and feedback gains for ACMC [52-53]

|  | Buck | Boost | Buck-Boost |
| :---: | :---: | :---: | :---: |
| $K_{f}$ | $-\frac{D D^{\prime} T_{s}}{2 L} \xi-\frac{R_{i}}{2 L} \zeta$ | $-\frac{D^{\prime} T_{s}}{2 L} \xi-\frac{R_{i}}{2 L} \zeta$ | $-\frac{D D^{\prime} T_{s}}{2 L} \xi$ |
| $K_{r}$ | $-\frac{D^{\prime} T_{s}}{2 L} \xi-\frac{R_{i}}{2 L} \zeta$ | $-\frac{D^{\prime} T_{s}}{2 L} \xi$ | $-\frac{D^{\prime} T_{s}}{2 L} \xi$ |

$$
\begin{gather*}
\alpha=\frac{1}{R_{f}\left(C_{f p}+C_{f z}\right)},  \tag{4-19}\\
\beta=\frac{R_{f} C_{f z}^{2}}{\left(C_{f p}+C_{f z}\right)},  \tag{4-20}\\
\gamma=\frac{R_{f} C_{f p} C_{f z}}{\left(C_{f p}+C_{f z}\right)} . \tag{4-21}
\end{gather*}
$$

According to Fig. 4.3, the control-to-output transfer function can be expressed as:

$$
\begin{equation*}
G_{v c}(s)=\frac{\hat{v}_{o}}{\hat{v}_{c}}=\frac{F_{m} G_{p}(s) G_{s}(s) G_{v d}(s)}{1+R_{i} F_{m} H_{e}(s) G_{s}(s) G_{i d}(s)-K_{r} F_{m} G_{v d}(s)} . \tag{4-22}
\end{equation*}
$$

This model uses the sampling gain $H_{e}(s)$ directly from the PCMC model without strict derivation. Therefore, it can be inaccurate if the gain of the current amplifier is high. Also, this model contains a nonlinear expression for the modulator gain, which adds complexity to the model.

The Bode plots of $G_{v c}(s)$ of the three models for the ACMC boost converter used in this implementation are plotted in Fig. 4.4. The measured transfer function is also plotted for comparison. According to Fig. 4.4, the three models can provide very accurate predictions at low frequency. However, all of them deviate from the measurement at above half of the switching frequency, while Tang's model is relatively more accurate. Since the actual $G_{v c}(s)$ has an infinite number of poles, all of the theoretical models are based on some approximations. Therefore, $G_{v c}(s)$ from the experimental measurement is always the first choice when it is possible, as in this implementation.


Fig. 4.4 Comparison of the ACMC models

## 4-2. System Design

## 4-2-1. System overview

The block diagram for the microcontroller-based hybrid ACMC boost converter is shown in Fig. 4.5. In the current loop, a current amplifier, which is constructed using the on-board OPA module, is inserted to obtain the average value of the inductor current, so the output of the current amplifier is proportional to the average inductor current with some ripple. Its current reference is calculated in software using a PI compensator. Using the on-chip analog comparator $\mathrm{C}_{1}$, the amplified error from the current amplifier OPA is compared to a sawtooth reference waveform produced by the PSMC module. A pulse is generated when they are equal, and is sent to the PSMC module to generate a


Fig. 4.5 Block diagram of a hybrid ACMC converter controlled by a PIC16C782 microcontroller

PWM signal that controls the switch.
Just as in designing a PCMC system, the current loop should be constructed first when designing an ACMC power converter. Three components in the current loop need to be designed or configured: OPA, $\mathrm{C}_{1}$ and PSMC module. Once the current loop is designed, the converter with the closed current loop can be treated as a new open loop plant with $G_{v c}(s)$ as its control-to-output transfer function. When using a microcontroller, the sampling operation and digital to analog conversion should be considered and modeled in the design procedure. When $G_{v c}(s)$ is obtained, the voltage loop compensator
$G_{c}(z)$ can be designed based on $G_{v c}(s)$ as a typical digital control system. Thus, the block diagram of the ACMC system is the identical to the PCMC system shown in Fig. 3.5. The hidden difference is that they have different control to output transfer function $G_{v c}(s)$.

In this implementation, the operating specifications and circuit parameters are listed as following:

- Nominal input voltage: 12 V
- Nominal output voltage: 28 V
- Switching frequency: 156.25 kHz :
- Nominal load: $50 \Omega$ ( $0.56 \mathrm{~A}, 15.68 \mathrm{~W}$ )
- Operating mode: CCM
- Inductor: $257 \mu \mathrm{H}$
- Output capacitor: $57.35 \mu \mathrm{~F}$


## 4-2-2. Current loop design

The complete current loop realized on the PIC16C782 is shown in Fig. 4.6. Since both the OPA module and the comparator $\mathrm{C}_{1}$ are analog peripherals inside the microcontroller, the current loop is the same as a traditional analog ACMC case. Therefore, no complex algorithm is required to estimate the inductor current.

The current amplifier in the current loop can be designed by using the on-board analog operational amplifier module (OPA module) with several external capacitors and resistors, as illustrated in Fig. 4.6. When designing the current amplifier, its gain should be chosen first. Since the down slope of the amplified inductor current error must not exceed the slope of the external ramp, there is an upper limitation on the current amplifier gain $G_{C A}$ at the switching frequency $f_{s}$. This indirectly establishes the maximum current


Fig. 4.6 Current loop for hybrid ACMC power converter realized on a PIC16C782
loop gain and crossover frequency. $G_{C A}$ is approximately $R_{f} / R_{l}$ at the switching frequency, and can be expressed by [4, 44 and 48]:

$$
\begin{equation*}
G_{C A} \cong \frac{R_{f}}{R_{l}}<\min \left\{\frac{2 V_{m} f_{s} L}{V_{g} R_{i}}, \frac{V_{m} f_{s} L}{V_{o} R_{i}}\right\} . \tag{4-23}
\end{equation*}
$$

Equations (4-1) and (4-23) set the criteria to choose $R_{f}$ and $R_{l}$. According to desired locations of the pole and zero, capacitor values can be selected. In this implementation, the zero $\omega_{z}$ is placed at one-half of $\omega_{0}$, which is given by $\omega_{0}=1 / \sqrt{L C}$, to maximize the current loop crossover frequency. The high frequency pole $\omega_{p}$, is placed at one-half of the switching frequency $f_{s}$ to filter out the switching frequency ripple. The following steps are employed to design the current amplifier:

1. Compute $R_{f}$ and $R_{l}$ such that the current amplifier has a smaller gain than
the maximum gain allowed at switching frequency:

$$
\begin{equation*}
\frac{R_{f}}{R_{l}} \leq G_{C A \max }=\frac{V_{m} f_{s} L}{V_{o} R_{i}}=\frac{3 \times 156.25 \times 10^{3} \times 109.8 \times 10^{-6}}{28 \times 0.1}=18.38 . \tag{4-24}
\end{equation*}
$$

Ideally, $V_{m}$ should be 5 V (which is the supply voltage of the microcontroller) to achieve the maximum gain. However, $v_{m}$ is generated by an RC network, which will be discussed in detail later, so $V_{m}$ has to be set below 5 V to ensure an approximate linear ramp signal. Select $R_{f}=91 \mathrm{k} \Omega$ and $R_{l}=5.1 \mathrm{k} \Omega$, so $\frac{R_{f}}{R_{l}}=17.8$, which satisfies the requirement in (4-24) that $\frac{R_{f}}{R_{l}} \leq 18.38$.
3. Compute the resonant frequency $\omega_{0}$ of the power stage:

$$
\begin{equation*}
\omega_{0}=1 / \sqrt{L C}=1 / \sqrt{109.8 \times 10^{-6} \times 57.35 \times 10^{-6}}=12.6 \times 10^{3} \mathrm{rad} / \mathrm{s} . \tag{4-25}
\end{equation*}
$$

4. Compute $C_{f z}$ according to the location of the zero $\omega_{z}$. In this implementation, $\omega_{z}$ is placed at one-half of $\omega_{0}$ :

$$
\begin{gather*}
\omega_{z}=\frac{1}{R_{f} C_{f_{z}}}=\frac{\omega_{0}}{2} .  \tag{4-26}\\
C_{f_{z}}=\frac{2}{R_{f} \omega_{0}}=\frac{2}{91 \times 10^{3} \times 12.6 \times 10^{3}}=1.74 \times 10^{-9} \mathrm{~F} \cong 1500 \mathrm{pF} . \tag{4-27}
\end{gather*}
$$

The reason that $C_{f z}$ is selected 1500 pF instead of 1740 pF is that this is the closest available value to 1740 pF . Thus, the zero is actually at:

$$
\begin{equation*}
\omega_{z}=\frac{1}{91 \times 10^{3} \times 1500 \times 10^{-12}}=7.3 \times 10^{3} \mathrm{rad} / \mathrm{s} . \tag{4-28}
\end{equation*}
$$

5. Find $C_{f p}$ according the location of the pole $\omega_{p}$. The typical $\omega_{p}$ location is between one-third and one-half of the switching frequency. In this implementation, onehalf of the switching frequency is selected:

$$
\begin{equation*}
\omega_{p}=\frac{\left(C_{f p}+C_{f z}\right)}{R_{f} C_{f p} C_{f z}}=\frac{2 \pi f_{s}}{2}=156.25 \pi \times 10^{3} \mathrm{rad} / \mathrm{sec} . \tag{4-29}
\end{equation*}
$$

Substitute $R_{f}=91 \mathrm{k} \Omega$ and $C_{f_{z}}=1500 \mathrm{pF}$ into (4-29), we have:

$$
\begin{gather*}
C_{f p}+1.5 \times 10^{-9}=156.25 \pi \times 10^{3} \times 91 \times 10^{3} \times 1.5 \times 10^{-9} \times C_{f p} .  \tag{4-30}\\
C_{f p}=22.7 \times 10^{-12} \cong 22 \mathrm{pF} . \tag{4-31}
\end{gather*}
$$

Thus, the pole is actually located at:

$$
\begin{equation*}
\omega_{p}=\frac{\left(C_{f p}+C_{f z}\right)}{R_{f} C_{f p} C_{f z}}=\frac{(22+1500) \times 10^{-12}}{91 \times 10^{3} \times 22 \times 10^{-12} \times 1.5 \times 10^{-9}}=5.07 \times 10^{5} \mathrm{rad} / \mathrm{sec} \tag{4-32}
\end{equation*}
$$

At this time,

$$
\begin{equation*}
K_{c}=\frac{1}{R_{l}\left(C_{f p}+C_{f z}\right)}=\frac{1}{5.1 \times 10^{3} \times(22+1500) \times 10^{-12}}=1.28 \times 10^{5} . \tag{4-33}
\end{equation*}
$$

The Bode plot of this current amplifier is shown in Fig. 4.7.
Notice that both of the inputs of the current amplifier should be within the normal operational range of the OPA module. In addition, the magnitude difference of the two inputs should not be too large. The reference of the current amplifier $v_{c}$, referring to Fig. 4.5 , is the output of $\mathrm{D} / \mathrm{A}$ converter. In order to ensure enough resolution, the $\mathrm{D} / \mathrm{A}$ output should be around 2.5 V at nominal operating condition. Therefore, it is desired that the sense resistor should provide adequate linear gain $R_{i}$ such that the sensed voltage


Fig. 4.7 Bode plot of the current amplifier
$v_{s}=R_{i} i_{L}$ is around 2.5 V . However, the actual $v_{s}$ is well below 0.1 V , much lower than the reference voltage $v_{c}$. The simplest way to solve this problem is to increase the value of the sense resistor. However, this approach will significantly increase the power loss in the power stage, so it is not a preferable method.

Another simple way to solve this problem is to add a dc bias voltage to the sensed current signal directly, as illustrated in Fig. 4.8. However, if the dc bias voltage is much higher than the sensed signal, the gain of the current amplifier is seriously restricted. Another commonly used approach is to amplify the sensed current signal by an opamp, as shown in Fig. 4.9. This amplifier also acts as a low-pass filter to filter out switching spikes. Indeed, many power converters use this method to condition the sensed current. However, this method requires an extra opamp that increases the cost and complexity of


Fig. 4.8 Sensed current signal is biased by a dc voltage


Fig. 4.9 Sensed current signal is amplified by an opamp
the circuit.
In this implementation, instead of manipulating the sensed current signal, the current reference of the current amplifier is modified. As shown in Fig. 4.10, the D/A output, instead of being sent directly to the current amplifier, is connected to a voltage divider. This method scales down the $\mathrm{D} / \mathrm{A}$ output, such that it is compatible with the low sensed current signal. This method is simple and low-cost, but it can effectively solve the problem.

Since there is no internal analog path between the OPA module and the on-board comparator $\mathrm{C}_{1}$, the output of the current amplifier $v_{c a}$ is sent out of the PIC16C782


Fig. $4.10 \mathrm{D} / \mathrm{A}$ output is scaled down by a voltage divider
through an analog IO port, and then is sent to $\mathrm{C}_{1}$ through another analog IO port. The waveforms at $\mathrm{C}_{1}$ inputs are shown in Fig. 4.11, where $v_{m}$ is the ramp signal at the $\mathrm{C}_{1}$ negative input. It can be seen that $v_{c a}$ has ripple, which makes the design of the current loop more complicated.

In the hybrid PCMC scheme, a ramp signal for slope compensation is generated by the PSMC module and an external RC network. In the hybrid ACMC scheme, although slope compensation is eliminated, the ramp signal $v_{m}$ is still needed as the reference for the comparator. For a fixed supply voltage ( 5 V in this implementation), referring to Fig. 4.6, $v_{m}$ is directly defined by $R$ and $C$. For an RC circuit, the time


Fig. 4.11 The waveforms at $C_{1}$ inputs
constant is $\tau=R C$, and $R$ and $C$ can be selected by:

$$
\begin{equation*}
v_{m}(t)=5-5 e^{-t / R C} \Rightarrow R C=-\frac{t}{\ln \frac{5-v_{m}}{5}} . \tag{4-34}
\end{equation*}
$$

When designing the RC network to generate $v_{m}$, the peak value of $v_{m}$, referred to as $V_{m}$, should be chosen as high as possible, according to (4-23). However, the linearity of $v_{m}$ should be considered. Therefore, $v_{m}$ should not be close to 5 V at any possible duty cycle. When the maximum duty cycle is specified, $v_{m}$ should be below 5 V at maximum duty cycle. For example, in this implementation, let $v_{m}$ equal 3.8 V at $75 \%$ duty cycle. Since $f_{s}=156.25 \mathrm{kHz}$, so $T_{s}=6.4 \mu \mathrm{~s}$. Thus,

$$
\begin{equation*}
R C=-\frac{6.4 \times 10^{-6} \times 0.75}{\ln \frac{5-3.8}{5}}=3.363 \times 10^{-6} \mathrm{~s} \tag{4-35}
\end{equation*}
$$

Choose $C=100 \mathrm{pF}$, then $R=33.63 \mathrm{k} \Omega \approx 33 \mathrm{k} \Omega$. Based experimental measurement, the actual value of $v_{m}$ reaches 3.4 V at $75 \%$ duty cycle $\left(D_{\max }\right.$, maximum duty cycle). The equivalent $V_{m}$ is:

$$
\begin{equation*}
V_{m}=\left.\frac{v_{m}(t)}{D_{\max }}\right|_{t=D_{\max } T_{s}}=\frac{3.4}{0.75}=4.6 \mathrm{~V} . \tag{4-36}
\end{equation*}
$$

## 4-2-3. Voltage loop design

Once the current loop is designed, the converter with the closed current loop can be treated as a new open loop plant with $G_{v c}(s)$ as its control-to-output transfer function. The voltage loop compensator $G_{c}(z)$ can be designed based on $G_{v c}(s)$.

In order to get higher $\mathrm{A} / \mathrm{D}$ resolution, just as in the hybrid PCMC system, a level-
shift circuit was designed such that the $A / D$ result represents a "windowed" range of the output voltage around the nominal value. In this implementation, the "window" is in the range of 25.67 V and 30.33 V for a 28 V nominal output voltage. The level shifter can be built from an external operational amplifier with several external resistors. A voltage buffer (voltage follower) is used to ensure accurate measurement of the output voltage. The circuit is similar to that of the hybrid PCMC converter (Fig. 3.4). The main difference is that, in the hybrid PCMC converter, the level-shift circuit is constructed using the on-board opamp OPA module. However, in the ACMC system, since the OPA module is used as the current amplifier, two external opamps, although they are integrated in one IC chip, are used to construct the level-shift circuit and the voltage buffer.

Due to the limited number of analog I/O ports of the PIC16C782, the full-range output voltage is not measured. However, this restriction does not degrade the performance of the controller because the output voltage variation during normal operation is always inside the windowed range even under large disturbances. When the converter starts up, the output voltage is out of the "windowed" range, and an overshoot may occur. At this time, a full-range measurement may be required. However, an appropriately designed voltage loop compensator can limit the overshoot to a small value, which has been verified by checking the step response of the ACMC boost converter. In addition, a soft start can be achieved easily by adding extra code before the software enters normal operating mode.

In this implementation, the voltage loop compensator $G_{c}(z)$, just as the PCMC system described in Chapter 3, is a digital PI controller, and the design procedure is also
very similar. Fig. 4.12 compares the Bode plots of $G_{v c}(s)$ of the ACMC boost converter at different loads ( $0.187 \mathrm{~A}, 0.56 \mathrm{~A}$ and 0.75 A ). The system with a 0.75 A load is chosen to compute the PI controller. Using MATLAB to fit measured frequency response data, $G_{v c}(s)$ can be reduced to a second order system for controller design. The Bode plots of $G_{v c}(s), G_{v c}(z)$ and $G_{v c}(z) z^{-1}$ of the ACMC boost converter when the load is 0.75 A (the voltage feedback gain $H_{v}$ is included) are compared in Fig. 4.13.

In this implementation, based on $H_{v} G_{v c}(z) / z$, the zero of the digital PI controller is placed at $2930 \mathrm{rad} / \mathrm{s}$, and the $s$-domain compensator can be expressed as:

$$
\begin{equation*}
G_{c}(s)=K_{P}+\frac{K_{I}}{s}=0.5058+\frac{1482}{s}=\frac{0.5058(s+2930)}{s} . \tag{4-37}
\end{equation*}
$$



Fig. 4.12 Bode plots of $G_{v c}(s)$ for different loads


Fig. 4.13 Bode plots of ACMC boost converter when the load is 0.75 A
where $K_{P}$ is the proportional gain and $K_{I}$ is the integral gain. The $s$-domain PI controller is then converted to a z -domain transfer function as:

$$
\begin{equation*}
G_{c}(z)=K_{P}+\frac{K_{I} T_{s} z}{z-1}=K_{P}+\frac{K_{I}^{\prime} z}{z-1}=0.5058+\frac{0.03794 z}{z-1} . \tag{4-38}
\end{equation*}
$$

According to $G_{c}(z)$, the control effort $v_{c}(k)$ can be computed using the following difference equation:

$$
\begin{equation*}
v_{c}(k)=K_{P}+K_{I}^{\prime} \sum_{j=0}^{k} e(j)=0.5058+0.03794 \sum_{j=0}^{k} e(j), \tag{4-39}
\end{equation*}
$$

where $e(k)$ is the error signal which is computed digitally by comparing the ADC result of the output voltage $v_{o}(k)$ and a voltage reference $V_{r e f}(k) . \quad V_{r e f}(k)$ is fixed at 7 Fh , which
represents a fixed nominal output voltage.
Power-of-two arithmetic is employed in this implementation. Therefore, $K_{P}=$ $0.5, K_{I}^{\prime}=1 / 32=0.03125$ are selected. The software keeps track of the sign by storing the error sign in a flag bit.

The DAC module inside the PIC16C782 is used to convert the output of the digital PI controller into an analog signal $v_{c}(t)$. The DAC reference voltage can only be 5 V or 3.072 V ; other reference voltages are not practical in this implementation because of restrictions on the I/O pins. As discussed in Section 4-2-2, a voltage divider made of two resistors is used to scale down the DAC output. This voltage divider introduces an extra gain to the voltage loop, which can provide more flexibility to design the PI controller and compensate the drawback of power-of-two arithmetic by adjusting the gain of the voltage divider, and hence adjusting $K_{P}$ and $K_{I}^{\prime}$.

In this implementation, the maximum duty cycle $D_{\max }$ is set to be $75 \%$.

## 4-3. Analog ACMC Power Converter

For comparison, an analog controller using an UC3886 from Texas Instruments [54-56] was designed to control the same boost converter.

The UC3886 was developed to implement dc to dc power converter system with ACMC. As illustrated in Fig. 4.14, this 16-pin IC chip internally includes one PWM comparator, three amplifiers (voltage amplifier, current amplifier and current sense amplifier), precision reference (trimmed 5 V reference at an output pin), RS latch (to ensure latched operation), 1.5 A totem pole output stage, and an oscillator (to provide fix frequency timing for RS latch and slope compensation). The current sense amplifier
inside the UC3886 can amplify the sensed current, and eliminate the need for external waveform synthesis circuitry. Using a UC3886, a one-chip solution for the ACMC controller, including input conditioning controller and gate drive, can be achieved. In addition to the basic ACMC functions, a UC3886 also has comprehensive supplementary functions, such as undervoltage lockout, short circuit protection, current limit for high load and soft start.

Since both of the current loops using the PIC16C782 and the UC3886 are implemented using analog circuitry, the design procedures for the current loops using the UC3886 were similar. In the voltage loop, an analog PI controller was implemented. This analog PI controller contains gains equivalent to the digital counterparts as close as possible.


Fig. 4.14 Internal block diagram of UC3886 [54]

The schematic for the ACMC boost converter system is illustrated in Fig. 4.15. For the UC3886, the maximum duty cycle $D_{\max }$ is determined by the resistor $R_{T}$, and can be expressed as:

$$
\begin{equation*}
D_{\max }=1-\frac{2}{4 \times 10^{-3} R_{T}} . \tag{4-40}
\end{equation*}
$$

In this implementation, $D_{\max }=0.75$ is selected. Therefore,


Fig. 4.15 Schematic of the ACMC boost converter controlled by a UC3886

$$
\begin{equation*}
R_{T}=\frac{2}{4 \times 10^{-3}\left(1-D_{\max }\right)}=\frac{2}{4 \times 10^{-3} \times(1-0.75)}=2 \mathrm{k} \Omega . \tag{4-41}
\end{equation*}
$$

The switching frequency is found by following equation:

$$
\begin{equation*}
f_{s}=\frac{2\left(4 \times 10^{-3} R_{T}-2\right)}{1.8 \times 4 \times 10^{-3} C_{T} R_{T}^{2}} . \tag{4-42}
\end{equation*}
$$

Substitute $f_{s}=156.25 \mathrm{kHz}$ and $R_{T}=2 \mathrm{k} \Omega$ into (4-42), $C_{T}$ is obtained:

$$
\begin{equation*}
C_{T}=\frac{2\left(4 \times 10^{-3} \times 2 \times 10^{3}-2\right)}{1.8 \times 4 \times 10^{-3} \times 156.25 \times 10^{3} \times\left(2 \times 10^{3}\right)^{2}}=2.67 \times 10^{-9} \mathrm{~F}=(2.2+0.47) \mathrm{nF} . \tag{4-43}
\end{equation*}
$$

The current sense amplifier (CSA) inside UC3886 can provide adequate gain and offset to the sensed inductor current. The gain $G_{C S A}$ of CSA must be larger than 5 ( 14 dB ), otherwise it is not stable. In addition, $G_{C S A}$ has an upper limit:

$$
\begin{equation*}
G_{C S A} \leq \frac{2.5 \times 10^{6}}{f_{s}}=\frac{2.5 \times 10^{6}}{156.25 \times 10^{3}}=16(24 \mathrm{~dB}) \tag{4-44}
\end{equation*}
$$

$G_{C S A}$ is given by the resistors $R_{1}$ and $R_{2}$, and is set to be 10 in this implementation:

$$
\begin{equation*}
G_{C S A}=\frac{R_{2}}{R_{1}}=10 . \tag{4-45}
\end{equation*}
$$

Let $R_{I}=5 \mathrm{k} \Omega$, and $R_{2}=50 \mathrm{k} \Omega$. Then, the CSA output $V_{I S O}$ is expressed as:

$$
\begin{equation*}
V_{I S O}=V_{B U F}+V_{S E N S E} G_{C S A}=2.5+10 I_{L} R_{i}, \tag{4-46}
\end{equation*}
$$

where $V_{\text {SENSE }}$ is the output voltage feedback at Pin VSENSE, and $V_{B U F}$ is dc bias voltage, and is set to 2.5 V in this implementation. Indeed, $V_{B U F}$ equals to $V_{\text {command }}$, which is set by resistors $R_{3}$ and $R_{4}$. In this implementation, $R_{3}=R_{4}=40 \mathrm{k} \Omega$, such that $V_{B U F}=2.5 \mathrm{~V}$. $V_{\text {command }}$ is also the reference of the voltage amplifier.

The ramp signal $v_{m}$ used as the reference of the comparator is generated internally by the on-board oscillator. The signal $v_{m}$ rings from 1 V to 2.8 V . Therefore, $\Delta v_{m}$, the peak-to-peak voltage of $v_{m}$, equals to $2.8-1=1.8 \mathrm{~V}$. Thus, the equivalent full-cycle peak-to-peak voltage $V_{m}$ can be computed as:

$$
\begin{equation*}
V_{m}=\left.\frac{\Delta v_{m}(t)}{D_{\max }}\right|_{t=D_{\max } T_{s}}=\frac{(2.8-1)}{0.85}=2.12 \mathrm{~V} \tag{4-47}
\end{equation*}
$$

According to (4-23), the ratio of $R_{f}$ and $R_{l}$ is defined by the maximum gain of the current amplifier (CA):

$$
\begin{equation*}
\frac{R_{f}}{R_{l}} \leq G_{C A \max }=\frac{V_{m} f_{s} L}{V_{o}\left(R_{i} G_{C S A}\right)}=\frac{2.12 \times 156.25 \times 10^{3} \times 109.8 \times 10^{-6}}{28 \times 0.1 \times 10}=1.3 \tag{4-48}
\end{equation*}
$$

Equation (4-48) shows that the CA gain is as low as 1.3 . This is because the linear gain to the inductor current has been increased by CSA. In other words, the upper limit of the CA gain is traded with the CSA gain. However, $V_{m}$ is only $2.12 \mathrm{~V} . v_{m}$ is in the range of 1 V and 2.8 V , which is a specification of the UC3886, and cannot be changed. Therefore, the only way to further increase $V_{m}$ (equivalent to increase the slope of the ramp signal) is to further decrease the maximum duty cycle below $75 \%$, which is undesirable in this implementation. Compared with $V_{m}=4.6 \mathrm{~V}$ in the PIC16C782 system, this restriction further limits $G_{C A m a x}$.

Select $R_{f}=31 \mathrm{k} \Omega$ and $R_{l}=24 \mathrm{k} \Omega$. Thus:

$$
\begin{equation*}
\frac{R_{f}}{R_{l}}=\frac{31 \mathrm{k} \Omega}{24 \mathrm{k} \Omega}=1.29 \leq G_{C A \max }=1.3 \tag{4-49}
\end{equation*}
$$

According to (4-25), the resonant frequency $\omega_{0}$ of the power stage is $12.6 \times 10^{3}$
$\mathrm{rad} / \mathrm{s}$. Place the zero of $\mathrm{CA} \omega_{z}$ at one-half of $\omega_{0}$ by setting $C_{f z}$ :

$$
\begin{equation*}
C_{f z}=\frac{1}{\omega_{z} R_{f}}=\frac{1}{0.5 \times 12.6 \times 10^{3} \times 31 \times 10^{3}}=5.12 \times 10^{-9} \mathrm{~F} \cong 5.1 \mathrm{nF} . \tag{4-50}
\end{equation*}
$$

$C_{f p}$ is selected based on the location of the pole of $\mathrm{CA} \omega_{p}$, which is at one-half of the switching frequency here. Substitute $R_{f}=31 \mathrm{k} \Omega$ and $C_{f z}=5.1 \mathrm{nF}$ into (4-29), the following equation is obtained:

$$
\begin{equation*}
\frac{\left(C_{f p}+5.1 \times 10^{-9}\right)}{31 \times 10^{3} \times 5.1 \times 10^{-9} C_{f p}}=156.25 \pi \times 10^{3} \mathrm{rad} / \mathrm{s} . \tag{4-51}
\end{equation*}
$$

Solve (4-51), $C_{f p}$ is calculated to be 66.6 pF , and a 68 pF capacitor is selected.
The voltage amplifier compares the output voltage feedback with a voltage reference $V_{\text {command }}$. Since $V_{\text {command }}$ is set to be 2.5 V in this implementation, the voltage divider at the output voltage feedback must provide 2.5 V feedback at nominal conditions. The gain of the voltage amplifier $G_{V A}$ is computed by:

$$
\begin{equation*}
G_{V A}=-\left(\frac{R_{6}}{R_{5}}+\frac{1}{R_{5} C_{f} s}\right)=-\left(K_{p}+\frac{K_{I}}{s}\right) \tag{4-52}
\end{equation*}
$$

Assume that the frequency response of the UC3886 controlled ACMC system is similar to the PIC16C782 controlled system, with the closed current loop, so its analog voltage loop design can be completed:

$$
\begin{gather*}
K_{P}=\left.\frac{1}{H_{v} G_{v c}}\right|_{\omega=3.22 \times 10^{4}}=\frac{1}{10^{(2.59 / 20)}}=0.5058 .  \tag{4-53}\\
K_{I}=0.1 \omega_{1} K_{P}=0.1 \times 2.93 \times 10^{4} \times 0.5058=1482 . \tag{4-54}
\end{gather*}
$$

Choose $R_{5}=20 \mathrm{k} \Omega, R_{6}=10 \mathrm{k} \Omega$, then $C_{f}$ can be computed:

$$
\begin{equation*}
C_{f}=\frac{1}{K_{I} R_{5}}=\frac{1}{1482 \times 20 \times 10^{3}}=3.37 \times 10^{-8} \mathrm{~F} \cong 33 \mathrm{nF} \tag{4-55}
\end{equation*}
$$

In the hybrid ACMC system controlled by the PIC16C782, the sense resistor and the current amplifier provide a gain of 1.78 to the inductor current signal. When the system is controlled by the UC3886, the sense resistor, the current sense amplifier and the current amplifier provide an overall gain of 1.29. Therefore, there is some difference between their gains, so the model used to design the analog controller has an error. For this reason, the system needs to be tuned experimentally. According to experimental results, the system performs best when $R_{5}=24 \mathrm{k} \Omega$.

The soft start ability provided by the UC3886 can be realized by adding the capacitor $C_{s s}$ at the voltage reference $V_{\text {commond }}$. When using the voltage divider to change $V_{R E F}$ to the reference voltage $V_{\text {command }}$, the sum of the two resistors ( $R_{1}$ and $R_{2}$ ) should not be smaller than $2.5 \mathrm{k} \Omega$, such that the soft start time $t_{s s}$ can be long enough without adding a large capacitor. The soft start time $t_{s s}$ is computed by:

$$
\begin{equation*}
t_{s s}=5 C_{s s} \frac{R_{3} R_{4}}{R_{3}+R_{4}} \tag{4-56}
\end{equation*}
$$

Select $t_{s s}=10 \mathrm{~ms}$, then $C_{s s}$ can be computed:

$$
\begin{equation*}
C_{s s}=\frac{t_{s s}\left(R_{3}+R_{4}\right)}{5 R_{3} R_{4}}=\frac{10 \times 10^{-3}(40+40)}{5 \times 40 \times 10^{3}}=10^{-7} \mathrm{~F}=0.1 \mu \mathrm{~F} . \tag{4-57}
\end{equation*}
$$

## 4-4. Experimental Results

The system block diagram of the hybrid ACMC boost converter controlled by the

PIC16C782 is shown in Fig. 4.16. AC coupling is utilized on the oscilloscope channel in measuring the output voltage.

The key component of the control system is the PIC16C782 microcontroller. Its on-board opamp OPA module is used as the current amplifier, and its on-board comparator is used as the PWM comparator. In order to obtain high A/D resolution, a level-shift circuit is constricted using an external opamp. The voltage follower (voltage buffer), which is constructed by an external opamp, is used to condition the voltage feedback. The UC3705N IC is used as the gate drive. Totally, there are three IC chips used for the controller and its interfaces.

When a large disturbance occurs, such as a load change from 0.187 A to 0.75 A (Fig. 4.17), the response time of the hybrid ACMC system was roughly 2.5 ms to reach


Fig. 4.16 An ACMC boost converter controlled by a PIC16C782
steady state with a small overshoot. The maximum transient error was 1.6 V , which is $5.7 \%$ of 28 V . The maximum transient error occurred at 0.4 ms after the load change. In 1.3 ms , the transient error was reduced to 0.1 V , which is $0.36 \%$ of 28 V . The peak of overshoot was only 0.1 V . Compared to the 28 V output voltage, this overshoot ( $0.36 \%$ of 28 V ) was negligible. The steady-state error of the system was approximately zero.

When the load change was from 0.75 A to 0.187 A (Fig. 4.18), the response was similar. The system reached steady state in about 2.6 ms after the load change. The maximum transient error was 1.5 V ( $5.4 \%$ of 28 V output voltage), occurring at 0.45 ms .


Fig. 4.17 Transient response of the hybrid ACMC boost converter when the load change was from 0.75 A to 0.187 A. Output voltage: $500 \mathrm{mV} / \mathrm{DIV}$; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$


Fig. 4.18 Transient response of the hybrid ACMC boost converter when the load change was from 0.187 A to 0.75 A. Output voltage: $500 \mathrm{mV} / \mathrm{DIV}$; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$

The system reduced this transient error down to 0.1 V in about 1.1 ms . The overshoot was about 0.15 V , which is only $0.54 \%$ of 28 V output voltage. Again, the steady-state error of the system was approximately zero.

From Fig. 4.17-4.18, it can seen that the transient error was within the "window" range of the level-shift circuit ( 25.67 V to 30.33 V ) even when a large disturbance occurs. Therefore, full-range measurement of the output voltage was not necessary during normal operation and even large disturbance conditions.

However, at startup, the output voltage was far below 28 V , and surely outside of the "window". It was still possible that a very large disturbance may pull the output voltage out of the "window". In order to analyze the performance under these conditions,
the step response of the hybrid ACMC system was tested by changing the voltage reference. Since the voltage loop is a digital controller, the reference change was realized by setting the voltage reference digitally from 00 h to 7 Fh and vice versa. This was equivalent to change the output voltage from 12 V to 28 V and vice versa. The system was tested under the nominal load condition, that is, the load is $50 \Omega$. Fig. 4.19 shows the response when the voltage reference changes from 00 h to 7 Fh . The output voltage increased from 12 V to 28 V in 1.8 ms , and reached steady state in about 3 ms with a small overshoot of about 1 V , which is $3.57 \%$ of 28 V .

In Fig. 4.20, the voltage reference changed from 7Fh to 00 h . The output voltage decreased from 28 V to 12 V in 2.8 ms . At this time, no overshoot occurred.

The step responses in Fig. 4.19-4.20 show that the system can maintain stability to changes in the voltage reference, and the transient response is smooth. The step change represented in Fig. 4.19 is equivalent to a start up condition, where the output voltage change is from 12 V to 28 V . Since the output voltage is far below the nominal value at the beginning of start up, and is out of the "window" of the level-shift circuit, the calculated control effort is at its maximum, and the difference between the control effort and the voltage reference is 7 Fh . The step responses prove that the system can start up safely and can operate properly for a large disturbance. Therefore, there is no need to measure the full-range of the output voltage for start up if the power stage and the compensator are designed properly.

The analog controller using the UC3886 is designed to control the same boost converter. When the load changes from 0.75 A to 0.187 A , the system's response time


Fig. 4.19 Step response of the hybrid ACMC boost converter for voltage reference changing from 00 h to 7 Fh when load was 0.56 A . Output voltage: $5 \mathrm{~V} / \mathrm{DIV}$; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$


Fig. 4.20 Step response of the hybrid ACMC boost converter for voltage reference changing from 7Fh to 00 h when load was 0.56 A. Output voltage: 5 V/DIV; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$
was about 3.6 ms to reach steady state with maximum transient error of 2.6 V , as shown in Fig. 4.21. Fig. 4.21 also shows the transient response when the load changed from 0.187 A to 0.75 A , where the system took more than 3.4 ms to reach steady state with maximum transient error of 2.4 V . According to the experimental results, the performance of the analog ACMC system controlled by the UC3886 is close but inferior to that of the hybrid ACMC system controlled by the PIC16C782. One reason is that the analog system is a little bit overdamped, while the hybrid system is a little bit underdamped. Also, the design of the analog controller followed all the design criteria of the hybrid controller, so it may not be optimized. In addition, $\Delta v_{m}$ was fixed at 1.8 V on


Fig. 4.21 Transient response of the analog ACMC boost converter when the load change was from 0.75 A to 0.187 A and from 0.187 A to 0.75 A . Top: The load change is from 0.75 A to 0.187 A . Bottom: The load change is from 0.187 A to 0.75 A . Output voltage: $1 \mathrm{~V} / \mathrm{DIV}$; Time: $1 \mathrm{~ms} / \mathrm{DIV}$.
the UC3886, which limited the value of $V_{m}$ and resulted in a smaller overall current loop gain than the hybrid system. More importantly, there were some differences in the circuit realization. Because of the previous restrictions, it may be difficult to claim that the hybrid ACMC system can outperform the analog PCMC system, but it is fair to claim that the hybrid ACMC system can achieve a performance that is equivalent to the analog counterpart. In addition, the analog controller is more susceptible to switching noise.

## 4-5. Conclusion

Presented in this chapter is the practical design of a microcontroller-based average current mode controller for a boost converter. A PIC16C782 microcontroller, which provides a one-chip solution, was used to design an ACMC boost converter. The onboard peripherals of the PIC16C782 are suitable and critical in designing this ACMC boost converter. Experimental results were also presented, and encouragingly demonstrate the performance that a microcontroller-based hybrid ACMC converter can achieve. A pure analog ACMC controller using the UC3886 was designed for comparison.

Though the microcontroller-based hybrid ACMC has only been applied to a boost converter, it can be applied to many different converter topologies with minor modifications.

## CHAPTER 5

## Microcontroller-Based Fuzzy Logic Current-Mode Control

Presented in this chapter is the design and implementation of microcontrollerbased fuzzy logic current-mode control (CMC) for dc-dc converters. Using the PIC16C782 microcontrollers, a fuzzy logic ACMC controller and a fuzzy logic PCMC controller have been designed to control a CCM boost converter.

## 5-1. Fuzzy Logic Control Theory

## 5-1-1. Introduction of fuzzy logic control in power converter systems

As discussed in previous chapters, CMC power converters are essentially nonlinear, time-varying systems. The characteristics of these systems impose difficulties in obtaining accurate mathematical models required for design. Most models used to design the power converter controllers are linear, small signal models. Usually, there is a tradeoff between complexity and accuracy for models in the design process. Parasitic resistances, stray capacitances and leakage inductances increase the difficulty in obtaining accurate models.

In addition, changes in the operating conditions may result in the change in system transfer functions. For example, small signal models based on the assumptions that the signal variation is small, or some parameters, such as input voltage and output load, are constant. These assumptions may be violated during normal operating conditions. Also, the changes in ambient conditions, such as temperature, humidity,
pressure, etc, may change the electrical characteristics of the circuit components. All these create difficulties in designing an optimal control system for power converters.

Fuzzy logic control, as a nonlinear control technique, can be a solution to these difficulties. A fuzzy logic controller is developed based a linguistic description of the system and not a complicated mathematical model, so it is especially suitable for a system for which it is difficult to obtain an accurate mathematical model.

Fuzzy logic, first proposed in the 1960's, is a kind of artificial intelligence that has been extended to handle the vague concept of partial truth - truth values between "completely true" and "completely false". Dr. Lotfi Zadeh, the father of fuzzy logic, published a serial of papers that introduced fuzzy logic theory in the 1960's and 1970's [57-64]. The fuzzy logic approach provides an effective way of capturing the approximate, non-exact nature of the way that human beings describe the real world. In 1970's, fuzzy logic technology began to be applied in control applications. Mamdani and his colleagues made remarkable contributions to the development of fuzzy logic control in 1970's [60-68]. Many other researchers investigated fuzzy logic control intensely [6972], and fuzzy logic control has become a new well-known automatic control scheme.

Fuzzy logic controllers have been successfully used in many applications for many years, such as motor control [80, 85]. Because of the inherent nonlinear and timevarying nature of switching-mode power converters, fuzzy logic controllers are an attractive and promising control method for switching-mode power converters. Therefore, researchers have been investigating the application of fuzzy logic principles to the control of switching-mode power converters [73-78], including CMC converters [7678].

Essentially, fuzzy logic control is a digital control method. It can be realized on a digital signal processor (DSP) [75, 79-80], a field programmable gate arrays (FPGA) [8182], a very-large-scale IC (VLSI) [83-84], a microcontroller [85-86], or other types of digital hardware.

However, the logic and arithmetic calculations of the fuzzy logic algorithm can be difficult to implement on a low-cost general-purpose microcontroller to control real-time switch-mode power converter systems. In [87-88], fuzzy logic control has been successfully applied on a microcontroller to control voltage-mode dc-dc converters. This provides valuable techniques and considerations in designing fuzzy logic controllers on a microcontroller.

In order to investigate the feasibility to implement a fuzzy control algorithm for a real-time CMC dc-dc converter on a low-cost microcontroller, both fuzzy logic ACMC controller and fuzzy logic PCMC controller have been implemented using a PIC16C782 microcontroller to control dc-dc converters.

## 5-1-2. Fuzzy sets

In order to clearly understand the fuzzy logic theory, it is necessary to clarify some of the commonly used terminologies related to fuzzy sets.

Fuzzy set: A set is any collection of objects which can be treated as a whole. To become a member of a set, certain criteria must be satisfied. To become a member of fuzzy set, the criterion is not simply "yes" or "no", "true" or "false". For example, pick a set of good students (academically). If a student's GPA is 4.0, obviously, this student belongs to the set of good students (a member of the set). If a student has GPA of 2.0, he is not a member of the set. How about students who have a GPA of 2.8, 3.0 and 3.2?

Here, the criterion to become a member of the set is fuzzy (non-discrete, non-distinct, continuous).

Degree of membership: Degree of membership is used to describe the transition from membership to non-membership. In the previous example, a student with 3.9 GPA has higher degree of membership than a student with 3.2 GPA to be in the set of good students. An object's grade of membership to a fuzzy set is a real number between 0 and 1 , and usually is denoted by the symbol $\mu$. The higher is the number, the higher degree of membership. Fig. 5.1 shows sets of students and their grades of membership. For a special case where all elements of a set have full membership, i.e., $\mu=1$, the set is called crisp (non-fuzzy, discrete) set.

Universe of discourse: Universe of discourse is the collection of all elements that can come into consideration for a fuzzy set. For example, referring to Fig. 5.1, the fuzzy set of good students is taken from students as a universe of discourse. Every element in the universe of discourse is a member of the fuzzy set to some degree. A very poor student is a member of the set of very good students with $\mu=0$.


Fig. 5.1 The sets very poor students, poor student, ordinary students, good students and very good students are derived from students as a universe of discourse.

Membership function: Since every member of a fuzzy set has a degree of membership associated with it, a fuzzy set can be viewed as a set of ordered pairs of generic elements and their degrees of membership. Every element of the universe of discourse has exactly one $\mu$ to a fuzzy set. That is, each element of the universe of discourse is represented by exactly one ordered pair. This defines a mapping between elements of the universe discourse and the degrees of membership to the fuzzy set, and this mapping is defined to be the membership function $\mu(x)$ of the fuzzy set. In practice, the terms "membership function" and "fuzzy set" are usually interchangeable.

Support, crossover point and fuzzy singleton: The crisp set of all elements that have a non-zero membership $(\mu \neq 0)$ is called the support of the fuzzy set. In particular, the element with $\mu=0.5$ is called the crossover point. If a fuzzy set whose support is a single point with $\mu=1.0$, then this fuzzy set is a fuzzy singleton.

The operations on fuzzy sets by means of their membership functions create new fuzzy sets from given fuzzy sets. There are totally three basic fuzzy set operations: union, intersection and complement. Let fuzzy sets $A$ and $B$ belongs to a universe discourse $U$ with $\mu_{A}(x)$ and $\mu_{B}(x)$ as their membership functions, respectively.

The union of $A$ and $B$ is denoted by $A \cup B$, and the membership function of $A \cup B$ is defined by:

$$
\begin{equation*}
\mu_{A \cup B}(x)=\max \left\{\mu_{A}(x), \mu_{B}(x)\right\} . \tag{5-1}
\end{equation*}
$$

The intersection of $A$ and $B$ is denoted by $A \cap B$, and the membership function of $A \cap B$ is defined by:

$$
\begin{equation*}
\mu_{A \cap B}(x)=\min \left\{\mu_{A}(x), \mu_{B}(x)\right\} . \tag{5-2}
\end{equation*}
$$

The complement of $A$ is denoted by $\bar{A}$, and the membership function of $\bar{A}$ is defined by:

$$
\begin{equation*}
\mu_{A}(x)=1-\mu_{A}(x) . \tag{5-3}
\end{equation*}
$$

Fig. 5.2 demonstrates the three basic fuzzy set operations.

## 5-1-3. Basic fuzzy logic control algorithm

The fuzzy control algorithm is divided into three processes: fuzzification, decision making and defuzzification,. During the fuzzification process, input data is classified into suitable linguistic values or sets. According to the knowledge base of the control rules (rule base) and the linguistic variable definitions (data base), a fuzzy control action is derived in the decision making process. Then, a crisp or nonfuzzy control action is obtained by converting the inferred fuzzy control action in the defuzzification process. The block diagram of a fuzzy logic control algorithm is shown in Fig. 5.3.


Fig. 5.2 The three basic fuzzy set operations


Fig. 5.3 Block diagram of fuzzy logic control algorithm

The knowledge base is the collection of knowledge of the application domain and the control goals. The knowledge base construction plays an important role in determining the performance of a fuzzy control system. Indeed, the construction of an appropriate knowledge base is time-consuming and usually requires expert knowledge in the domain.

The data base, one of the two parts of the knowledge base, defines linguistic control rules and fuzzy data manipulation. The universe of discourse needs to be normalized. That is, the universe of discourse should have finite number of segments, and each segment is mapped into a suitable segment of the normalized universe. Consider the output voltage of our boost converter. Table 5.1 illustrates a data base that is used to normalize the universe. For computer processing, a continuous universe of discourse needs to be discretized. Because of this discretization, fuzzy logic control is less sensitive to small variations of the input variables. In Table 5.1, the universe of
discourse includes 7 fuzzy sets (primary fuzzy sets); in Table 5.2, the output voltage is discretized into 9 levels with the 7 fuzzy sets. The data base also defines the membership function of the primary fuzzy set through either numerical definition (for a continuous universe of discourse) or functional definition (for discrete universe of discourse) [69]. Triangular, trapezoidal and bell-shaped membership functions, as shown in Fig. 5.4, are three basic fuzzy membership functions [73]. The triangular membership function is the simplest one and is selected in this dissertation.

Table 5.1 Data base for normalization of fuzzy sets

| Original range <br> $(\mathrm{V})$ | Primary fuzzy sets | Normalized <br> segments | Normalized universe |
| :---: | :--- | :---: | :---: |
| $[24.0,26.0]$ | NB (negative big) | $[-1,-0.5]$ |  |
| $[26.0,27.0]$ | NM (negative middle) | $[-0.5,-0.25]$ |  |
| $[27.0,27.8]$ | NS (negative small) | $[-0.25,-0.05]$ | [-1,1]{} |
| $[27.8,28.2]$ | ZE (zero equal) | $[-0.05,0.05]$ |  |
| $[28.2,29.0]$ | PS (positive small) | $[0.05,0.25]$ |  |
| $[29.0,30.0]$ | PM (positive middle) | $[0.25,0.5]$ |  |
| $[30.0,32.0]$ | PB (positive big) | $[0.5,1]$ |  |

Table 5.2 Data base for discretization

| Level \# | Range | NB | NM | NS | ZE | PS | PM | PB |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $[0,26.0]$ | 1.0 | 0.3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 2 | $(24.0,26.0]$ | 1.0 | 0.7 | 0.3 | 0.0 | 0.0 | 0.0 | 0.0 |
| 3 | $(26.0,27.0]$ | 0.7 | 1.0 | 0.7 | 0.3 | 0.0 | 0.0 | 0.0 |
| 4 | $(27.0,27.8]$ | 0.3 | 0.7 | 1.0 | 0.7 | 0.3 | 0.0 | 0.0 |
| 5 | $(27.8,28.2]$ | 0.0 | 0.3 | 0.7 | 1.0 | 0.7 | 0.3 | 0.0 |
| 6 | $(28.2,29.0]$ | 0.0 | 0.0 | 0.3 | 0.7 | 1.0 | 0.7 | 0.3 |
| 7 | $(29.0,30.0]$ | 0.0 | 0.0 | 0.0 | 0.3 | 0.7 | 1.0 | 0.7 |
| 8 | $(30.2,32.0]$ | 0.0 | 0.0 | 0.0 | 0.0 | 0.3 | 0.7 | 1.0 |
| 9 | $(32.0,+\infty)$ | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.3 | 1.0 |



Fig. 5.4 Basic membership functions: (a) triangular membership function, (b) trapezoidal membership function, (c) bell-shaped membership function [73]

The rule base is the collection of fuzzy control rules that are expressed as fuzzy conditional statements. These fuzzy conditional statements are in the form of "if-then" rules, such as:

$$
\begin{equation*}
\text { If } x \text { is } A \text { and } y \text { is } B \text {, then } z \text { is } C . \tag{5-4}
\end{equation*}
$$

Fuzzy control rules can be derived in four modes [89]:

- Expert experience and control engineering knowledge;
- Operator's control action;
- Fuzzy model of a process;
- Learning.

The fuzzification process is a methodology to generalize a specific element from a crisp value to a fuzzy value. During this process, input variables are measured and are mapped into corresponding universes of discourse by converting the input data into suitable linguistic values which may be viewed as labels of fuzzy sets. The fuzzification process is guided by the data base.

In the decision-making process, a fuzzy control action is derived in the framework of fuzzy logic and approximate reasoning following the fuzzy control rules. Those fuzzy control rules are expressed as fuzzy implications. The definition of a fuzzy implication can be expressed as a fuzzy implication function. Researchers have proposed dozens of implication functions, such as Mamdani's mini-operation rule of fuzzy implication and Larsen's product operation rule of fuzzy implication. They are the mostly commonly used inference mechanism of the fuzzy reasoning [70, 74, 90]. If the fuzzy variables are fuzzy singletons, the two fuzzy reasoning approaches yield the same results, and can be expressed as:

$$
\begin{equation*}
z_{i}=\min \left\{\mu_{A i}\left(x_{0}\right), \ldots, \mu_{B i}\left(y_{0}\right)\right\} \cdot C_{i}, \tag{5-5}
\end{equation*}
$$

where $x_{0}$ and $y_{0}$ are fuzzy singletons, $A_{i}, B_{i}$ and $C_{i}$ are fuzzy sets in universes $X, Y$ and $Z$, and $C_{i}$ is the singleton value of $z$ using the $i^{\text {th }}$ rule. The graphical representation of this method is illustrated in Fig. 5.5. This fuzzy implication method will be used in this dissertation to design the fuzzy logic CMC controllers.


Fig. 5.5 Graphic representation of fuzzy reasoning [70]
Defuzzification maps fuzzy control action to crisp (nonfuzzy) control action. This operation is required because most practical applications use crisp control action. In the decision-making operation, many control actions are usually derived. The defuzzification process combines those fuzzy control actions through defuzzification strategies. Commonly used strategies include the maximum criterion method, the mean of maximum method, and the center of gravity method [70].

The maximum criterion method: This method finds the point where its membership function is the maximum, which can be expressed as:

$$
\begin{equation*}
z_{0}=\left\{w \mid \mu_{z}(w)=\max _{i} \mu_{z}\left(w_{i}\right)\right\}, \tag{5-6}
\end{equation*}
$$

where $z_{0}$ is the crisp control action, and $w_{i}$ is the support value at which the membership function reaches the maximum.

The mean of maximum method: This method averages all the control actions for which their membership functions are a maximum. This method can be expressed as:

$$
\begin{equation*}
z_{0}=\sum_{i=1}^{n} \frac{w_{i}}{n} \tag{5-7}
\end{equation*}
$$

where $n$ is number of local crisp control actions. This method is used in this dissertation to obtain the crisp control action to control the fuzzy logic ACMC boost converter.

The center of gravity method: This method is the most widely used. This method finds the center of gravity of all the local control actions. The final crisp control action can be found by:

$$
\begin{equation*}
z_{0}=\frac{\sum_{i}^{n} \mu_{z}\left(w_{i}\right) \cdot w_{i}}{\sum_{i}^{n} \mu_{z}\left(w_{i}\right)} . \tag{5-8}
\end{equation*}
$$

This method is used in this dissertation to obtain the crisp control action to control the fuzzy logic PCMC boost converter.

## 5-2. Microcontroller-Based Fuzzy Logic ACMC Power Converters

This section describes the design and implementation considerations for microcontroller-based fuzzy logic ACMC converters. Using the PIC16C782, a hybrid fuzzy logic ACMC controller has been designed to control the same boost converter described in Chapter 4. A one-chip solution has been achieved, and encouragingly demonstrates that the fuzzy logic current-mode control of DC-DC converters can be implemented using a microcontroller.

## 5-2-1. System overview

The block diagram for the microcontroller-based fuzzy logic ACMC boost converter is shown in Fig. 5.6. In the current loop, a current amplifier, which is
constructed using the OPA module, is inserted to obtain the average value of the inductor current. Its current reference is calculated in software using a fuzzy logic controller. Using the on-chip analog comparator $\mathrm{C}_{1}$, the amplified error from the current amplifier OPA is compared to a sawtooth reference waveform produced by the PSMC module. A pulse is generated when they are equal, and is sent to the PSMC module to generate a PWM signal that controls the switch.

In designing the hybrid fuzzy logic ACMC controller, the current loop is designed first. Three components in the current loop need to be designed or configured: OPA, $\mathrm{C}_{1}$ and PSMC module. Once the current loop is designed, the converter with the closed current loop can be treated as a "new" open-loop plant, and the voltage loop compensator is designed to control the "new" plant. The new system is actually a digital control system. Since a fuzzy logic controller does not require a mathematical model of the system, the "new" plant can be treated as a "black box". All the information inside the


Fig. 5.6 Block diagram of a fuzzy logic ACMC converter controlled by a PIC16C782 microcontroller
"box" is not required. Since the control action in a fuzzy logic controller is determined from the evaluation of a set of linguistic rules, more than one type of DC-DC converter could share the same control scheme without any modification.

Since the circuit and design method of the current loop are identical to the hybrid ACMC system described in Chapter 4, they will not be discussed in this section.

## 5-2-2. Fuzzy logic controller

The fuzzy logic controller inside the PIC16C782 is shown in Fig. 5.7. The inputs of the fuzzy logic controller are the error $e$ and the change of error $c e$ of the output voltage of the boost converter. The sampled output voltage is used to create these two inputs. The error $e$ can be expressed as


Fig. 5.7 Fuzzy logic controller inside the PIC16C782 microcontroller for ACMC boost converter

$$
\begin{equation*}
e(k)=V_{r e f}-v_{o}(k), \tag{5-9}
\end{equation*}
$$

where $V_{\text {ref }}$ is the voltage reference, and $v_{o}(k)$ is the sampled output voltage at the $k^{\text {th }}$ sampling instant. $V_{\text {ref }}$ is fixed at 128 (or 80 h ) as the nominal value, because 80 h is at the middle of an 8 -bit number (maximum 255, or FFh). The change in error ce can be expressed as:

$$
\begin{equation*}
c e(k)=e(k)-e(k-1)=v_{o}(k-1)-v_{o}(k) . \tag{5-10}
\end{equation*}
$$

As in a typical fuzzy logic control system, the fuzzy control algorithm is divided into three sections: fuzzification, decision making and defuzzification.

Fuzzification: Both $e$ and $c e$ are classified into fuzzy levels based on the resolution needed in an application. The input resolution increases with the number of fuzzy levels. In this implementation, seven fuzzy levels or sets are chosen and defined by the library of fuzzy-set values for $e$ and $c e$, shown in Table 5.3. A "membership degree" is assigned to each fuzzy set. Triangular fuzzy sets, or membership functions, as shown in Fig. 5.8, may be the most simple and efficient form for microcontroller implementation. The fuzzy representation of $e$ and ce contains two parts: the fuzzy set and the degree $\mu$ associated with the fuzzy set. It can be seen that each fuzzy representation of $e$ or $c e$

Table 5.3 Fuzzy-set values for fuzzy logic ACMC boost converter

| NE | Negative Big |
| :--- | :--- |
| NM | Negative Medium |
| NS | Negative Small |
| ZE | Zero Equal |
| PS | Positive Small |
| PM | Positive Medium |
| PB | Positive Big |



Fig. 5.8 Membership functions for $e$ and $c e$
belongs to at most two fuzzy sets. For example, when $e$ equals -0.625 , its fuzzy sets are NB and NM with degrees of $\mu_{N B}(e)=\mu_{N M}(e)=0.5$.

Decision-making: General knowledge of the converter behavior and design experiences are the basis to derive the control rules that associate the fuzzy input and fuzzy output. The rule base used in this implementation including following criteria [74]:

1) When the output of the converter is far from the set point, the change of duty cycle must be large so as to bring the output to the set point quickly;
2) When the output of the converter is approaching the set point, a small change of duty cycle is necessary;
3) When the output of the converter is near the set point and is approaching it rapidly, the duty cycle must be kept constant so as to prevent overshoot;
4) When the set point is reached and the output is still changing, the duty cycle must be changed a little bit to prevent the output from moving away;
5) When the set point is reached and the output is steady, the duty cycle remains unchanged;
6) When the output is above the set point, the sign of the change of duty cycle
must be negative, and vice versa;
Table 5.4 is the rule table derived from the above fuzzy control rules. However, the control rules are usually developed using "trial and error" and from an "intuitive" feel of the process being controlled. Since every $e$ and $c e$ belongs to at most two fuzzy sets, any combination of feedback samples of signals $(e, c e)$ can result in a maximum of four control rules. The inference result of each rule consists of two parts: change in control effort $C_{i}$ and its weighting factor $w_{i}$. Change in control effort $C_{i}$ is obtained directly from the control rule table (Table 5.4). The inferred output of each rule is written as:

$$
\begin{equation*}
z_{i}=\min \left\{\mu_{i}(e), \mu_{i}(c e)\right\} C_{i}=w_{i} C_{i}, \tag{5-11}
\end{equation*}
$$

where $z_{i}$ is the fuzzy representation output of change in control effort inferred by the $i^{\text {th }}$ control rule. Since $z_{i}$ is a linguistic result, a defuzzification operation is required next to obtain a crisp result.

Defuzzification: The most desirable way to perform the defuzzification operation is the center of gravity method, where the crisp value of change in control effort $\delta v_{c}$ can be computed by a logical sum of the inference results of the four control rules:

Table 5.4 Control rule table for fuzzy logic ACMC boost converter

| Error |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | NB | NM | NS | ZE | PS | PM | PB |
|  | NB | NB | NB | NB | NB | NM | NS | ZE |
|  | NM | NB | NB | NB | NM | NS | ZE | PS |
|  | NS | NB | NB | NM | NS | ZE | PS | PM |
|  | ZE | ZB | NM | NS | ZE | PS | PM | PB |
|  | PS | NM | NS | ZE | PS | PM | PB | PB |
|  | PM | NS | ZE | PS | PM | PB | PB | PB |
|  | PB | ZE | PS | PM | PB | PB | PB | PB |

$$
\begin{equation*}
\delta v_{c}=\frac{\sum_{i=1}^{4} w_{i} m_{i}}{\sum_{i=1}^{4} w_{i}} \tag{5-12}
\end{equation*}
$$

where $m_{i}$ is the centroid of $C_{i}$. Notice that (5-12) involves multiplication and division of variables, not just the scaling of signals by constant gains. Many microcontrollers, just as the PIC16C782, do not have direct multiplication and division instructions, so they do not have the capacity to compute the control effort fast enough to control the converter satisfactorily. In order to solve this problem, Gupta et al. [87] developed a modified centroid method, which can be expressed as:

$$
\begin{equation*}
\delta v_{c}=\frac{m_{a}+m_{b}}{2} \tag{5-13}
\end{equation*}
$$

where $m_{a}$ and $m_{b}$ are the centroids corresponding to the two largest degrees of the fuzzy sets belonging to the fuzzy representation of the change in control effort. The modified centroid method requires only one addition and a right-shift. However, this method is valid only if the centroids of adjacent fuzzy sets are close to each other, and does not give comparable results if the centroids are far apart. Also, this method needs to search out the two largest degrees, which slows down the computation significantly, since many microcontrollers, including the PIC16C782, do not have direct instructions for comparison.

The mean of maximum method is another defuzzification strategy. This strategy yields a control action that represents the mean value of all control rules whose membership functions reach the maximum. In this implementation, the control action can be expressed as:

$$
\begin{equation*}
\delta v_{c}=\frac{1}{4} \sum_{i=1}^{4} m_{i}, \tag{5-14}
\end{equation*}
$$

where $m_{i}$ is the centroid corresponding to each of the four largest degrees of the fuzzy sets belonging to the fuzzy representation of the change in control effort.

Equation (5-14) shows that $\delta v_{c}$ is simply the average of the centroids of all the four fuzzy representations of the change in control effort. When using this method, the action of the fuzzy logic controller is similar to that of a multilevel relay system. This method is actually a special case of the center of gravity method when $w_{i}=1$ for all $i$. The mean of maximum method yields a better transient performance, while the center of gravity method yields a better steady-state performance [70].

The output of the fuzzy control algorithm is the change in control effort $\delta v_{c}(k)$. The actual control effort $v_{c}(k)$ is determined by adding the previous control effort $v_{c}(k-1)$ to the calculated change in control effort $\delta v_{c}(k)$, which can expressed as

$$
\begin{equation*}
v_{c}(k)=v_{c}(k-1)+\delta v_{c}(k) . \tag{5-15}
\end{equation*}
$$

In classical control theory, (5-15) represents an integrating process which increases the system type and reduces the steady-state error. The calculated control effort $v_{c}(k)$ is then sent to the current compensator as the current reference.

## 5-2-3. Implementation challenges and solutions

In Chapter 2-4, the solutions that solve the challenges facing to hybrid CMC power converter have been presented. Most of the solutions can also be applied to hybrid fuzzy logic ACMC system. In this implementation, some of challenges are solved using different approaches. In addition, there are some new challenges that need to be solved.

The PIC16C782 does not allow negative numbers in the system. However, $e$ and $c e$ can have negative physical values. Therefore, their digital representations $\hat{e}$ and $c \hat{e}$ are biased by 128 :

$$
e, c e\left\{\begin{array} { l } 
{ < 0 }  \tag{5-16}\\
{ = 0 , } \\
{ > 0 }
\end{array} \text { then } \left\{\begin{array}{l}
0 \leq \hat{e}, c \hat{e}<128 \\
\hat{e}, c \hat{e}=128 \\
128<\hat{e}, c \hat{e} \leq 255
\end{array}\right.\right.
$$

where the variables $\hat{e}$ and $c \hat{e}$ are the error and change in error with the 128 offset, respectively. When an overflow or an underflow occurs, 255 or 0 is set for a maximum or minimum value. As the result, the universe of discourse for the membership functions for $\hat{e}$ and ce extends from 0 to 255 , and is spaced equally. The resultant $\delta v_{c}$ is also biased by 128 , and needs to be adjusted back before it is added to $v_{c}$.

In order to achieve simple and fast computation, the mean of maximum method is employed in the defuzzification process. This method requires only three additions and three right-shifts without any other calculations, and hence reduces the computation complexity dramatically. By using the carry as an extra bit during addition and followed by right-shift through carry, the calculation procedure becomes 9 bits instead of 8 . Therefore, the calculation procedure is guaranteed to not overflow, which further simplifies the calculation procedure without sacrificing any accuracy.

When the mean of maximum method is used, only the centroids of the fuzzy sets are required in the calculation. Therefore, the degrees associated with the fuzzy sets are not calculated or stored. This further simplifies the calculation procedure and saves memory space.

The control rules (Table 5.4) are stored as a look-up table that contains the
centroids of the output fuzzy sets. The output fuzzy sets for change in control effort $\delta v_{c}$ follow the universe of discourse as shown in Fig. 5.9. Note $\delta v_{c}$ in Fig. 5.9 has an offset of 128. The range for the universe of discourse is limited because only seven output fuzzy sets are chosen. This limits the maximum $\delta v_{c}$, and hence limits the maximum change in duty cycle $\delta d$. Extensive experimental tests show that the overshoot in the transient response can be very large if $\delta d$ is too large, which may result in instability.

As stated previously, the mean of maximum method has a relatively poor steadystate performance because of its relay-like characteristic, which results in a steady-state error and a triangular ripple in the output voltage. Therefore, the range for the universe of discourse should be small enough such that the change in control effort is small enough to eliminate the steady-state ripple and error. That is, the centroids of adjacent output fuzzy sets are close to each other. Since the change in control effort $\delta v_{c}$ is very small at steady state, it is especially important to have closer fuzzy sets when $\delta v_{c}$ is small, which is also shown in Fig. 5.9.

On the other hand, a smaller range of change in control effort results in smaller change in control effort, which slows down the transient response. Therefore, there is a tradeoff between transient and steady-state performances. This tradeoff can be


Fig. 5.9 Membership function (1) for $\delta v_{c}$
eliminated by switching between two or more sets of membership functions with different ranges for the universe of discourse. In this implementation, one more membership function for $\delta v_{c}$ is added, as shown in Fig. 5.10. The membership function in Fig. 5.10 has a smaller range for the universe of discourse, and the output fuzzy sets are closer to each other than the membership function in Fig. 5.9. In this implementation, when the error is smaller than 0.29 V , the membership function in Fig. 5.10 is selected; for an error is greater than 0.29 V , the membership function in Fig. 5.9 is employed.

Initial tests with a 0.56 A load showed steady-state oscillations. Hence, a gain was applied to the two inputs (the error $\hat{e}$ and change in error $c \hat{e}$ ). Extensive tests showed that a gain of $1 / 4$ for $\hat{e}$ and a gain of 4 for $c \hat{e}$ eliminated steady-state oscillations and improved the transient response. Indeed, this approach is equivalent to scaling the control rule table such that it is close to an optimal numerical range.

In this implementation, switching noise in the output voltage is avoided by sending the PWM signal back to another I/O pin to trigger an interrupt that starts an A/D conversion. As a result, the sampling moment can be controlled, and the output voltage can always be captured after the switching noise has subsided. In order to ensure the proper sampling moment, an interrupt from any other source is not allowed. In this


Fig. 5.10 Membership function (2) for $\delta v_{c}$
implementation, the interrupt service routine (ISR) also contains all logical and mathematical calculations, and the main routine simply waits for the next interrupt after all the calculations have been finished. Since the A/D conversion time is much faster than total calculation time, the controller sampling frequency is directly determined by the speed of the calculations.

## 5-2-4. Experimental results

The system diagram for the microcontroller-based fuzzy logic ACMC boost converter is shown in Fig. 5.11. The power stage is the same boost converter described in Chapter 4. The nominal input and output voltages of the boost converter were 12 V and 28 V , respectively, and the nominal load was $50 \Omega(0.56 \mathrm{~A})$. AC coupling was utilized on the oscilloscope channel in measuring the output voltage. The boost converter


Fig. 5.11 A fuzzy logic ACMC boost converter controlled by a PIC16C782
operated in CCM when the switching frequency was 156.25 kHz , or $6.4 \mu \mathrm{~s}$ per switching cycle. The PIC16C782 operated at 20 MHz . All waveforms were recorded using a Tektronix TDS 744A oscilloscope.

Fig. 5.12 shows the calculation timing status. The top line is the gate signal. The bottom line is obtained by toggling an output pin when the program enters or exits the ISR, so it represents the time required to finish all arithmetic and logic calculations. Fig. 5.12 shows that all calculations can be completed in around $31 \mu \mathrm{~s}$, so the output voltage can be sampled every 5 switching cycles, or $32 \mu \mathrm{~s}$. This is much longer than the ADC conversion cycle, which is only $15.2 \mu \mathrm{~s}$ when the clock frequency is 20 MHz . Fig. 5.13 is the same as Fig. 5.12, except it has an expanded time axis. Fig. 5.13 clearly shows that


Fig. 5.12 Gate and ISR timing diagram 1. Top: gate signal, 10 V/DIV; Bottom: timing signal on an output pin, 2 V/DIV; Time: $5 \mu \mathrm{~s} /$ DIV


Fig. 5.13 Gate and ISR timing diagram 2. Top: gate signal, $10 \mathrm{~V} / \mathrm{DIV}$; Bottom: timing signal on an output pin, 2 V/DIV; Time: $1 \mu \mathrm{~s} /$ DIV
$\mathrm{A} / \mathrm{D}$ conversion is started $1.2 \mu \mathrm{~s}$ after the switch is turned on, when the switching noise has subsided. The starting point of each $A / D$ conversion can be controlled precisely at a $0.2 \mu \mathrm{~s}$ (one instruction cycle) precision.

When a large disturbance occurs, such as a load change from 0.187 A to 0.75 A , as shown in Fig. 5.14, the response time of the system was around 1 ms to reach steady state with $1.2 \mathrm{~V}(4.3 \%$ of 28 V$)$ of maximum transient error. At this time, the transient error was reduced to less than $0.3 \mathrm{~V}(1 \%$ of 28 V$)$ in $300 \mu \mathrm{~s}$. When the load change was from 0.75 A to 0.187 A , as shown in Fig. 5.15 , the system required 1.5 ms to reach steady state with $1.3 \mathrm{~V}(4.6 \%$ of 28 V$)$ of maximum transient error. At this time, the transient error was reduced to 0.3 V in less than $600 \mu \mathrm{~s}$. In both cases, the steady-state error of the system was approximately zero. The top lines in Fig. 5.14 and Fig. 5.15 are the full range


Fig. 5.14 Transient response of the fuzzy logic ACMC boost converter when the load change was from 0.187 A to 0.75 A . Top: output voltage, $10 \mathrm{~V} / \mathrm{DIV}$; Bottom: output voltage, $500 \mathrm{mV} / \mathrm{DIV}$; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$


Fig. 5.15 Transient response of the fuzzy logic ACMC boost converter when the load change was from 0.75 A to 0.187 A. Top: output voltage, $10 \mathrm{~V} / \mathrm{DIV}$; Bottom: output voltage, $500 \mathrm{mV} / \mathrm{DIV}$; Time: $500 \mu \mathrm{~s} / \mathrm{DIV}$
of the output voltage, and the bottom lines are the AC coupled output voltage.
The step response for the voltage reference, illustrated in Fig. 5.16, was obtained by changing $V_{\text {ref }}$ from 00 h to 80 h (nominal value). The step response shows that the system reaches steady state in less than 2 ms with an overshoot of about 1.5 V , which is about $5.4 \%$ of 28 V . This proves that there is no need to measure the full-range of the output voltage for start up if the voltage loop compensator is designed appropriately.

## 5-3. Microcontroller-Based Fuzzy Logic PCMC Power Converters

Described in this section are the design and implementation considerations for a microcontroller-based fuzzy logic PCMC converter. A hybrid fuzzy logic PCMC boost converter has been implemented using a PIC16C782 microcontroller. For generality, the


Fig. 5.16 Step response of the fuzzy logic ACMC boost converter. Output voltage: 5 V/DIV; Time: 500 $\mu \mathrm{s} / \mathrm{DIV}$
boost converter operates in the continuous conduction mode (CCM). By using the onboard peripherals of the microcontroller and rule-based look-up tables, a one-chip solution has been achieved. Experimental results indicate successful operation of the fuzzy logic implementation for a PCMC dc-dc converter.

## 5-3-1. System overview

The block diagram for the microcontroller-based fuzzy logic PCMC boost converter is shown in Fig. 5.17. In the current loop, the peak switch current (inductor current) is sensed by a low-value resistor $R_{i}$. The on-board comparator $\mathrm{C}_{1}$ compares the peak switch current (after slope compensation) with a reference current, which is calculated in software using fuzzy logic. A pulse is generated when they are equal, and is sent to the PSMC module to generate a PWM signal that controls the switch. The PSMC module is also used to generate a positive-going ramp function to perform slope


Fig. 5.17 Block diagram of a fuzzy logic PCMC converter controlled by a PIC16C782 microcontroller
compensation by adding it to the sensed current. Design procedures are the same as hybrid fuzzy logic ACMC power converter described in previous section.

Since the current loop design is identical to the hybrid PCMC power converter introduced in Chapter 3, it will not be discussed in this section.

## 5-3-2. Fuzzy logic controller

Once the current loop is designed, the converter with the closed current loop can be treated as a "new" open loop plant, and the voltage loop compensator is designed to control the "new" plant. Since a fuzzy logic controller does not need a converter model, the "new" plant can be treated as a "black box". Only knowledge of the converter behavior, in the form of linguistic rules, is needed. The fuzzy control algorithm is divided into three sections: fuzzification, decision making and defuzzification. The output of the fuzzy control algorithm is the change in control effort $\delta v_{c}(k)$.

Fuzzification: Just as the hybrid fuzzy logic ACMC system, the inputs of the fuzzy controller are the error $e$, the change of error $c e$. Since $e$ and $c e$ can have negative physical values, their digital representations are biased by 128.

Both $e$ and $c e$ are classified into fuzzy levels based on the resolution needed in an application. The input resolution increases with the number of fuzzy levels. In this implementation, nine fuzzy levels or sets are chosen and defined by the library of fuzzyset values for $e$ and $c e$, as shown in Table 5.5. A "membership degree" can be assigned to each fuzzy set. Triangular fuzzy-sets, or membership functions, as shown in Fig. 5.18, were selected here, since it is the simplest and most efficient form for microcontroller implementation. The fuzzy representation of $e$ and $c e$ contains two parts: the fuzzy set and the degree $\mu$ associated with the fuzzy set. It can be seen that each fuzzy

Table 5.5 Fuzzy-set values for fuzzy logic PCMC boost converter

| NB | Negative Big |
| :--- | :--- |
| NM | Negative Medium |
| NS | Negative Small |
| NE | Negative Equal |
| ZE | Zero Equal |
| PE | Positive Equal |
| PS | Positive Small |
| PM | Positive Medium |
| PB | Positive Big |



Fig. 5.18 Membership functions for $e$ and $c e$
representation of $e$ or $c e$ belongs to at most two fuzzy sets. For example, when the digital representation of e equals 24 , its fuzzy sets are NB and NM with degrees of $\mu_{N B}(e)=192$ and $\mu_{N M}(e)=64$.

Decision-making: General knowledge of the converter behavior is the basis on which to derive control rules that associate the fuzzy input and fuzzy output. Table 5.6 contains the control rules to determine the fuzzy set output. Since every $e$ and $c e$ belongs to at most two fuzzy sets, any combination of feedback samples of signals ( $e, c e$ ) can result in a maximum of four control rules. However, the control rules are usually
developed using "trial and error" and from an "intuitive" feel of the process being controlled. Table 5.6 is obtained by understanding the behavior of the converter. The inference result of each rule consists of two parts: the degree of change in control effort $C_{i}$, and its weighting factor $w_{i} . C_{i}$ is obtained directly from Table 5.6 , and $w_{i}$ can be obtained by means of Mamdani's min fuzzy implication. The inferred output of each rule can be computed using (5-11).

Defuzzification: The output fuzzy sets for change in control effort $\delta v_{c}$ follow the universe of discourse as shown in Fig. 5.19. Note $\delta v_{c}$ in Fig. 5.19 also has an offset of 128.

As described in previous section, the mean of maximum method yields a control action that represents the mean value of all control rules whose membership functions reach the maximum. When using this method, the action of the fuzzy logic controller is similar to that of a multilevel relay system. This method can be implemented by using only several additions and right-shifts without any other calculations, and hence reduces

Table 5.6 Control rule table for fuzzy logic PCMC boost converter



Fig. 5.19 Membership functions for $\delta v_{c}$
the computational complexity dramatically. Therefore, this method is an effective defuzzification strategy especially suitable for microcontrollers with limited computing power. However, direct application of this method has a relatively poor steady-state performance because of its relay-like characteristic, which results in a steady-state error and a triangular ripple in the output voltage. In the previous section, this problem was solved by using two or more membership functions for $\delta v_{c}$ with different ranges for the universe of discourse. Based on the output voltage error, one of the membership functions is selected each time. When the error is small, the membership function with a smaller range for the universe of discourse is employed. However, this method imposes a burden of determining the extra membership functions.

Probably the most desirable way to perform the defuzzification operation is the center of gravity method, where $\delta v_{c}$ can be computed by a logical sum of the inference results of the four control rules, as in (5-12). However, the PIC16C782 does not have direct multiplication and division instructions, so they do not have the capacity to directly compute the control effort fast enough to control an on-line converter. In this implementation, the center of gravity method is employed in the defuzzification process.

In order to avoid excessive on-line calculations, the control efforts are calculated off-line, and are stored in a lookup table. Indeed, this lookup table combines all the three sections of the fuzzy logic algorithm. That is, once error $e$ and change in error $c e$ are computed, they are converted to table indices, and the proper $\delta v_{c}$ is selected from the table directly. However, this lookup table can consume 64 kB memory for an 8 -bit resolution. Many microcontrollers do not contains large enough on-board memory to store the table. For instance, the program memory inside a PIC16C782 is only 2 kB , which is also used to store the program. External memory may solve this problem, but it is not desirable because it will increase the cost and complexity of the system. In order to overcome the challenge of very limited memory, several techniques were employed.

1. The program was designed as concise as possible to save program memory. More subroutines were used to perform common tasks at the cost of slightly slowing down the calculation speed.
2. Use multiple lookup tables with different resolution. When $e$ and $c e$ are large, the resulting control effort $\delta v_{c}$ is also large, so using a lower resolution may result in a satisfactory dynamic response. In this implementation, a high resolution (7-bit) table was chosen when $e$ and $c e$ were small enough, i.e., half of the full range of $e$, and one third of the full range of $c e$. When either $e$ or $c e$ was large, a low-resolution (5-bit) table was selected which covers the full range of $e$ and $c e$. The low-resolution lookup table is illustrated in Table 5.6. The high resolution table is not shown here because of its size.
3. Notice the left-upper half of Table 5.6 is identical to right-lower half of the table with reversed sign in its numerical representation, and the resulting lookup table (Table 5.7) has the same characteristic. Therefore, only half of Table 5.7 was stored.

Table 5.7 Fuzzy logic lookup table (low resolution)
Error

|  | 0 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 | 88 | 96 | 104 | 112 | 120 | 128 | 136 | 144 | 152 | 160 | 168 | 176 | 184 | 192 | 200 | 208 | 216 | 224 | 232 | 240 | 248 | 255 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 14 | 27 | 41 | 55 | 64 | 73 | 82 | 91 | 96 | 101 | 105 | 110 | 114 | 119 | 123 | 128 |
| 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 9 | 9 | 9 | 14 | 34 | 43 | 52 | 64 | 76 | 82 | 88 | 96 | 104 | 107 | 110 | 114 | 122 | 125 | 128 | 133 |
| 16 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 9 | 14 | 18 | 27 | 43 | 50 | 58 | 73 | 82 | 87 | 91 | 101 | 107 | 110 | 113 | 119 | 125 | 128 | 131 | 137 |
| 24 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 9 | 18 | 27 | 41 | 52 | 58 | 64 | 82 | 88 | 91 | 94 | 105 | 110 | 113 | 116 | 123 | 128 | 131 | 134 | 142 |
| 32 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 14 | 27 | 41 | 55 | 64 | 73 | 82 | 91 | 96 | 101 | 105 | 110 | 114 | 119 | 123 | 128 | 133 | 137 | 142 | 146 |
| 40 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 9 | 9 | 9 | 14 | 34 | 43 | 52 | 64 | 76 | 82 | 88 | 96 | 104 | 107 | 110 | 114 | 122 | 125 | 128 | 133 | 140 | 143 | 146 | 151 |
| 48 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 9 | 14 | 18 | 27 | 43 | 50 | 58 | 73 | 82 | 87 | 91 | 101 | 107 | 110 | 113 | 119 | 125 | 128 | 131 | 137 | 143 | 146 | 149 | 155 |
| 56 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 9 | 18 | 27 | 41 | 52 | 58 | 64 | 82 | 88 | 91 | 94 | 105 | 110 | 113 | 116 | 123 | 128 | 131 | 134 | 142 | 146 | 149 | 152 | 160 |
| 64 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 14 | 27 | 41 | 55 | 64 | 73 | 82 | 91 | 96 | 101 | 105 | 110 | 114 | 119 | 123 | 128 | 133 | 137 | 142 | 146 | 151 | 155 | 160 | 165 |
| 72 | 0 | 0 | 0 | 0 | 0 | 9 | 9 | 9 | 14 | 34 | 43 | 52 | 64 | 76 | 82 | 88 | 96 | 104 | 107 | 110 | 114 | 122 | 125 | 128 | 133 | 140 | 143 | 146 | 151 | 162 | 165 | 168 | 174 |
| 80 | 0 | 0 | 0 | 0 | 0 | 9 | 14 | 18 | 27 | 43 | 50 | 58 | 73 | 82 | 87 | 91 | 101 | 107 | 110 | 113 | 119 | 125 | 128 | 131 | 137 | 143 | 146 | 149 | 155 | 165 | 169 | 174 | 183 |
| 88 | 0 | 0 | 0 | 0 | 0 | 9 | 18 | 27 | 41 | 52 | 58 | 64 | 82 | 88 | 91 | 94 | 105 | 110 | 113 | 116 | 123 | 128 | 131 | 134 | 142 | 146 | 149 | 152 | 160 | 168 | 174 | 180 | 192 |
| 96 | 0 | 0 | 0 | 0 | 0 | 14 | 27 | 41 | 55 | 64 | 73 | 82 | 91 | 96 | 101 | 105 | 110 | 114 | 119 | 123 | 128 | 133 | 137 | 142 | 146 | 151 | 155 | 160 | 165 | 174 | 183 | 192 | 201 |
| 104 | 0 | 9 | 9 | 9 | 14 | 34 | 43 | 52 | 64 | 76 | 82 | 88 | 96 | 104 | 107 | 110 | 114 | 122 | 125 | 128 | 133 | 140 | 143 | 146 | 151 | 162 | 165 | 168 | 174 | 192 | 198 | 204 | 215 |
| 112 | 0 | 9 | 14 | 18 | 27 | 43 | 50 | 58 | 73 | 82 | 87 | 91 | 101 | 107 | 110 | 113 | 119 | 125 | 128 | 131 | 137 | 143 | 146 | 149 | 155 | 165 | 169 | 174 | 183 | 198 | 206 | 213 | 229 |
| 120 | 0 | 9 | 18 | 27 | 41 | 52 | 58 | 64 | 82 | 88 | 91 | 94 | 105 | 110 | 113 | 116 | 123 | 128 | 131 | 134 | 142 | 146 | 149 | 152 | 160 | 168 | 174 | 180 | 192 | 204 | 213 | 222 | 242 |
| 128 | 0 | 14 | 27 | 41 | 55 | 64 | 73 | 82 | 91 | 96 | 101 | 105 | 110 | 114 | 119 | 123 | 128 | 133 | 137 | 142 | 146 | 151 | 155 | 160 | 165 | 174 | 183 | 192 | 201 | 215 | 229 | 242 | 255 |
| 136 | 14 | 34 | 43 | 52 | 64 | 76 | 82 | 88 | 96 | 104 | 107 | 110 | 114 | 122 | 125 | 128 | 133 | 140 | 143 | 146 | 151 | 162 | 165 | 168 | 174 | 192 | 198 | 204 | 215 | 229 | 238 | 247 | 255 |
| 144 | 27 | 43 | 50 | 58 | 73 | 82 | 87 | 91 | 101 | 107 | 110 | 113 | 119 | 12 | 128 | 131 | 137 | 143 | 146 | 149 | 155 | 165 | 169 | 174 | 183 | 198 | 206 | 213 | 229 | 238 | 242 | 247 | 255 |
| 152 | 41 | 52 | 58 | 64 | 82 | 88 | 91 | 94 | 10 | 110 | 11 | 11 | 12 | 12 | 13 | 13 | 142 | 146 | 149 | 152 | 160 | 168 | 174 | 180 | 192 | 204 | 213 | 222 | 242 | 247 | 247 | 247 | 255 |
| 160 | 55 | 64 | 73 | 82 | 91 | 96 | 101 | 105 | 110 | 11 | 11 | 12 | 12 | 13 | 137 | 142 | 146 | 151 | 155 | 160 | 165 | 174 | 183 | 192 | 201 | 215 | 229 | 242 | 255 | 255 | 255 | 255 | 255 |
| 168 | 64 | 76 | 82 | 88 | 96 | 104 | 107 | 110 | 11 | 122 | 125 | 128 | 13 | 140 | 143 | 146 | 151 | 162 | 165 | 168 | 174 | 192 | 198 | 204 | 215 | 229 | 238 | 247 | 255 | 255 | 255 | 255 | 255 |
| 176 | 73 | 82 | 87 | 91 | 101 | 107 | 110 | 113 | 119 | 125 | 12 | 13 | 137 | 143 | 146 | 149 | 155 | 165 | 169 | 174 | 183 | 198 | 206 | 213 | 229 | 238 | 242 | 247 | 255 | 255 | 255 | 255 | 255 |
| 184 | 82 | 88 | 91 | 94 | 105 | 110 | 113 | 116 | 123 | 128 | 131 | 13 | 142 | 146 | 149 | 152 | 160 | 168 | 174 | 180 | 192 | 204 | 213 | 222 | 242 | 247 | 247 | 247 | 255 | 255 | 255 | 255 | 255 |
| 192 | 91 | 96 | 101 | 105 | 110 | 114 | 119 | 123 | 128 | 133 | 137 | 142 | 146 | 151 | 155 | 160 | 165 | 174 | 183 | 192 | 201 | 215 | 229 | 242 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 200 | 96 | 104 | 107 | 110 | 114 | 122 | 125 | 128 | 133 | 140 | 143 | 146 | 15 | 16 | 16 | 16 | 17 | 192 | 198 | 204 | 215 | 229 | 238 | 247 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 208 | 101 | 107 | 110 | 113 | 119 | 125 | 128 | 131 | 137 | 143 | 146 | 149 | 155 | 165 | 169 | 174 | 183 | 198 | 206 | 213 | 229 | 238 | 242 | 247 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 216 | 105 | 110 | 113 | 116 | 123 | 128 | 131 | 134 | 142 | 146 | 149 | 152 | 160 | 168 | 174 | 180 | 192 | 204 | 213 | 222 | 242 | 247 | 247 | 247 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 224 | 110 | 114 | 119 | 123 | 128 | 133 | 137 | 142 | 146 | 151 | 155 | 160 | 165 | 174 | 183 | 192 | 201 | 215 | 229 | 242 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 232 | 114 | 122 | 125 | 128 | 133 | 140 | 143 | 146 | 151 | 162 | 165 | 168 | 174 | 192 | 198 | 204 | 215 | 229 | 238 | 247 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 240 | 119 | 125 | 128 | 131 | 137 | 143 | 146 | 149 | 155 | 165 | 169 | 174 | 183 | 198 | 206 | 213 | 229 | 238 | 242 | 247 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 248 | 123 | 128 | 131 | 134 | 142 | 146 | 149 | 152 | 160 | 168 | 174 | 180 | 192 | 204 | 213 | 222 | 242 | 247 | 247 | 247 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |
| 255 | 128 | 133 | 137 | 142 | 146 | 151 | 155 | 160 | 165 | 174 | 183 | 192 | 201 | 215 | 229 | 242 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 | 255 |

Since the PIC16C782 does not have a sign bit, the signs of $e$ and $c e$ were stored in another register. After the data was read from the lookup table, $\delta v_{c}$ was obtained based on the signs of $e$ and $c e$.
4. The PIC16C782 program memory is divided into 8 pages, and each page contains 256 bytes. The indices of the lookup tables must contain the page number and the entry inside the page. Referring to Table 5.7, the lookup table has an odd number of total entries, which is also true for high resolution table. In order to avoid overcomplexity in constructing indices or sacrificing resolution, one more lookup table was added. This small-size table ( 32 bytes) was checked only when $e$ equals zero.

By using the techniques above, the low resolution table used 512 bytes memory, and the high resolution table consumed 1 kB memory. The space left for the program is less than 480 bytes.

## 5-3-3. Integrating process

The control effort $v_{c}(k)$ was determined by adding the calculated change in control effort $\delta v_{c}(k)$ to the previous control effort $v_{c}(k-1)$, which can be expressed as (5-14), which is an integrating process.

Another gain $k_{f}$ can also be applied to the fuzzy logic output $\delta v_{c}$ to improve the performance. At steady state, a rapid change of $\delta v_{c}$ was not desired, so a smaller $k_{f}$ was preferred. During a transient period, it was desired that $\delta v_{c}$ be large to ensure fast response, so $k_{f}$ was larger. In this implementation, a gain of 1 was applied to $\delta v_{c}$ when $e$ is close to 0 , and a gain of 2 was employed in other cases.

Initial tests with a 0.56 A load showed steady-state oscillations or slow response. In order to enhance steady state and transient response, gains were applied to the error $e$
and change in error $c e$. Extensive tests showed that a gain of $1 / 4$ for the error and a gain of 4 for the change in error eliminated steady-state oscillations and improved the transient response. However, due to the 8 -bit resolution, when these gains were less than 1 , they introduced steady-state error that cannot be eliminated by the integrating process in (514). In order to eliminate the steady-state error introduced by scaling the fuzzy logic inputs (the error and change in error), the error was scaled and added to $\delta v_{c}$, so the control effort $v_{c}(k)$ can expressed as:

$$
\begin{equation*}
v_{c}(k)=v_{c}(k-1)+k_{f} \delta v_{c}(k)+k_{i} e(k), \tag{5-17}
\end{equation*}
$$

where $k_{f}$ was the gain for the fuzzy logic output, and $k_{i}$ was the gain for the error. The term $k_{i} e(k)$ also introduced a integrating process, and can smooth the transient response. It also eliminated the steady-state error introduced by 7-bit resolution of the lookup table. Since its main role was to eliminate the steady-state error, $k_{i}$ was small compared to $k_{f}$. In this implementation, $k_{i}$ equaled $1 / 4$. The fuzzy logic controller inside the microcontroller then can be illustrated as Fig. 5.20.

## 5-3-4. Experimental results

The system diagram for the microcontroller-based fuzzy logic PCMC boost converter is shown in Fig. 5.21. The power stage is the same boost converter used in hybrid fuzzy logic system described earlier. The boost converter operated in the continuous conduction mode when the switching frequency was 156.25 kHz . The PIC16C782 operated at 20 MHz . AC coupling was utilized on the oscilloscope channel measuring the output voltage.


Fig. 5.20 Fuzzy logic controller inside the PIC16C782 microcontroller for PCMC boost converter


Fig. 5.21 A fuzzy logic PCMC boost converter controlled by a PIC16C782

Fig. 5.22 shows the calculation timing status. The top line is the gate signal. The bottom line was obtained by toggling an output pin when the program entered or exited the ISR, so it represented the time required to finish all arithmetic and logic calculations. Fig. 5.22 shows that all calculations can be completed in around $36 \mu \mathrm{~s}$, so the output voltage can be sampled every 6 switching cycles, or $37.5 \mu \mathrm{~s}$. This was much longer than the ADC conversion cycle, which was $15.2 \mu \mathrm{~s}$ when the clock frequency is 20 MHz . The starting point of each $\mathrm{A} / \mathrm{D}$ conversion can be controlled precisely at a $0.2 \mu \mathrm{~s}$ (one instruction cycle) precision. When the time-axis of Fig. 5.22 is extended, as shown in Fig. 5.23, it can be seen clearly that each A/D conversion cycle was started about $1.2 \mu \mathrm{~s}$ after the switch was turned on, where the switching noise had subsided.


Fig. 5.22 Gate and ISR timing diagram 1. Top: gate signal, $10 \mathrm{~V} / \mathrm{DIV}$; Bottom: timing signal on an output pin, $2 \mathrm{~V} / \mathrm{DIV}$; Time: $10 \mu \mathrm{~s} / \mathrm{DIV}$


Fig. 5.23 Gate and ISR timing diagram 2. Top: gate signal, $10 \mathrm{~V} / \mathrm{DIV}$; Bottom: timing signal on an output pin, 2 V/DIV; Time: $1 \mu \mathrm{~s} /$ DIV

When a large disturbance occurred, such as a load change from 0.187 A to 0.75 A , as shown in Fig. 5.24, the transient error reduced to less than $0.28 \mathrm{~V}(1 \%$ of 28 V$)$ in 700 $\mu \mathrm{s}$. The total response time of the system was less than 1.2 ms to reach steady state with 1.5 V of maximum transient error $(5.4 \%$ of 28 V$)$. When a load change was from 0.75 A to 0.187 A , as shown in Fig. 5.25 , the transient error reduced to less than $0.28 \mathrm{~V}(1 \%$ of 28 V ) in $700 \mu \mathrm{~s}$. The total response time of the system was less than 1.2 ms to reach steady state with 1.5 V of maximum transient error $(5.4 \%$ of 28 V$)$. In both cases, the steady-state error was approximately zero.

Fig. 5.26 shows the response when the voltage reference changes from 00 h to 7 Fh . The system can reached steady state in about 1.6 ms with a maximum overshoot of about 1 V , which is about $3.57 \%$ of 28 V . In Fig. 5.27, the voltage reference changes from 7Fh


Fig. 5.24 Transient response of the fuzzy logic PCMC boost when the load change was from 0.75 A to 0.187 A. Output voltage: $500 \mathrm{mV} / \mathrm{div}$; Time: $250 \mu \mathrm{~s} / \mathrm{div}$


Fig. 5.25 Transient response of the fuzzy logic PCMC boost when the load change was from 0.187 A to 0.75 A. Output voltage: $500 \mathrm{mV} / \mathrm{div}$; Time: $250 \mu \mathrm{~s} / \mathrm{div}$


Fig. 5.26 Step response of the fuzzy logic PCMC boost converter for voltage reference changing from 00 h to 7 Fh when load was 0.56 A . Output voltage: $5 \mathrm{~V} / \mathrm{div}$; Time: $500 \mu \mathrm{~s} / \mathrm{div}$


Fig. 5.27 Step response of the fuzzy logic PCMC boost converter for voltage reference changing from 7 Fh to 00 h when load was 0.56 A . Output voltage: $5 \mathrm{~V} / \mathrm{div}$; Time: $500 \mu \mathrm{~s} / \mathrm{div}$
to 00 h . The output voltage decreased from 28 V to 12 V in 2.4 ms . At this time, no overshoot occurred.

## 5-4. Conclusion

This chapter presented practical design issues for hybrid fuzzy logic ACMC and PCMC dc-dc converters. The PIC16C782 microcontroller was used to implement the controllers. The voltage loops of the two systems were implemented digitally. The compensator in the voltage loops were fuzzy logic controllers.

Experimental results were presented which show that a fuzzy logic controller can regulate the output voltage of a CMC boost converter with a satisfactory response without steady-state error and oscillation in case of a large load change.

These two designs prove that some advanced control methods, such as fuzzy logic control, can be realized on a microcontroller to control CMC converters without using more expensive DSPs or other complicated hardware, provided some appropriate adjustments in hardware and software are made.

## Chapter 6

## Conclusions and Future Directions

Presented in this dissertation is the implementation of microcontroller-based digital current-mode control switch-mode power converters using a hybrid control method.

A microcontroller usually has a significantly lower cost and is simpler than a DSP system or other kinds of digital hardware. Therefore, using microcontrollers, the development of digital control systems can be faster and less expensive than many other types of digital hardware. Meanwhile, a microcontroller also has some hardware and software limitations. The purpose of this dissertation is to examine the practical solutions to control CMC power converter using microcontrollers.

A hybrid control concept was introduced such that a one-chip solution can be achieved to control a CMC power converter using a microcontroller. By using on-board analog peripherals, the current loop can be designed using analog components. A pure digital controller can be implemented in the voltage loop. Many digital control methods, including fuzzy logic control, can be applied in the voltage loop design without changing the hardware of the control system.

Implementation issues for microcontroller-based digital controllers for CMC converters were discussed. These issues include system modeling, required functionalities of a microcontroller, main design procedures, and A/D conversion and
time delay, as well as some considerations in hardware and software implementation. The on-board peripherals of the PIC16C782 are suitable and critical in this implementation.

The hybrid CMC converters have been verified by experimental results. The PIC16C782 microcontroller, which provides a one-chip solution, was used as an example to control PCMC and ACMC boost converters. PI controllers and fuzzy logic controllers were designed to compensate the voltage loop in a PCMC and an ACMC boost converter. Experimental results have encouragingly demonstrated the performance that a microcontroller-based hybrid CMC converter can achieve.

Though the microcontroller-based hybrid system has only been realized on a boost converter, it can be directly applied to other power converters. All the efforts and results have proved that some advanced control methods, such as fuzzy logic control, can be realized on a microcontroller to control ACMC converters without using more expensive DSPs or other complicated hardware, provided some appropriate adjustments in hardware and software are made. Those adjustments simplify the overall hardware and software. A one-chip solution and concise program has been achieved, which imply a more reliable system.

Since this dissertation has proved the feasibility of microcontroller-based CMC systems, one obvious future work is to apply the design principles described in this dissertation to other power supply systems and power factor correction (PFC).

Many different topologies can be used in power supply systems. In this dissertation, only boost converters were realized experimentally. Other topologies, especially multiple outputs power converters, may have some special considerations
when designing the control systems. For example, the PIC16782 has two PWM outputs, so it may be a suitable solution for flyback or forward converters with multiple outputs, which are used widely in industry.

Typically, power factor correction schemes use ACMC with input voltage feedforward. That is, a typical PFC control system has three control loops: output voltage feedback loop, input voltage feedforward loop and inductor current feedback loop. Usually, an analog multiplier is required to multiply the input voltage feedforward and the compensated output voltage feedback. Therefore, its control system is relatively complicated, and it is very challenging to implement a PFC control system on a signle microcontroller. To the best of my knowledge, there is no existing PFC control system realized on a single microcontroller up to date. By using the hybrid control approach, it is possible to implement PFC on a single microcontroller. The voltage feedback loop and the current loop can be realized on the PIC16C782 as in this dissertation. The voltage feedforward loop and the multiplier can be realized by properly using the on-board DAC module. The DAC itself can be the multiplier of analog signal and digital signal, using the feedforward voltage as its reference voltage.

This dissertation also presents fuzzy logic realizations for CMC power converters. By using lookup tables and other techniques, the fuzzy logic controllers were implemented on the microcontroller successfully. However, the membership functions and various gains are obtained from previous experience with dc-dc converters and extensive experimental trials. Successful implementation of fuzzy logic control is highly empirical, and it is very time consuming to obtain appropriate membership functions and gains. Therefore, further efforts need to be put forward to determine a systematic
approach and procedure for finding the membership functions and various gains.
In this dissertation, the PIC16C782 microcontroller was selected to implement the control systems. However, this microcontroller has limited speed and computation capacity. Therefore, it is desired to find a more powerful microcontroller or DSP with appropriate analog peripherals to implement hybrid CMC power converter systems.

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